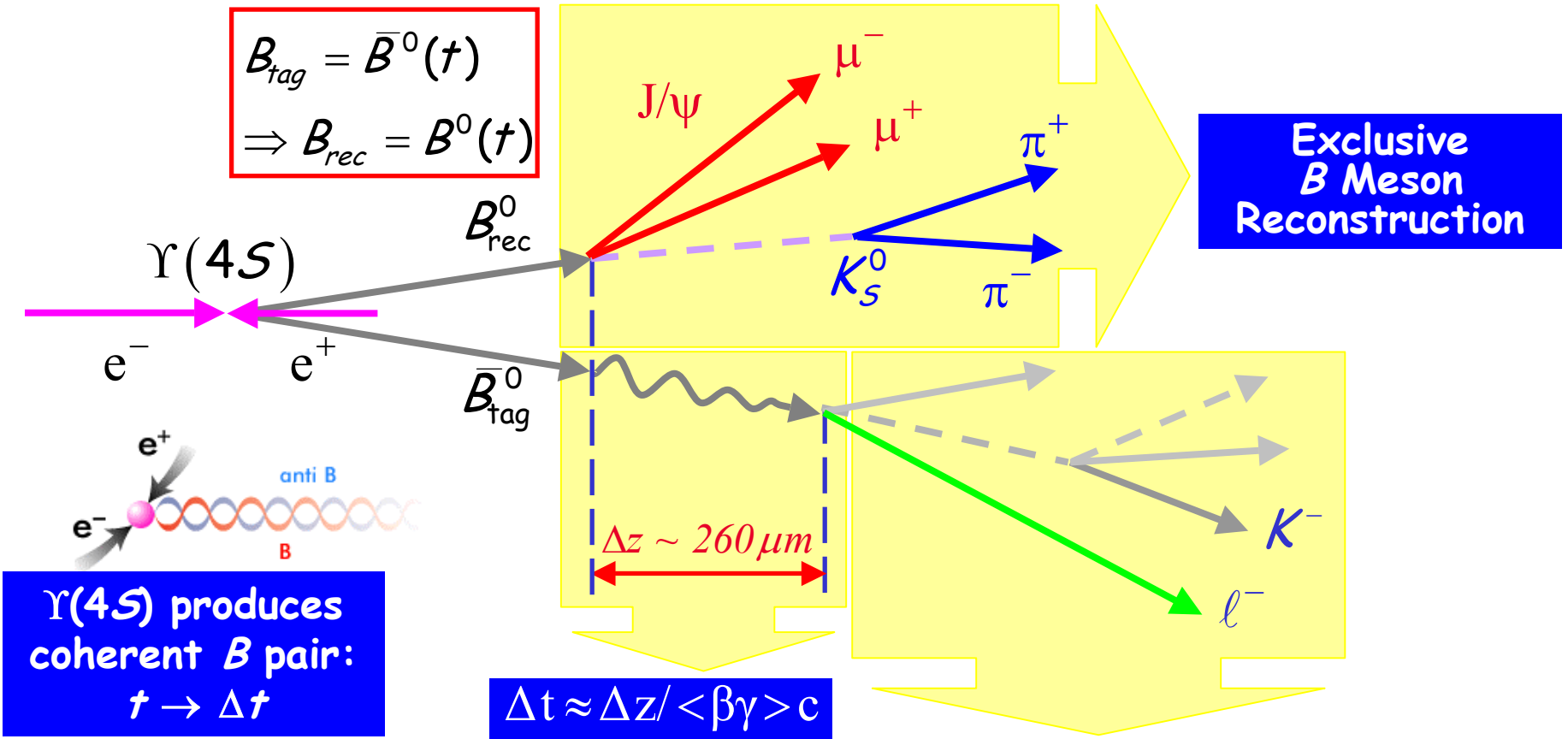


# *Lecture 3: Time-Dependent Asymmetries as a Test of the Standard Model*

- o *CP asymmetries in CP eigenstates involving  $b \rightarrow c\bar{c}s$  transitions*
- o *Measuring  $\sin 2\beta$  in other channels*
- o *Asymmetries in 2-body neutral B decays*
- o *Brief word on future prospects and plans*



