Transverse-momentum resummation

# Polarization and resummation for slepton-pair hadroproduction

#### Benjamin Fuks (LPSC Grenoble)

in collaboration with Giuseppe Bozzi and Michael Klasen [Phys. Lett. B609, 339 (2005) and hep-ph/0603074]

> LoopFest V SLAC (California), June 19-21, 2006

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Introduction	and	Motivations

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# Outline

- Introduction and Motivations
  - The Minimal Supersymmetric Model
  - Slepton production at hadron colliders
  - Tau slepton identification
  - Importance of transverse-momentum distribution
- 2 Fixed order calculations
  - Leading order
  - Next-to-leading order
  - Fixed order failure
- 3 Transverse-momentum resummation
  - Main features
  - The resummed component
  - The finite component
  - Non-perturbative effects
  - $q_T$ -resummation for slepton-pair production at the LHC

## Conclusions

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# The Minimal Supersymmetric Model

#### Main features

- High energy extension to Standard Model.
- Symmetry between fermions and bosons.
- One SUSY partner for each SM particle.
- 5 Higgs bosons.
- R-parity conservation.

#### Advantages

- Gauge couplings unification at Planck scale.
- Possible inclusion of gravity.
- Solution to hierarchy problem.
- Dark matter candidate.
- New CP-violation phases.

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## Why study slepton production ?

- Due to their purely electroweak couplings, sleptons are among the lightest SUSY particles in many SUSY-breaking scenarios.
   [Allanach et al., Eur. Phys. J. C25, 113 (2002)]
- Often directly decays into the lightest SUSY particle (LSP) plus the corresponding standard model partner (lepton or neutrino).
- Clean signal with a highly energetic lepton and missing energy.

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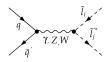
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# Slepton production at hadron colliders



 $q\bar{q} \rightarrow \tilde{l}_i \tilde{l}_j^*$ :

- slepton-pair production
- neutral current

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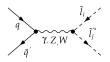
- slepton-sneutrino associated production
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#### We focus on tau slepton and sneutrino. Why?

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### Third generation slepton and sneutrino properties

 In general SUSY-breaking models, interaction eigenstates are not identical to mass eigenstates

$$\begin{pmatrix} \tilde{l}_1 \\ \tilde{l}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{\tilde{l}} & \sin \theta_{\tilde{l}} \\ -\sin \theta_{\tilde{l}} & \cos \theta_{\tilde{l}} \end{pmatrix} \begin{pmatrix} \tilde{l}_L \\ \tilde{l}_R \end{pmatrix} ,$$

where

$$\tan 2\theta_{\tilde{l}} = \frac{2 m_l m_{LR}}{m_{LL}^2 - m_{RR}^2}$$

[Haber, Kane, Phys. Rept. 117, 75 (1985)]

- Mixing proportional to corresponding lepton mass ⇒ only important for third generation.
- Third generation SUSY particles are lighter  $\Rightarrow$  more easily produced.

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## Are tau sleptons detectable ?

Tau slepton often decays in one tau lepton plus one neutralino  $\Rightarrow$  tau tagging at hadron colliders ?

- Leptonic decays (35%): isolated muons or electrons plus ∉<sub>T</sub> ⇒ Limited use (origin of the lepton unknown).
- Hadronic decays (65%): narrow isolated jet with low track multiplicity and invariant mass, plus *φ<sub>τ</sub>*.
- Require significant  $q_T$ .
- Atlas: [Hinchliffe, Nucl. Phys. Proc. Suppl. 123, 229 (2003)]
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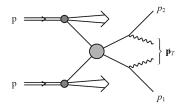
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### Importance of transverse-momentum distribution

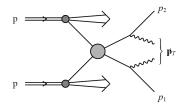
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- Longitudinal momentum balance unknown in hadronic collision
   ⇒ importance of a precise knowledge of the q<sub>T</sub>-balance.
- Can be used to distinguish SUSY signals from SM background (lepton-pairs from WW or  $t\bar{t}$  decays have a different  $q_T$ -shape) [Andreev, Bityukov, Krasnikov, Phys. Atom. Nucl. 68, 340 (2005)]



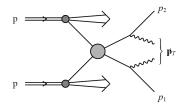
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### Transverse mass variables

Problem: We have two massive particles carrying missing momentum.

