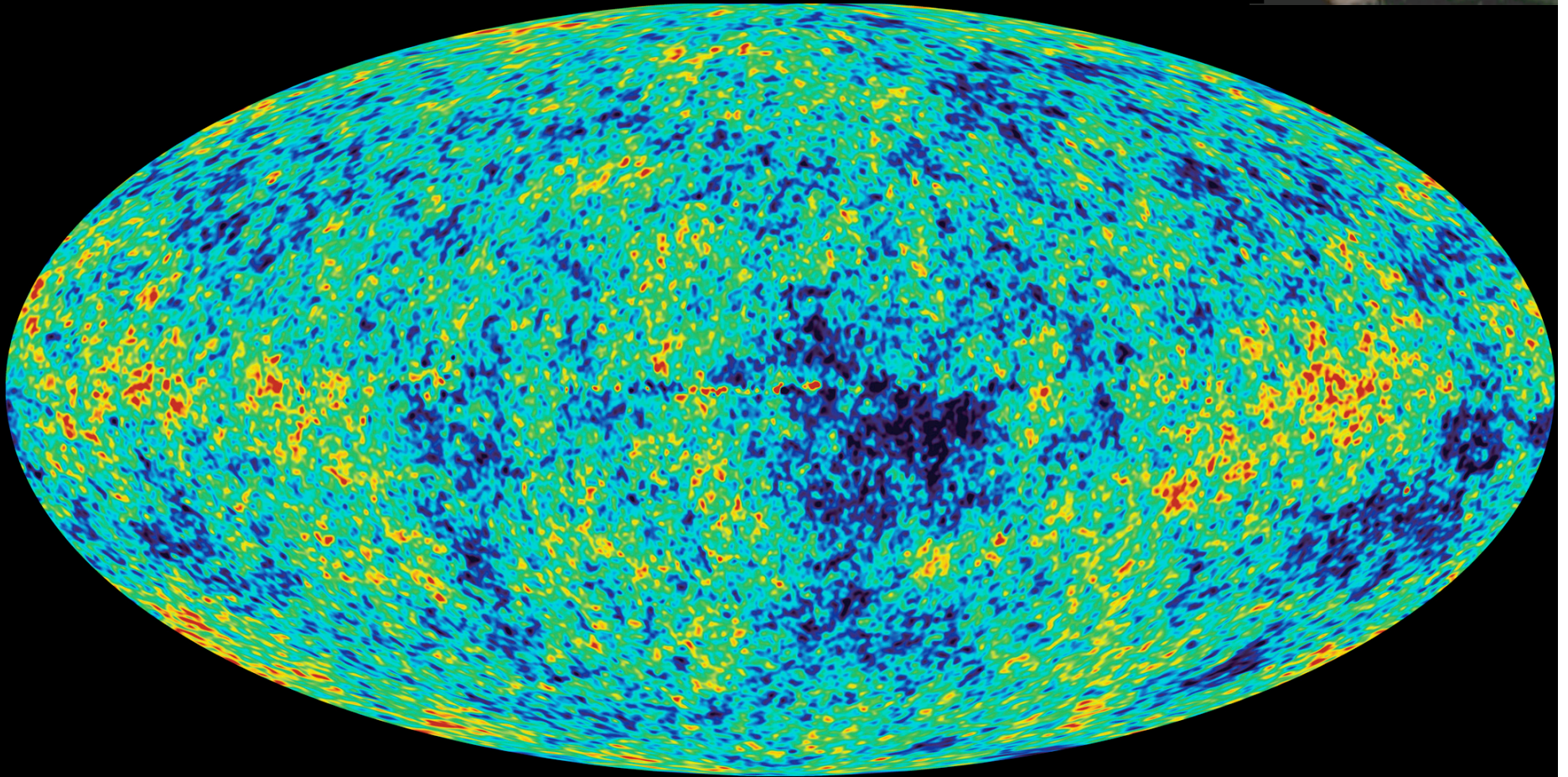
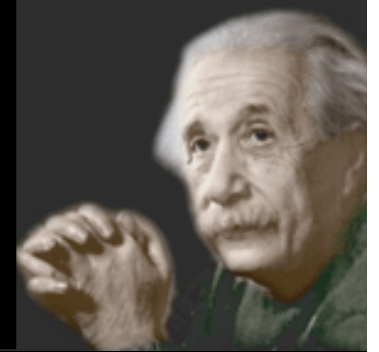
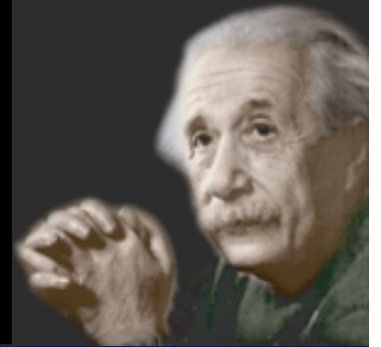


# Beyond Einstein



# 2004 Consensus Model



Hot Big Bang

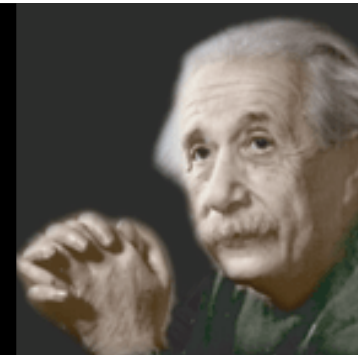
Inflation

Radiation

(Dark) Matter

Dark Energy

# Inflation: Open Issues



What causes the acceleration?

What is the inflaton?

and why are its couplings so finely tuned?

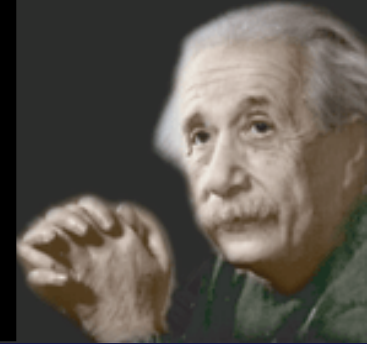
Predictions uncertain?

Transplanckian effects?

Variants?

Dark Energy?

# Inflation: What to do?



Determine if “simple”, “minimal” inflation explains our universe:

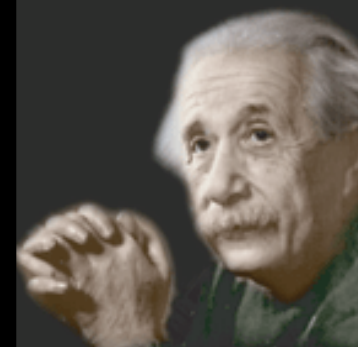
**single field**

**single characteristic mass scale**

**uniformly varying equation of state**

**minimum required fine-tuning**

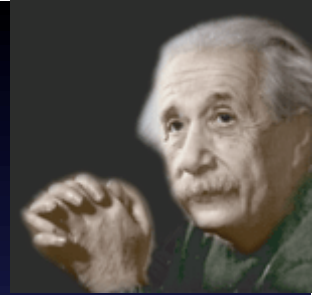
# Inflation: What to do?