# Experimental Technique for B Factories



Time-integrated asymmetries are zero

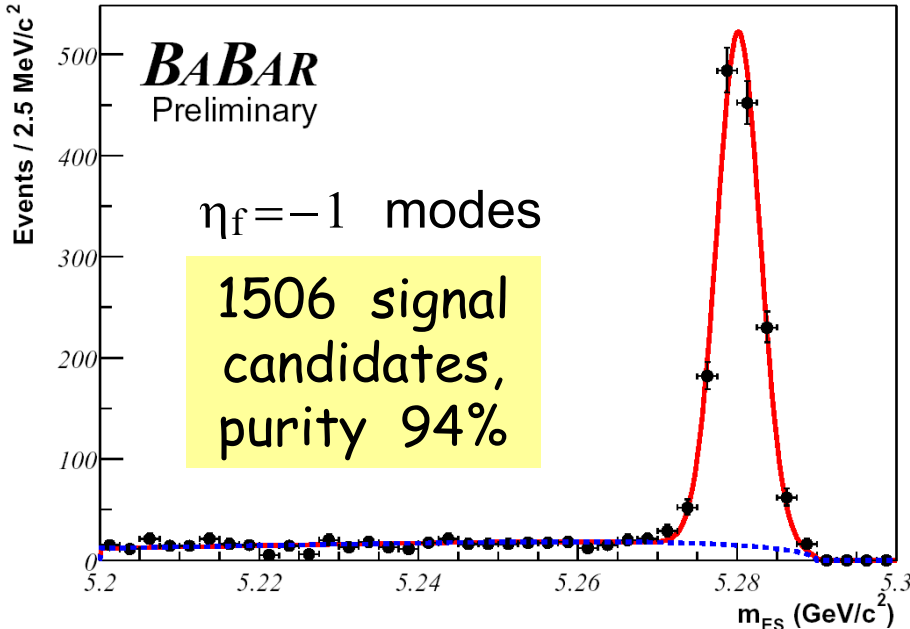
**B-Flavor Tagging**

$B_{rec}^0 = B_{flav}^0$  (flavor eigenstates)  $\Rightarrow$  lifetime, mixing analyses

$B_{rec}^0 = B_{CP}^0$  (CP eigenstates)  $\Rightarrow$  CP analysis



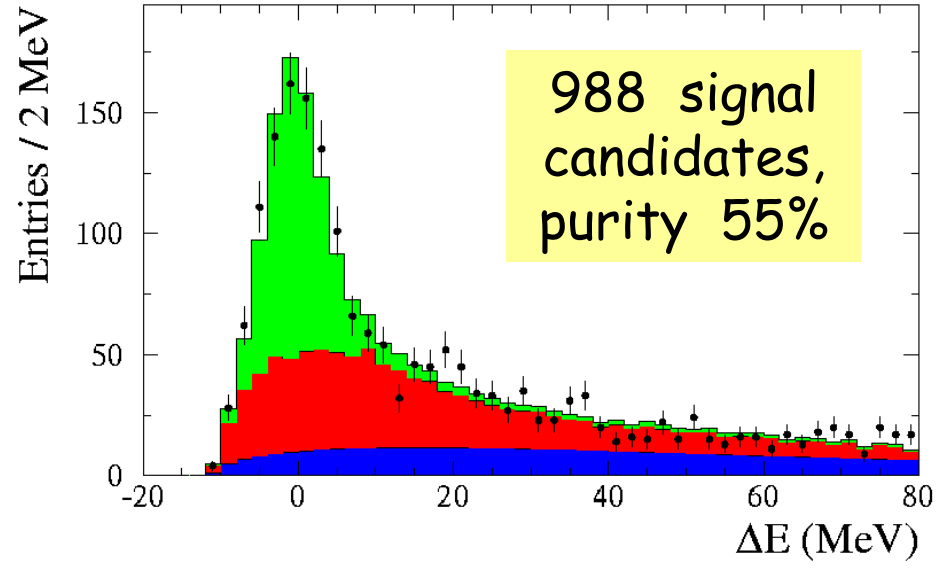
# CP Sample for BABAR



- $\eta_f = -1$  modes
- $B_{CP}^0 \rightarrow J/\psi K_S^0 \{ \rightarrow \pi^+ \pi^- \}$
  - $B_{CP}^0 \rightarrow J/\psi K_S^0 \{ \rightarrow \pi^0 \pi^0 \}$
  - $B_{CP}^0 \rightarrow \psi(2S) \{ \rightarrow \ell^+ \ell^- \text{ or } J/\psi \pi^+ \pi^- \} K_S^0$
  - $B_{CP}^0 \rightarrow \chi_{c1} \{ \rightarrow J/\psi \gamma \} K_S^0$
  - $B_{CP}^0 \rightarrow \eta_c \{ \rightarrow KK \pi \} K_S^0$