Solution: use of the Cambridge stransverse mass  $M_{T2}^2$ 

$$m_{T}^{2}(\mathbf{q}_{T}^{\prime}, \mathbf{q}_{T}^{\tilde{\chi}}) = m_{I}^{2} + m_{\tilde{\chi}}^{2} + 2\left(E_{T}^{\prime} E_{T}^{\tilde{\chi}} - \mathbf{q}_{T}^{\prime} \cdot \mathbf{q}_{T}^{\tilde{\chi}}\right)$$
$$m_{T2}^{2} = \min_{\mathfrak{g}_{1} + \mathfrak{g}_{2} = \mathfrak{g}_{T}}\left[\max\left\{m_{T}^{2}(\mathbf{q}_{T}^{\prime -}, \mathbf{q}_{T}^{1}), m_{T}^{2}(\mathbf{q}_{T}^{\prime +}, \mathbf{q}_{T}^{2})\right\}\right]$$
$$m_{T2}^{2} \leq m_{I}^{2}$$

- More realistic: relationship between neutralino and slepton masses. [Lester, Summers, Phys. Lett. B463, 99 (1999)]
- Bonus: can be used for spin determination.

[Barr, JHEP 0602, 042 (2006)]

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LO cross section and mixing effects for  $h_1 h_2 \rightarrow \hat{l}_i \hat{l}_i^*$ 

$$\begin{split} \frac{\mathrm{d}\hat{\sigma}_{h_a,h_b}}{\mathrm{d}t} &= \frac{4\pi\alpha^2}{3s^2} \Bigg[ \frac{u\,t - m_i^2 m_j^2}{s^2} \Bigg] \Bigg[ e_q^2 \, e_l^2 (1 - h_a h_b) \, \frac{\delta_{ij}}{2} \\ &+ \frac{e_q \, e_l \, \mathrm{Re}(L_l + R_l) \, [(1 - h_a) \, (1 + h_b) \, L_q + (1 + h_a) \, (1 - h_b) \, R_q] \, \delta_{ij}}{8 \, x_W \, (1 - x_W) \, (1 - m_Z^2/s)} \\ &+ \frac{|L_l + R_l|^2 [(1 - h_a) \, (1 + h_b) \, L_q^2 + (1 + h_a) \, (1 - h_b) \, R_q^2]}{64 \, x_W^2 (1 - x_W)^2 (1 - m_Z^2/s)^2} \Bigg] \,, \end{split}$$

with

$$L_{I} = (2 T_{f}^{3} - 2 e_{f} x_{W}) \frac{S_{i1} S_{j1}^{*}}{S_{j1}^{*}} \text{ and } R_{I} = (-2 e_{f} x_{W}) \frac{S_{i2} S_{j2}^{*}}{S_{j2}^{*}}.$$

- No mixing matrix S for sneutrino  $(S_{11}=1, \text{ and all others } S_{ij}=0)$ .
- For charged current, all right couplings and electric charges are set to zero, and  $L_l$  is set to  $\sqrt{2} \cos \theta_W S_{i1}$ .

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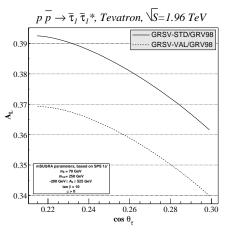
$$L_I = (2 T_f^3 - 2 e_f x_W) \frac{S_{i1} S_{j1}^*}{S_{j1}^*}$$
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Fixed order calculations

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## Leading order: Single-spin asymmetry and mixing effects



[Bozzi, BF, Klasen, Phys. Lett. B609, 339 (2005)]

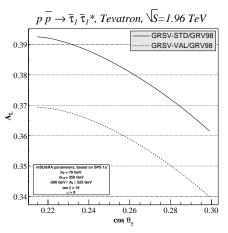
- Sensitive to the mixing angle (7% 8%).
- PDF uncertainties are still large (5% 6%).
  - Lepton-pair production:  $A_L \approx -0.09$  $\Rightarrow$  discrimination SUSY/SM.
- Missing: an upgraded Tevatron with one polarized beam. [SPIN collaboration, 10th Topical Workshop on Proton-Antiproton Collider Physics (1995)]