Determine if “simple”, “minimal” inflation explains our universe:

CMB Anisotropy & LSS	✓?	<b>flatness</b>
	✓	<b>nearly scale-invariant spectrum</b>
	✓?	<b>adiabaticity</b>
	✓??	<b>gaussianity</b>
CMB Pol		<b>spectral tilt (<math>n_s \sim 0.95</math>)</b>
		<b>gravitational waves (T/S <math>\sim 20-30\%</math>)</b>

# Density Fluctuation amplitude



$$\frac{\delta\rho}{\rho} \sim \frac{H^2}{\dot{\phi}} \quad \left| \quad \sim \frac{M^2}{\sqrt{1+w}} \sim 10^{-5}$$

With  $N \sim 60$   
e-folds to go

in Planck units

energy scale  
for inflation:

$$M \approx 10^{-5/2} (1+w)^{1/4} \sim 10^{(15-16)} \text{ GeV}$$

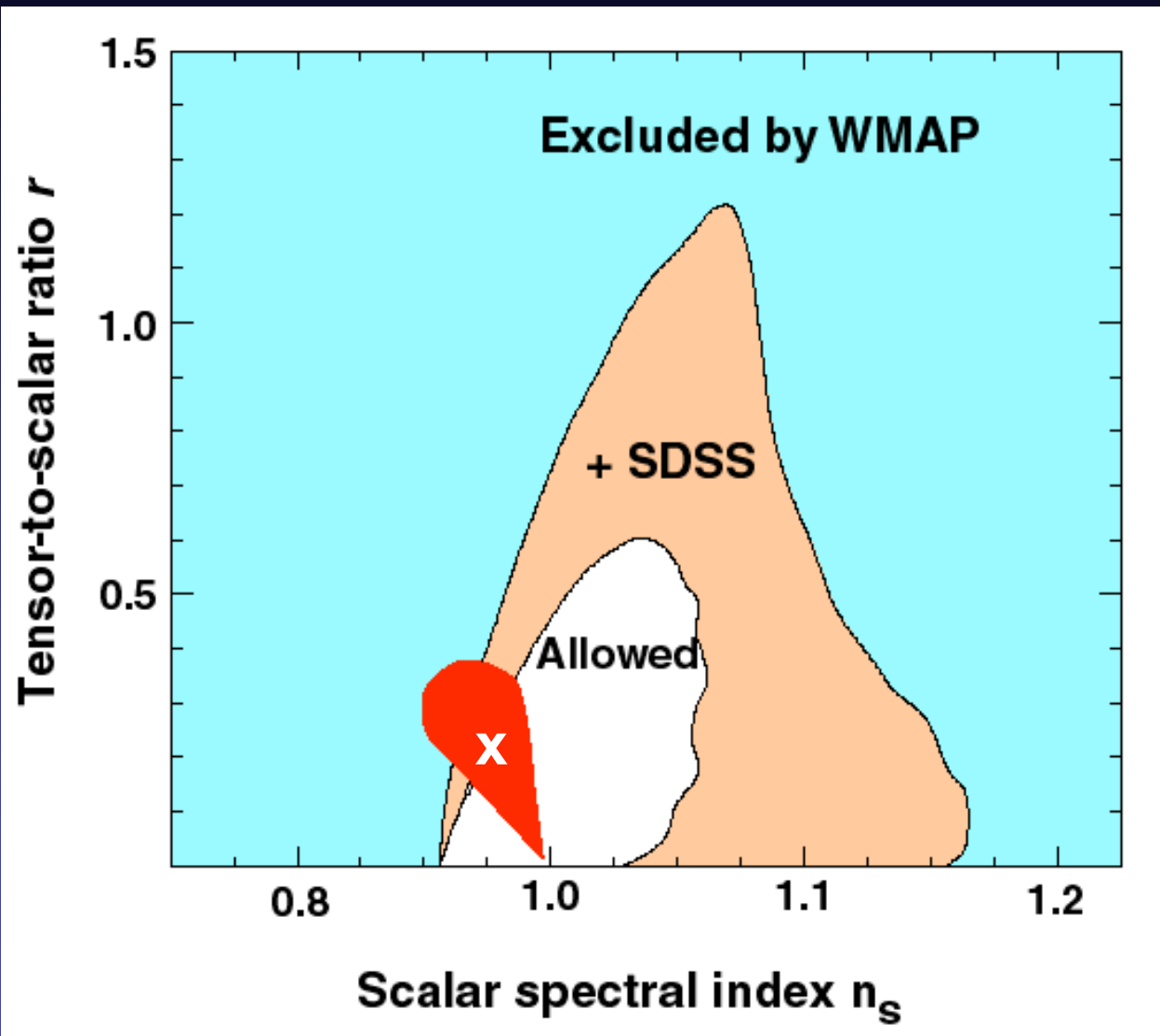
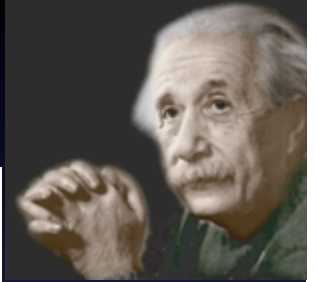
With  $N \sim 60$  e-folds to go,  $(1+w) \sim \frac{1}{N} \sim \frac{1}{60}$

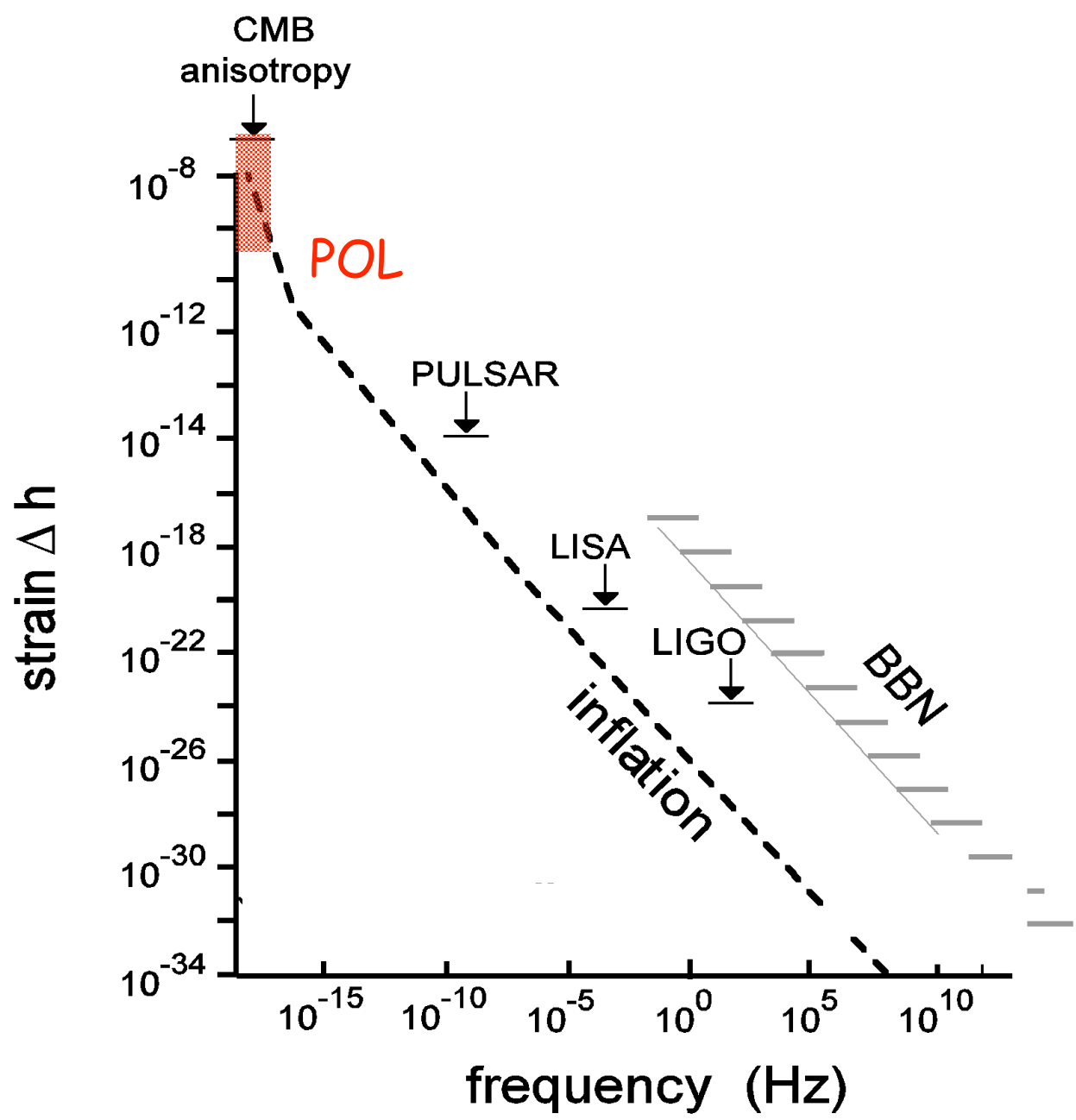
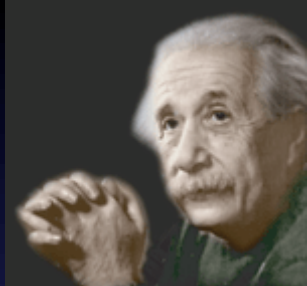
tilt:

$$n_s - 1 \approx -3(1+w) \sim 0.05$$

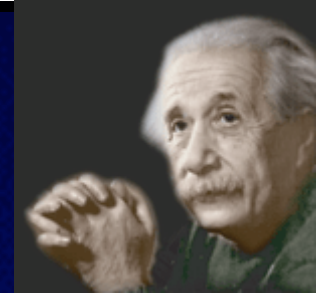
$$r \equiv \frac{\text{tensor}}{\text{scalar}} = 12(1+w) = 20\%$$

Based on M. Tegmark, et al, astro-ph/030173

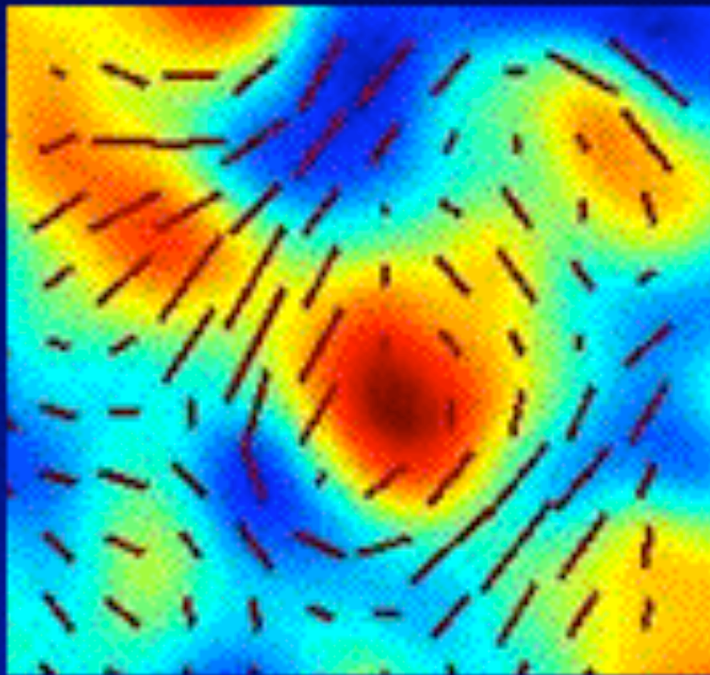




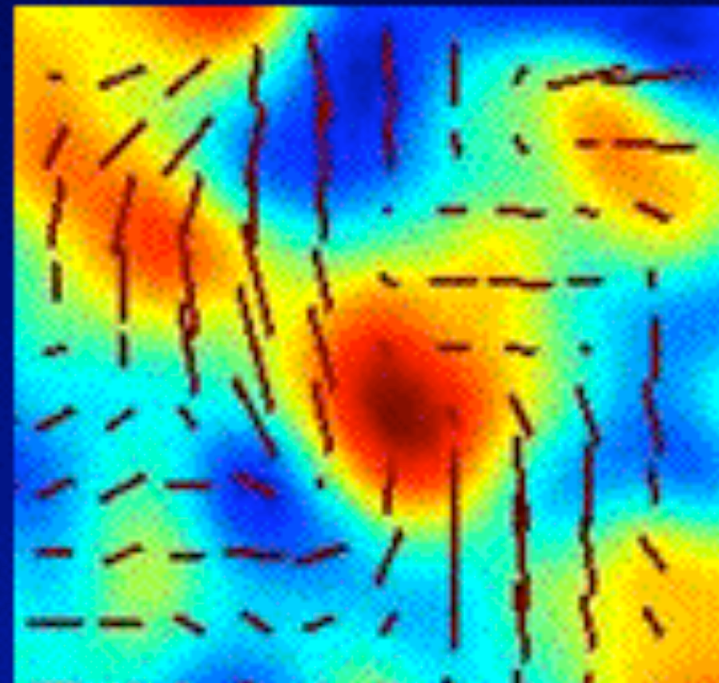




E-mode  
(energy density fluctuations)

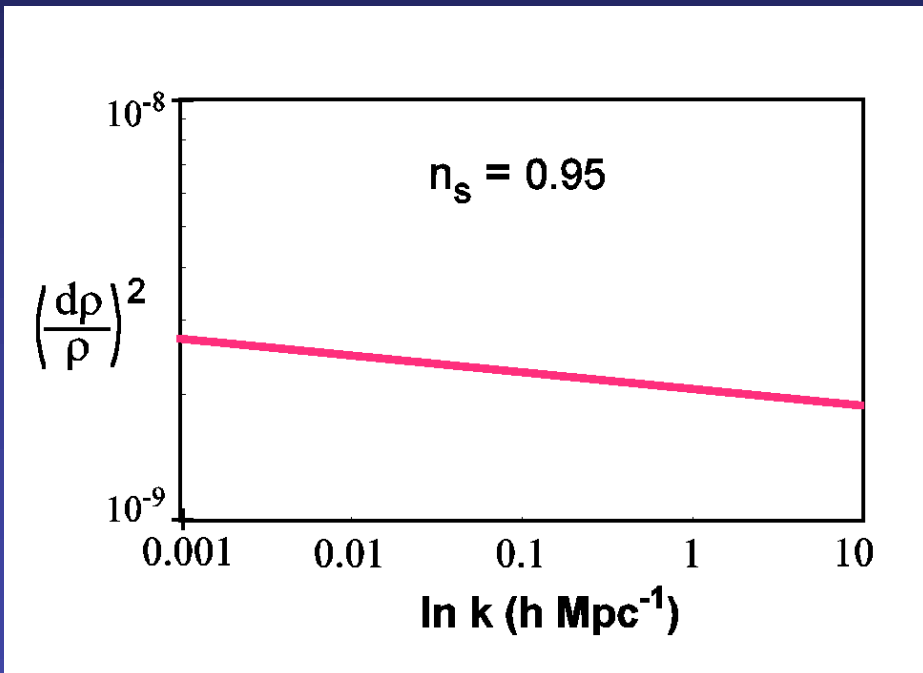
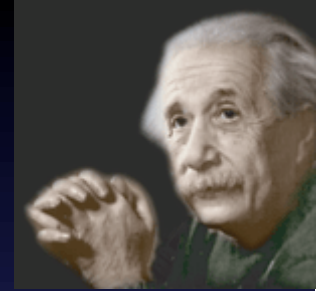