- $\eta_f = +1$  mode
- $B_{CP}^0 \rightarrow J/\psi K_L^0$

**BABAR**  
81.3 fb<sup>-1</sup>



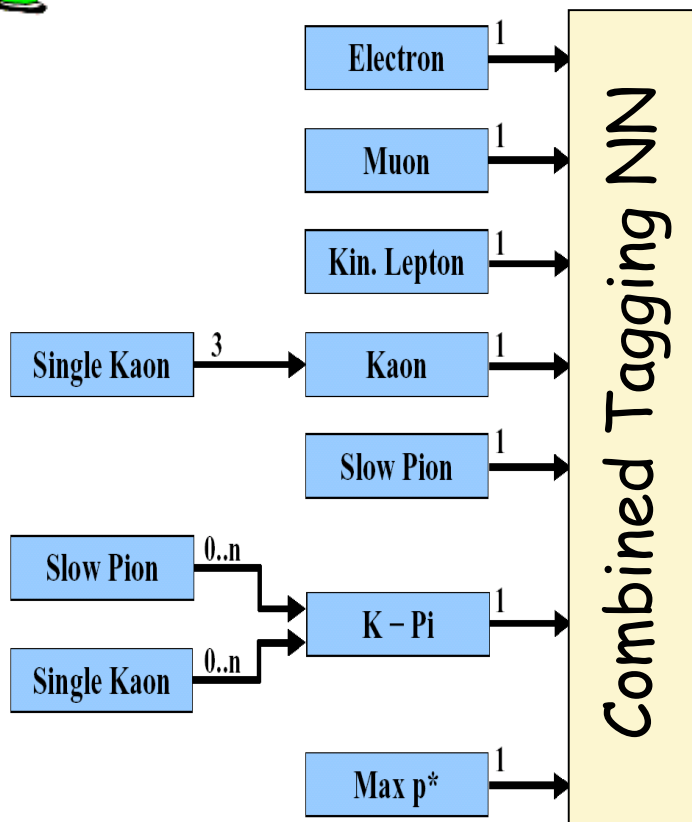
(after tagging & vertexing)



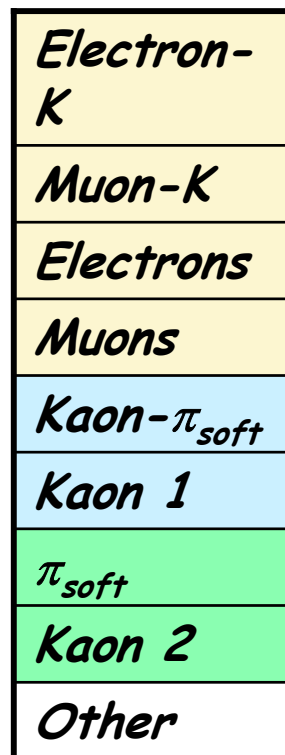
# Improved Tagging at BABAR



Sub-taggers



9 Tagging Categories



4 Physics Categories



7% improvement in  $Q = \epsilon D^2$  ( $\Delta Q = 1.9\%$ )



# Flavor Tagging Performance in Data

The large sample of fully reconstructed events provides the precise determination of the tagging parameters required in the  $CP$  fit

Tagging category	Fraction of tagged events $\varepsilon$ (%)	Wrong tag fraction $w$ (%)	Mistag fraction difference $\Delta w$ (%)	$Q = \varepsilon(1-2w)^2$ (%)
Lepton	$9.1 \pm 0.2$	$3.3 \pm 0.6$	$-0.9 \pm 0.5$	$7.9 \pm 0.3$
Kaon I	$16.7 \pm 0.2$	$9.9 \pm 0.7$	$-0.2 \pm 0.5$	$10.7 \pm 0.4$
Kaon II	$19.8 \pm 0.3$	$20.9 \pm 0.8$	$-2.7 \pm 0.6$	$6.7 \pm 0.4$
Inclusive	$20.0 \pm 0.3$	$31.6 \pm 0.9$	$-3.2 \pm 0.6$	$0.9 \pm 0.2$
ALL	$65.6 \pm 0.5$			$28.1 \pm 0.7$

Highest "efficiency"