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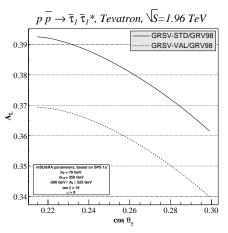
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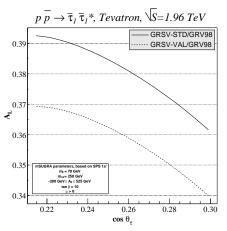
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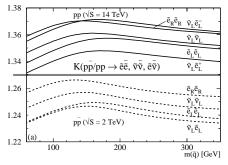
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## Next-to-leading order K factor

QCD: [Baer, Harris, Reno, Phys. Rev. D 57, 5871 (1998)]

SUSY-QCD: [Beenakker, Klasen, Kramer, Plehn, Spira, Zerwas, Phys. Rev. Lett. 83, 3780 (1999)]



- K factors for slepton-pair in NLO SUSY-QCD not too different from QCD only.
- NLO contributions not negligible ( $\sim$  35% for the LHC and  $\sim$  25% for Tevatron)

Importance of higher order calculations.

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Fixed order calculations

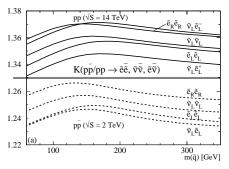
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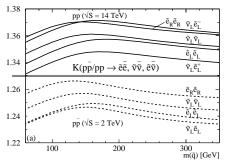
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## Fixed order failure at low $q_T$

#### $q_T$ -distribution features.

 Soft and collinear radiation enhance the cross section by powers of logarithmic terms ∝ <sup>α<sup>s</sup><sub>s</sub></sup>/<sub>q<sup>2</sup><sub>T</sub></sub> log<sup>m</sup> <sup>Q<sup>2</sup></sup>/<sub>q<sup>2</sup><sub>T</sub></sub> (m ≤ 2 n − 1).

• Cross section diverges as  $q_T \rightarrow 0$ .

- Higher order contributions increase the divergence.
- Fixed order theory convergence definitely spoiled.

Why?

- Real and virtual contributions highly unbalanced.
- Cancellation does not occur order by order.

 $\Rightarrow$  Resummation to all orders needed for reliable perturbative results.

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- Soft and collinear radiation enhance the cross section by powers of logarithmic terms  $\propto \frac{\alpha_s^n}{q_\tau^2} \log^m \frac{Q^2}{q_\tau^2}$   $(m \le 2 n 1)$ .
- Cross section diverges as  $q_T \rightarrow 0$ .
- Higher order contributions increase the divergence.
- Fixed order theory convergence definitely spoiled.

#### Why?

- Real and virtual contributions highly unbalanced.
- Cancellation does not occur order by order.
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Introduction	and	Motivations

Fixed order calculations

Transverse-momentum resummation

# Outline

- Introduction and Motivations
  - The Minimal Supersymmetric Model
  - Slepton production at hadron colliders
  - Tau slepton identification
  - Importance of transverse-momentum distribution
- 2 Fixed order calculations
  - Leading order
  - Next-to-leading order
  - Fixed order failure
- 3 Transverse-momentum resummation
  - Main features
  - The resummed component
  - The finite component
  - Non-perturbative effects
  - $q_T$ -resummation for slepton-pair production at the LHC

### Conclusions

Introduction and Motivations	Fixed order calculations	Transverse-momentum resummation	Conclusions
Main features			

#### Reorganization of the cross section

$$\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2} = \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{res}} + \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{fin}}$$

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- Contains all the logarithmic terms.
- Contains all the terms proportional to  $\delta(q_T)$ .
- Resummation to all orders in  $\alpha_s$ .
- Exponentiation  $\Rightarrow$  finite term.
- $\left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{fin}}$  is free of these contributions.