B-mode  
(gravitational waves)

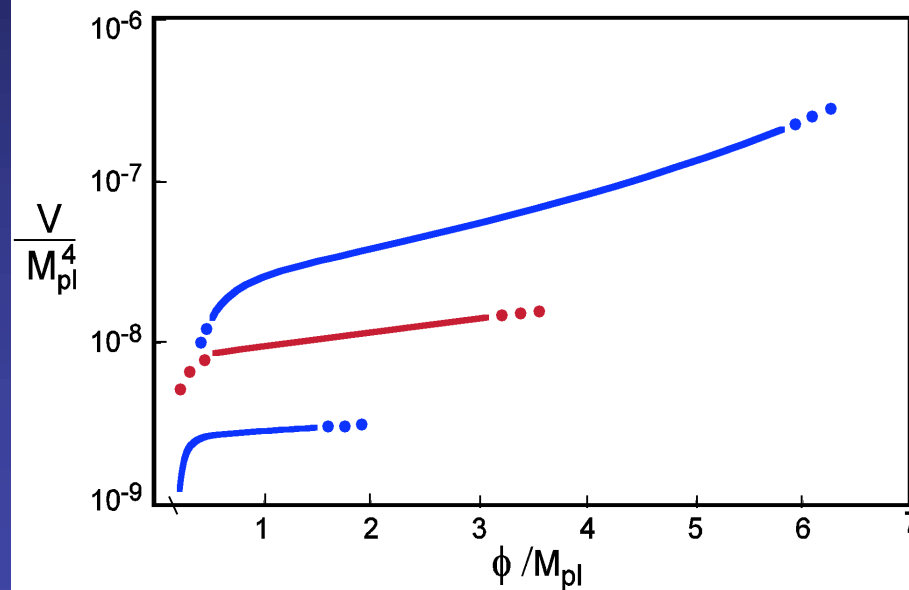
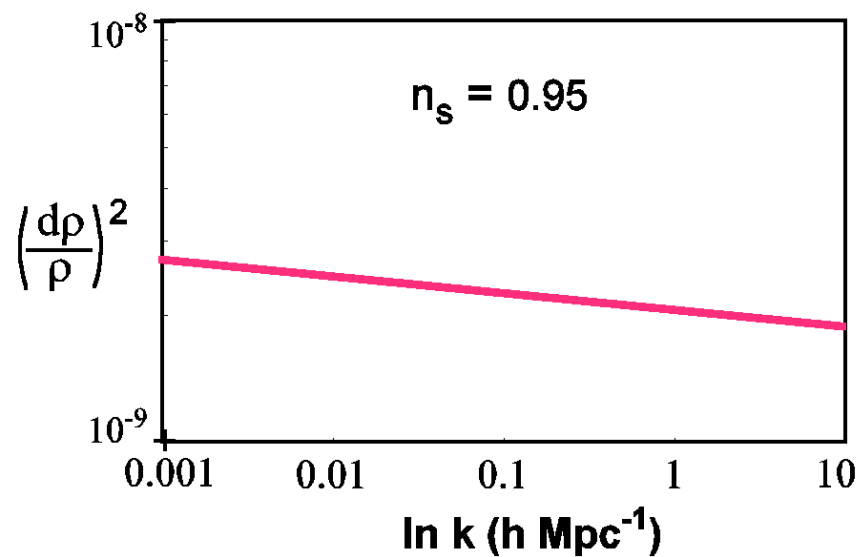
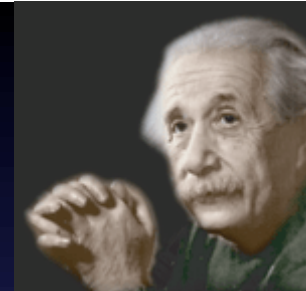


from U. Seljak & M. Zaldarriaga

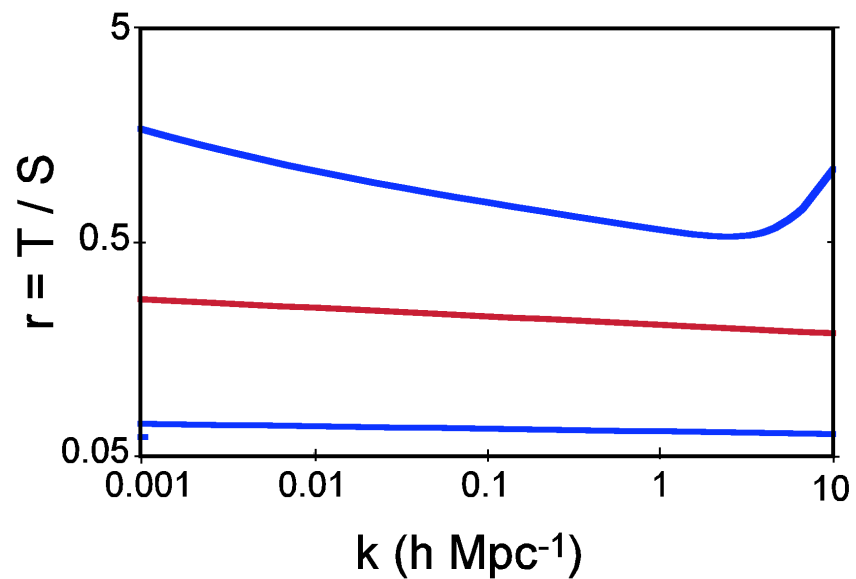
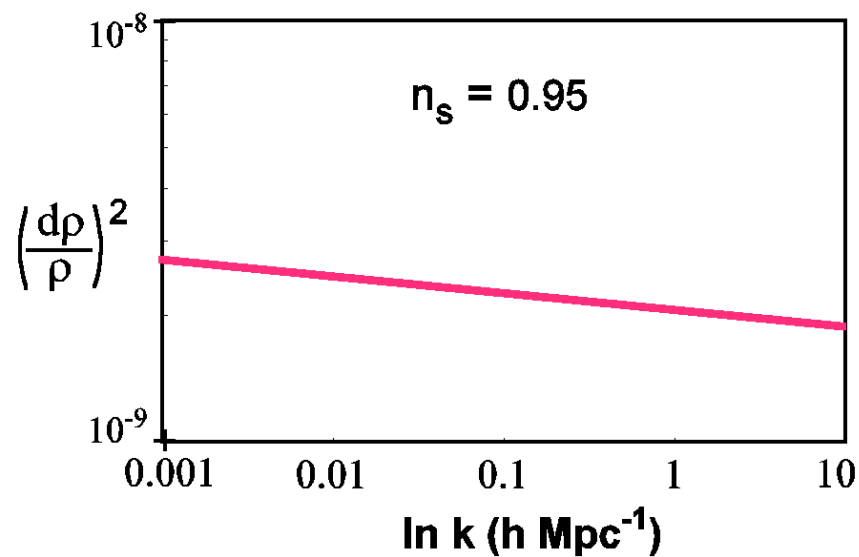
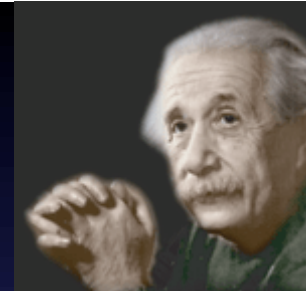
# G-waves & The Degeneracy Problem