Error on  $\sin 2\beta$  and  $\Delta m_d$  depend on the "quality factor"  $Q$  approx. as:

$$\sigma(\sin 2\beta) \sim \frac{1}{\sqrt{Q}}$$

Smallest mistag fraction



**BABAR**  
81.3 fb<sup>-1</sup>

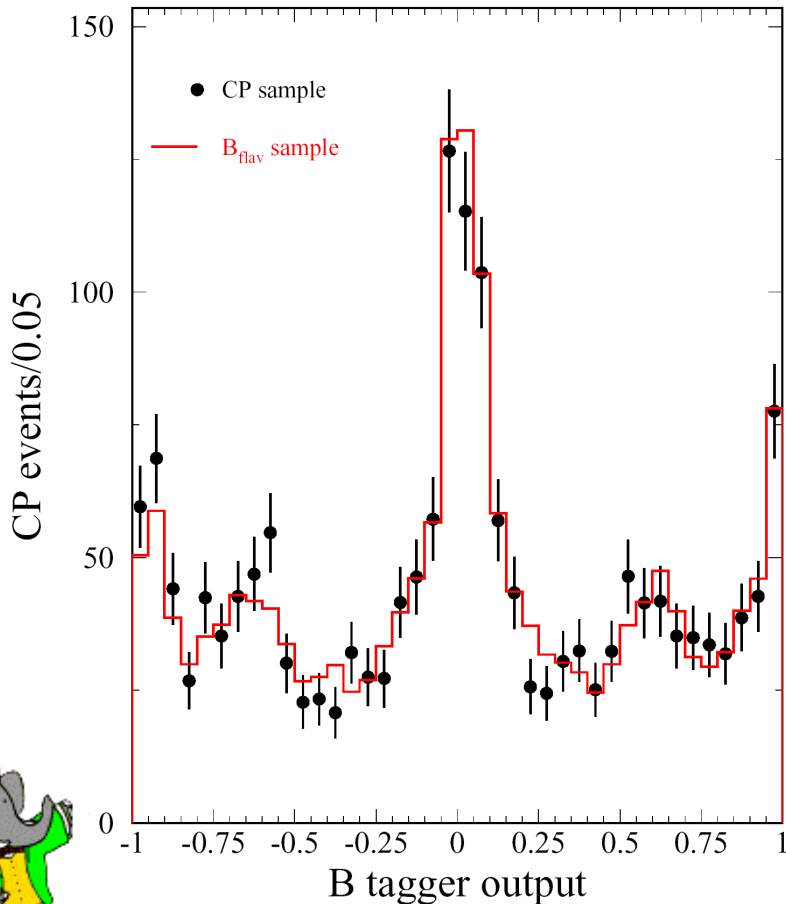


# Comparison Tests with New Tagger

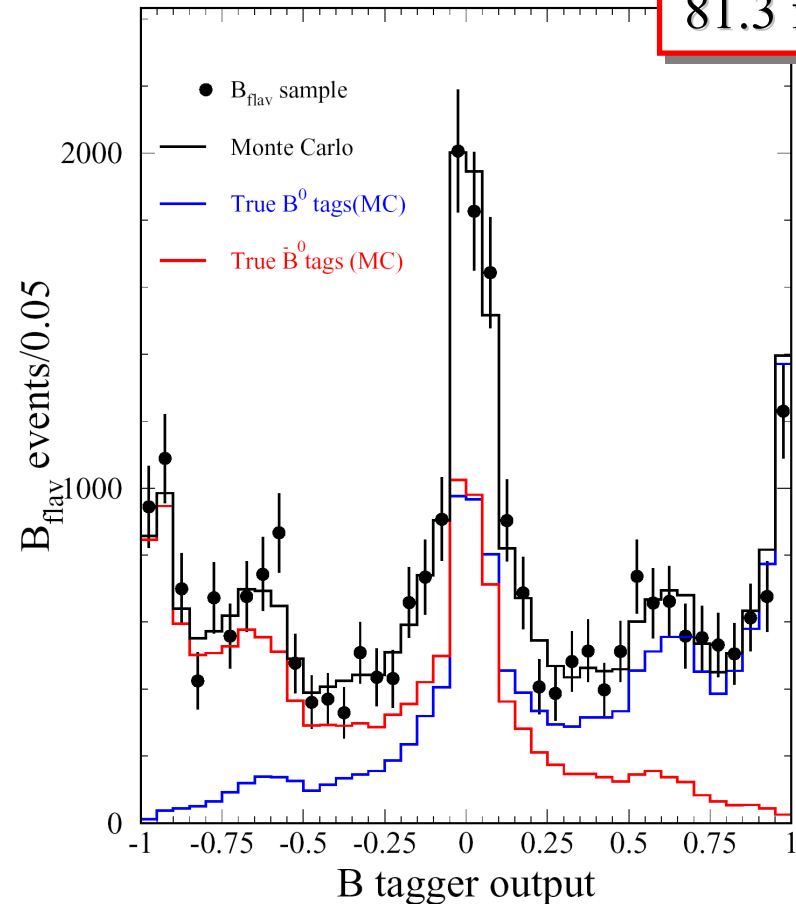
Test of crucial underlying assumption:  
tagging the same for  $CP$  &  $B_{flav}$  samples