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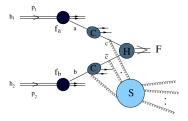
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Transverse-momentum resummation

#### Ingredients for resummation

Universal resummation formalism developed by Bozzi, Catani, de Florian, Grazzini. [Catani, de Florian, Grazzini, Nucl. Phys. B 596, 299 (2001)]



- process-independent coefficient functions  $C_{ac}$  (collinear radiation at very low  $q_T$ ),
- process-independent Sudakov form factor S<sub>c</sub> (soft radiation, and collinear radiation at intermediate q<sub>T</sub>),
- process-dependent factor  $H_c^F$  (hard contributions at  $q_T \sim Q$ ).

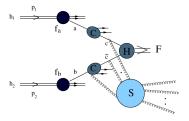
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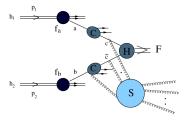
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#### The resummed component

$$\begin{bmatrix} \frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2} \end{bmatrix}_{\mathrm{res}} (q_T, Q, \mathbf{s}) = \sum_{a,b} \int_0^1 \mathrm{d}x_1 \int_0^1 \mathrm{d}x_2 f_{a/h_1}(x_1, \mu_F) f_{b/h_2}(x_2, \mu_F) \\ \times \left[ \frac{\mathrm{d}\sigma_{ab}}{\mathrm{d}q_T^2} \right]_{\mathrm{res}} (q_T, Q, \hat{\mathbf{s}}; \mu_R, \mu_F)$$

$$\left[\frac{\mathrm{d}^2\sigma_{ab}}{\mathrm{d}q_T^2}\right]_{\mathrm{res}}(q_T,Q,\hat{s};\mu_R,\mu_F) = \frac{Q^2}{\hat{s}}\int\frac{b}{2}\,\mathrm{d}b\,J_0(b\,q_T)\,\mathcal{W}^F_{ab}(b,Q,\hat{s};\mu_R,\mu_F)\;.$$

 $\mathcal{W}^{\mathsf{F}}_{\mathsf{ab}}$  contains all previously cited contributions, plus PDFs evolution.

- In the original impact-parameter space formula, the PDFs are evaluated at the scale  $b_0/b$ .
- $\Rightarrow$  involves an extrapolation of the PDFs in the non-perturbative region.
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#### N-space and exponentiation

Computation of  $\mathcal{W}_{ab}^{\mathcal{F}}$  in *N*-space  $\Rightarrow$  exponentiation.

$$\mathcal{W}_{ab,N}^{F}(b,Q;\mu_{R},\mu_{F}) = \mathcal{H}_{ab,N}^{F}(Q;\frac{Q^{2}}{\mu_{R}^{2}},\frac{Q^{2}}{\mu_{F}^{2}})\exp[\mathcal{G}_{N}(L \equiv \log\frac{Q^{2}b^{2}}{b_{0}^{2}};\frac{Q^{2}}{\mu_{R}^{2}})]$$

$$\mathcal{G}_{N}(L;\frac{Q^{2}}{\mu_{R}^{2}}) = Lg^{(1)}(\alpha_{s}L) + \sum_{n=2}^{\infty} \left(\frac{\alpha_{s}}{\pi}\right)^{n-2}g_{N}^{(n)}(\alpha_{s}L;\frac{Q^{2}}{\mu_{R}^{2}})$$

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• At large  $q_T$  (small b):

- Usual perturbation theory is valid.
- Use of the resummation is not justified.

•  $L \rightarrow \tilde{L} \equiv \log \left( \frac{Q^2 b^2}{b_0^2} + 1 \right)$  to reduce resummation impact at large- $q_T$ .

• Does not change anything at large b:  $\tilde{L} = L + O(1/(b^2 Q^2))$ .

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The finite com	onent		

- Logarithmic terms and contributions proportional to δ(q<sub>T</sub>) are included in the resummed component.
  - $\Rightarrow \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_{T}^{2}}\right]_{\mathrm{fin}} \text{ can be computed by}$

$$\left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{fin}} = \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{f.o.}} - \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{res}}\Big|_{\mathrm{f.o.}}.$$

•  $\left\lfloor \frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2} \right\rfloor_{\mathrm{f.o.}}$  is evaluated at a specific order of the perturbation theory.

•  $\left[\frac{d\sigma}{dq_T^2}\right]_{res} |_{f.o.}$  is the expansion of the resummed component at the same order.