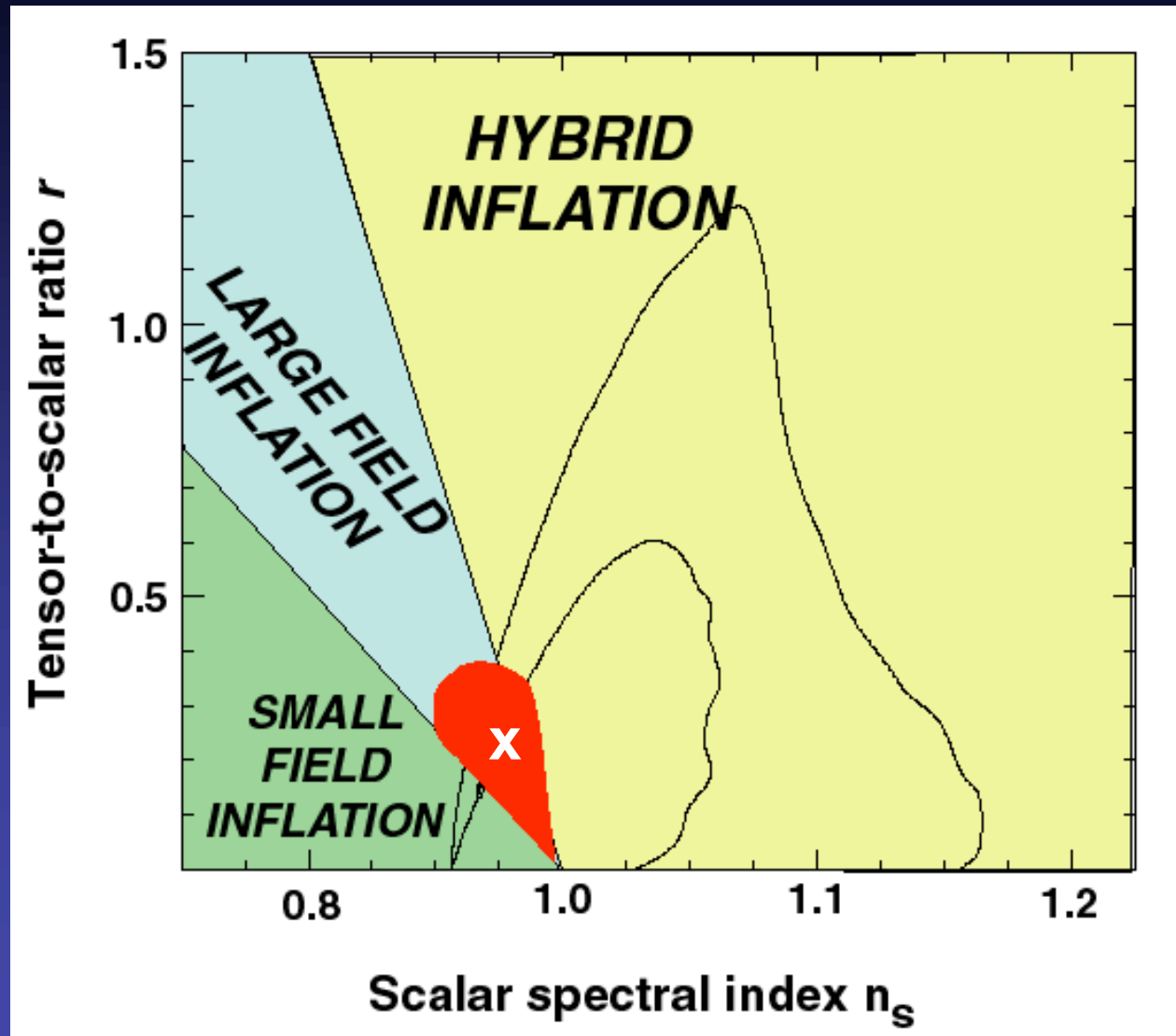
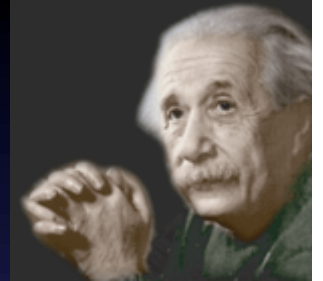
# G-waves & The Degeneracy Problem



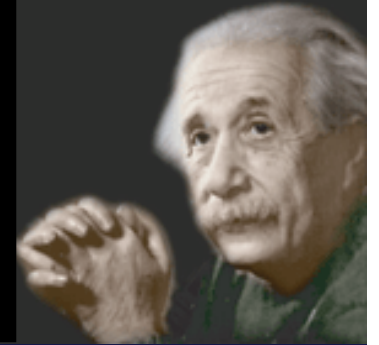
# G-waves & The Degeneracy Problem



# What if one or more tests fail ?



# Inflation



## “Non-Minimal” Inflation?

**flatness**

**nearly scale-invariant spectrum**

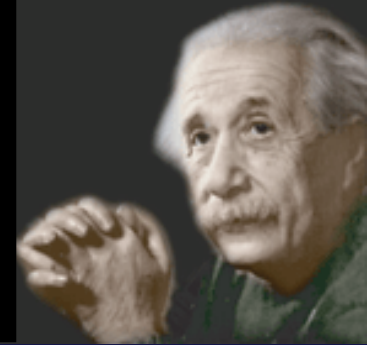
**adiabatic**

**gaussianity**

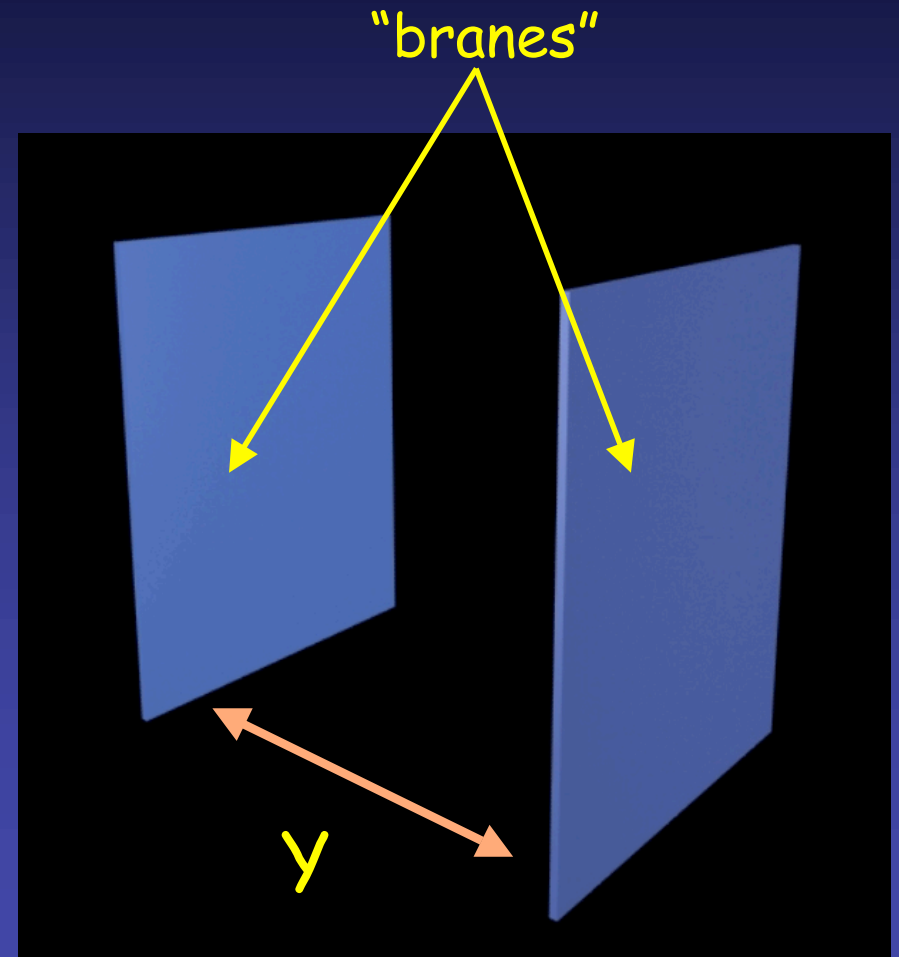
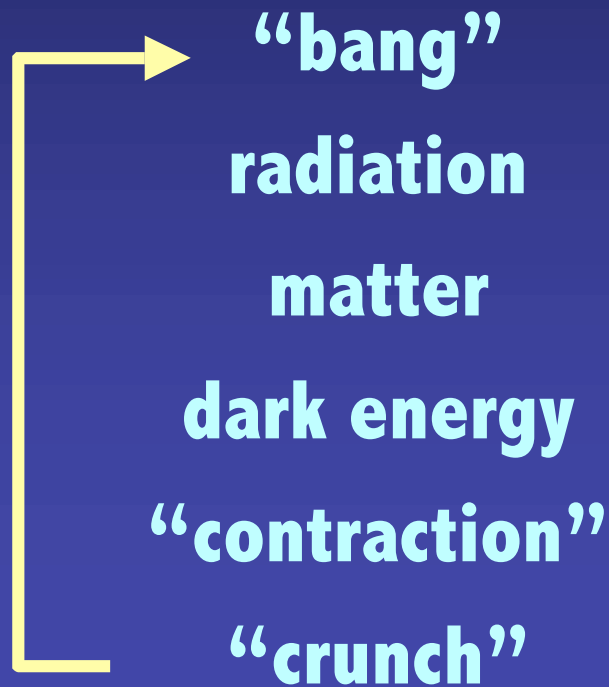
**spectral tilt ( $n_s \sim 0.95$ )**

**gravitational waves ( $T/S \sim 20-30\%$ )**

# Alternative ?

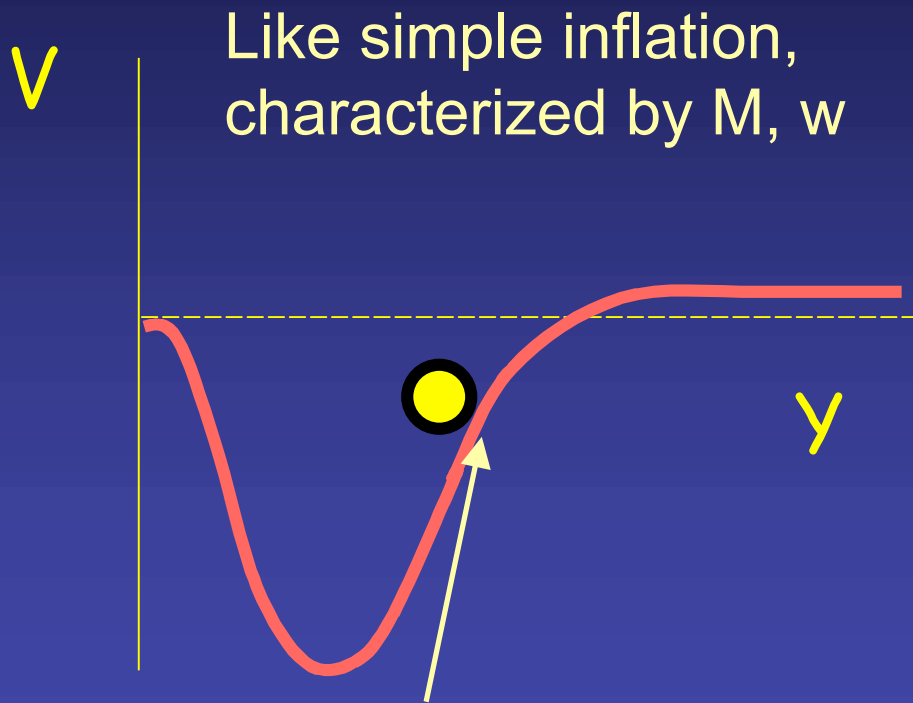
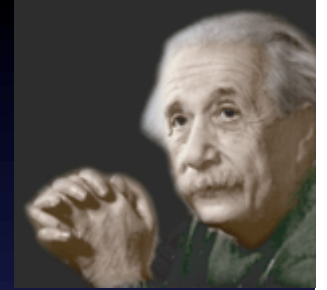