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Introduction and Motivations	Fixed order calculations	Transverse-momentum resummation ○○○○○●○○○	Conclusions
The finite comr	onent		

 Logarithmic terms and contributions proportional to δ(q<sub>T</sub>) are included in the resummed component.

 $\Rightarrow \left[ rac{\mathrm{d}\sigma}{\mathrm{d}q_T^2} 
ight]_{\mathrm{fin}}$  can be computed by

$$\left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{fin}} = \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{f.o.}} - \left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{res}}\Big|_{\mathrm{f.o.}}.$$

•  $\left[\frac{\mathrm{d}\sigma}{\mathrm{d}q_T^2}\right]_{\mathrm{f.o.}}$  is evaluated at a specific order of the perturbation theory.

•  $\left[\frac{d\sigma}{dq_7^2}\right]_{res}\Big|_{f.o.}$  is the expansion of the resummed component at the same order.

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### Summary

- At small  $q_T$ , the resummed component dominates, and the finite term is small.
- At intermediate q<sub>T</sub>, both contributions are consistently matched and double-counting of any term is prevented.
- At large  $q_T$ , the resummed component becomes negligible (see  $\tilde{L}$ ), and the usual fixed order perturbation theory is recovered.
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Introduction and Motivations	Fixed order calculations	Transverse-momentum resummation ○○○○○○●○	Conclusions
Non-perturbative	effects		

- Transverse-momentum distribution is affected by non-perturbative (NP) effects which are important in the large-*b* region.
- For Drell-Yan like processes, we multiply the previously cited  $W_{ab}^F$  function by a NP form factor obtained through experiment.
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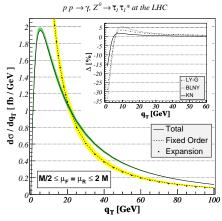
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Fixed order calculations

Transverse-momentum resummation

#### $q_T$ -resummation for slepton-pair production at the LHC



NLL + LO  $\mathcal{O}(\alpha_s)$  results for SPS 7

- Finite result at small q<sub>T</sub>, enhancement at intermediate q<sub>T</sub>.
- Improvement of scale dependence (NLL+LO:  $\lesssim 5\%$ ; LO: 10%).
- Non-perturbative effects cannot be neglected at small q<sub>T</sub>.

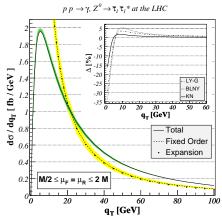
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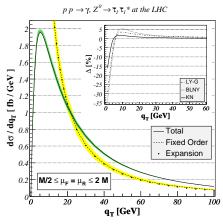
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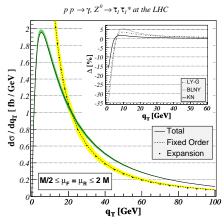
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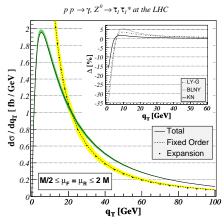
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Introduction	and	Motivations

Fixed order calculations

Transverse-momentum resummation

# Outline

- Introduction and Motivations
  - The Minimal Supersymmetric Model
  - Slepton production at hadron colliders
  - Tau slepton identification
  - Importance of transverse-momentum distribution
- 2 Fixed order calculations
  - Leading order
  - Next-to-leading order
  - Fixed order failure
- 3 Transverse-momentum resummation
  - Main features
  - The resummed component
  - The finite component
  - Non-perturbative effects
  - $q_T$ -resummation for slepton-pair production at the LHC

### Conclusions

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Introduction and Motivations	Fixed order calculations	Transverse-momentum resummation	Conclusions

#### Summary

- Slepton-pair hadroproduction
  - Unpolarized cross sections known at NLO
  - Polarized cross sections known at LO with sfermion mixing.
  - Beam polarization and sfermion mixing correlated.

- q<sub>T</sub>-resummation for sleptons
  - Accurate  $q_T$ -spectrum needed by experiment
    - Mass determination.
    - Spin determination.
  - Universal formalism implemented.
    - Important at small and intermediate  $q_T$ .
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    - Total cross section reproduced.

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