## Cyclic Model

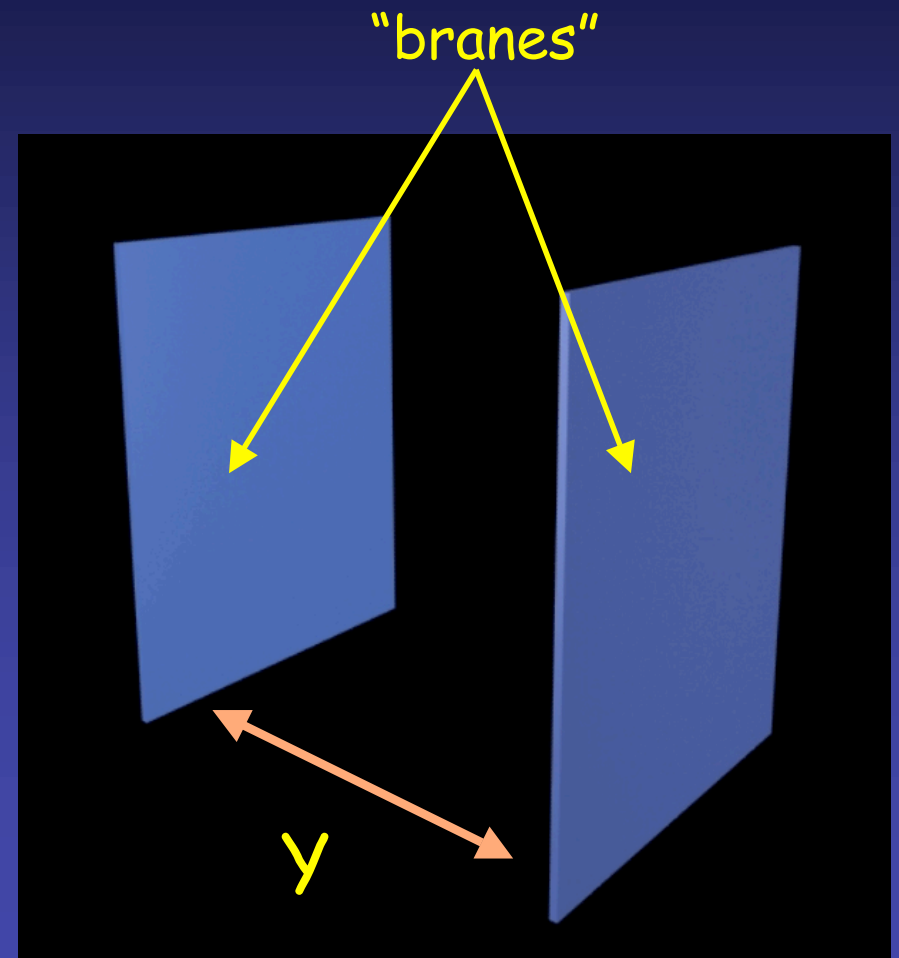


Superstring theory

# Cyclic Model

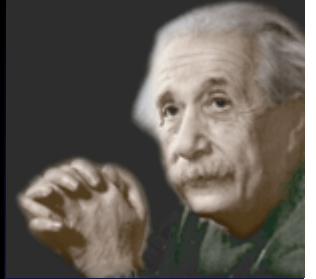


$$w = \frac{KE - PE}{KE + PE} > 1$$





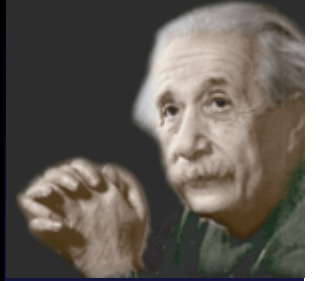
# INFLATION



***$w < -1/3$ : homogeneity, isotropy, flatness***

$$H^2 = \frac{8\pi G}{3} \frac{\rho_m^0}{a^3} + \frac{8\pi G}{3} \frac{\rho_r^0}{a^4} + \frac{\sigma^2}{a^6} + \dots \left( - \frac{k}{a^2} \right)$$

# INFLATION

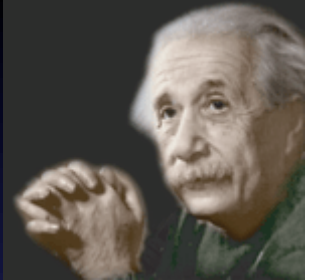


**$w < -1/3$ : homogeneity, isotropy, flatness**

$$H^2 = \frac{8\pi G}{3} \frac{\rho_m^0}{a^3} + \frac{8\pi G}{3} \frac{\rho_r^0}{a^4} + \frac{\sigma^2}{a^6} + \dots - \frac{k}{a^2}$$

$$+ \frac{8\pi G}{3} \frac{\rho_{\text{infl}}}{a^{3(1+w)}} \leftarrow 3(1+w) < 2$$

# CYCLIC

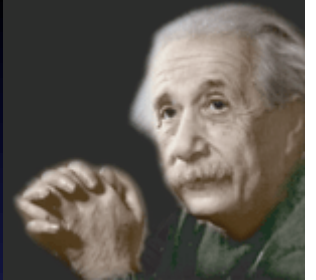


***w > 1: homogeneity, isotropy, flatness***

contraction

$$H^2 = \frac{8\pi G}{3} \frac{\rho_m^0}{a^3} + \frac{8\pi G}{3} \frac{\rho_r^0}{a^4} + \left( \frac{\sigma^2}{a^6} \right) + \dots - \frac{k}{a^2} + \Lambda$$

# CYCLIC



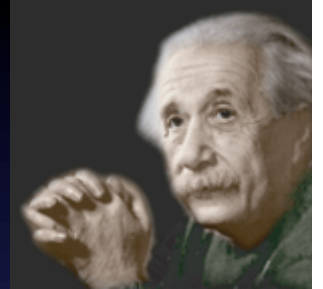
**$w > 1$ : homogeneity, isotropy, flatness**

contraction

$$H^2 = \frac{8\pi G}{3} \frac{\rho_m^0}{a^3} + \frac{8\pi G}{3} \frac{\rho_r^0}{a^4} + \frac{\sigma^2}{a^6} + \dots - \frac{k}{a^2} + \Lambda$$

$$+ \frac{8\pi G}{3} \frac{\rho_\phi^0}{a^{3(1+w)}} \leftarrow w > 1$$

# *scale-invariant perturbations*



*approach: quantum fluct. exit horizon & re-enter later*

$$\varepsilon \equiv \frac{3}{2}(1+w) \qquad a(t) \sim t^{\frac{1}{\varepsilon}} \sim (H^{-1})^{\frac{1}{\varepsilon}}$$

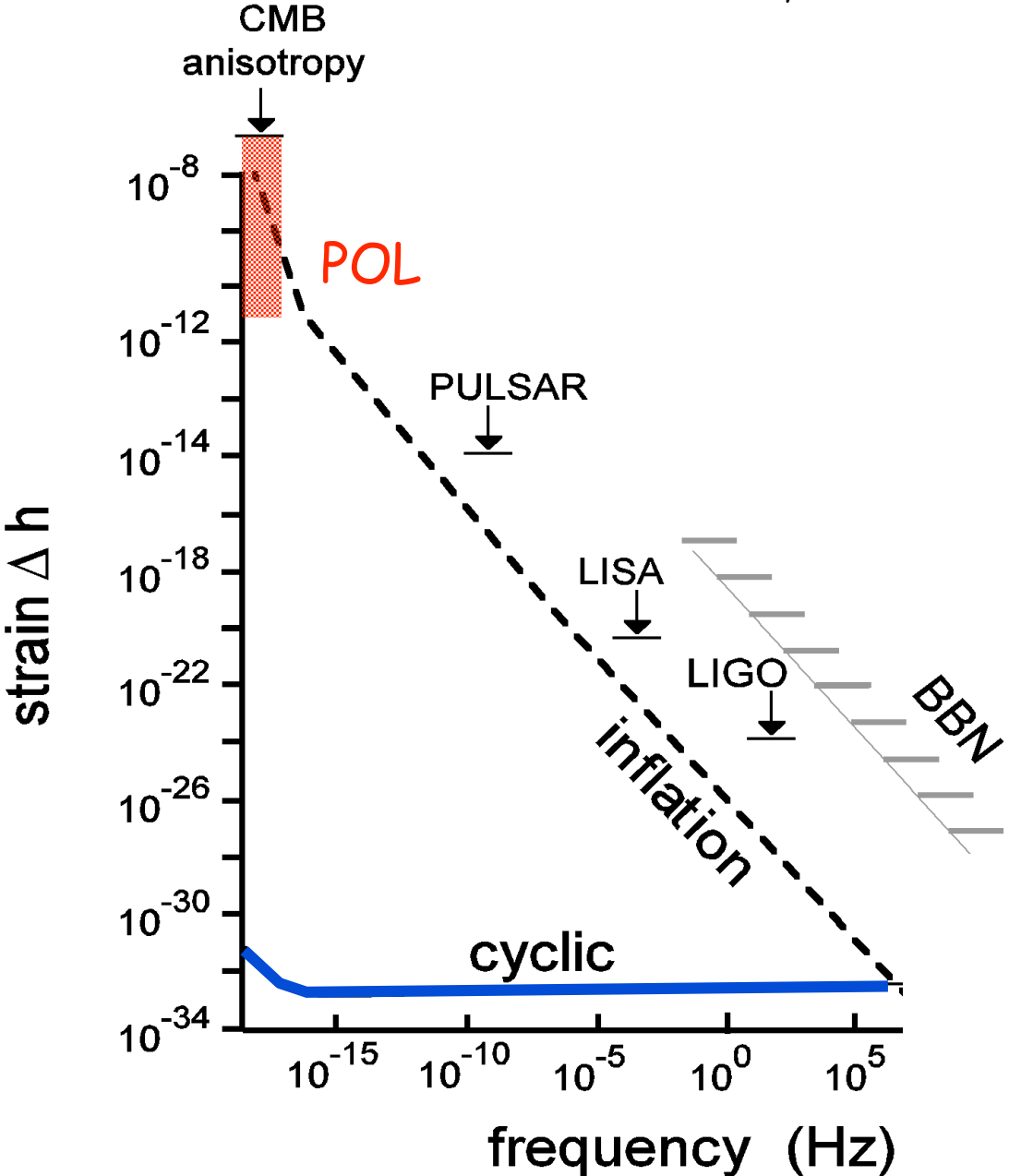
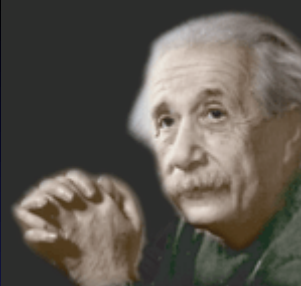
expanding

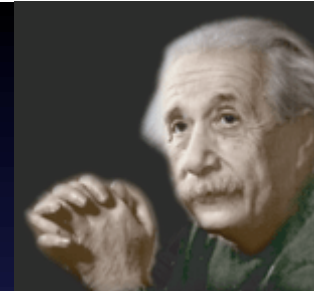
contracting

$$\varepsilon \ll 1 \quad \left\langle \begin{array}{c} \text{"dual"} \\ \varepsilon \rightarrow 1/\varepsilon \end{array} \right\rangle \quad \varepsilon \gg 1 \quad (\text{or } w \gg 1)$$

Another Degeneracy Problem !

From L. Boyle, PJS, N. Turok, astro-ph/0310533





Cyclic

Inflation

Gravitational  
Waves

**Very Blue**

**Slightly Red**

Non-gaussianity

**Never**

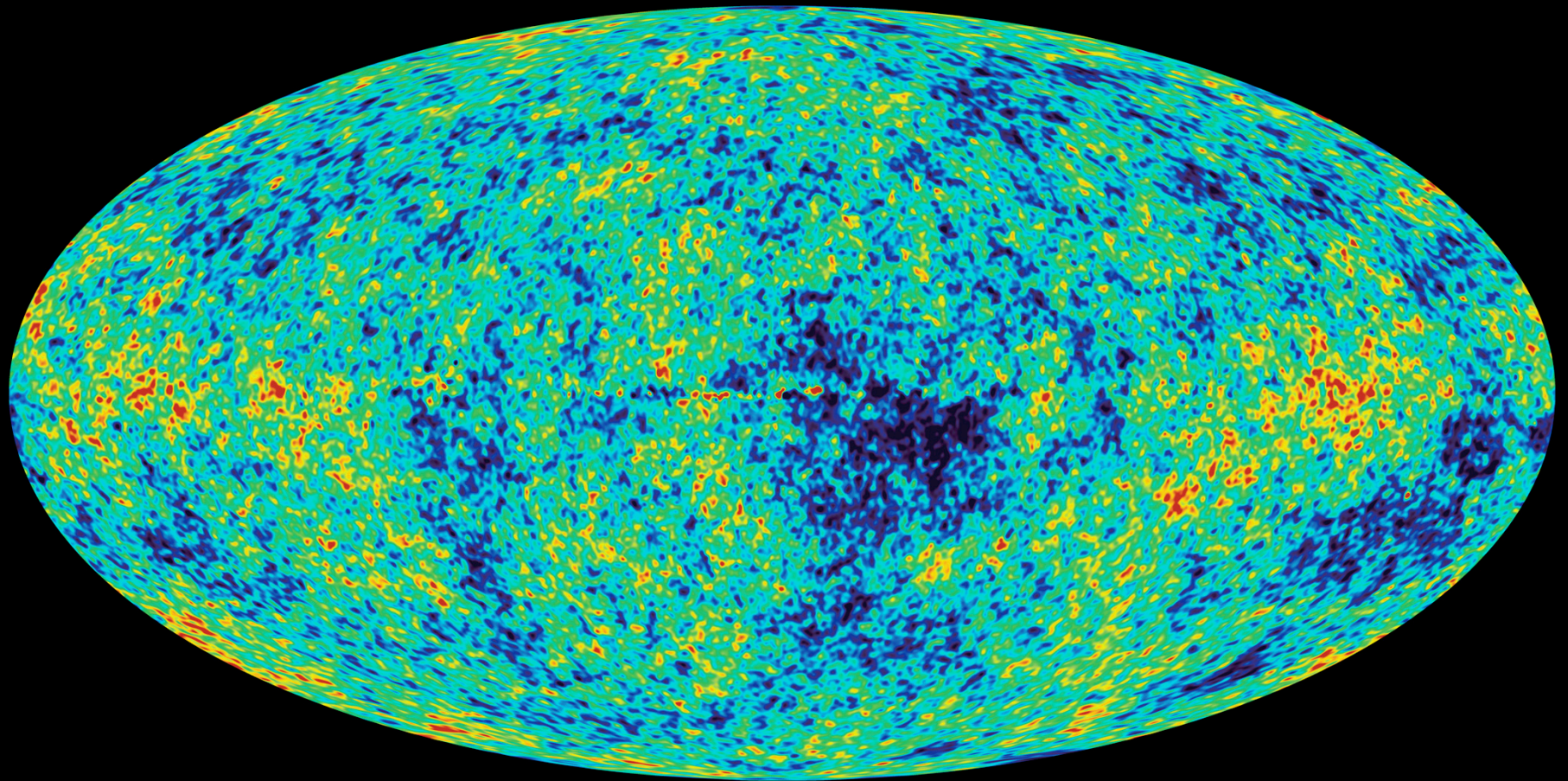
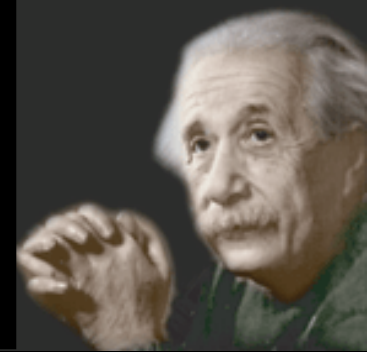
**Small  
to Moderate**

Non-adiabaticity

**Never**

**Some models**

# Beyond Einstein



What does this pattern represent?