**BABAR**

81.3 fb<sup>-1</sup>



**CP vs  $B_{flav}$  sample**

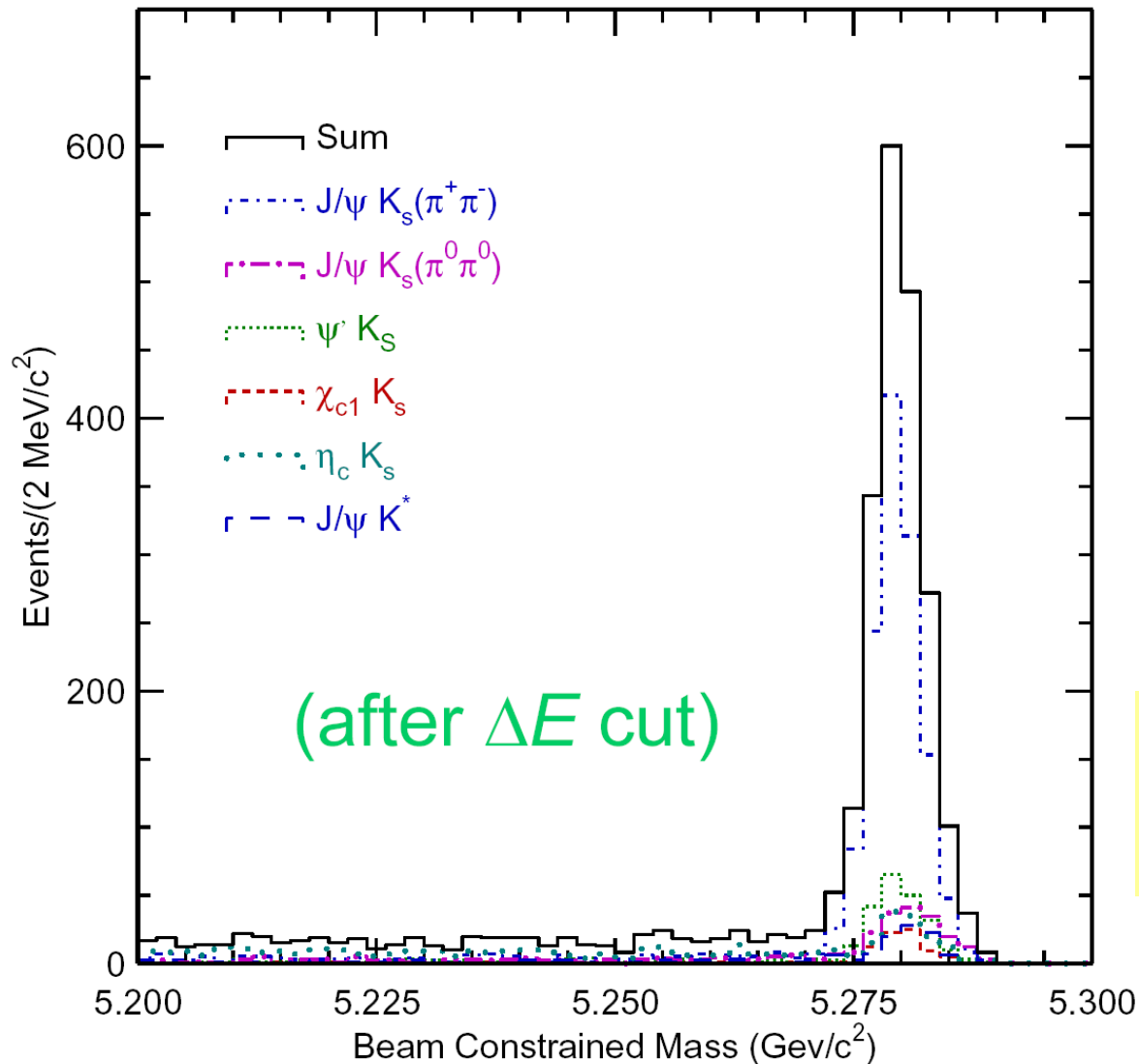


**$B_{flav}$  sample vs MC**



# Golden Sample: $(cc)K_S$ CP Eigenstates

**BELLE**  
78 fb<sup>-1</sup>



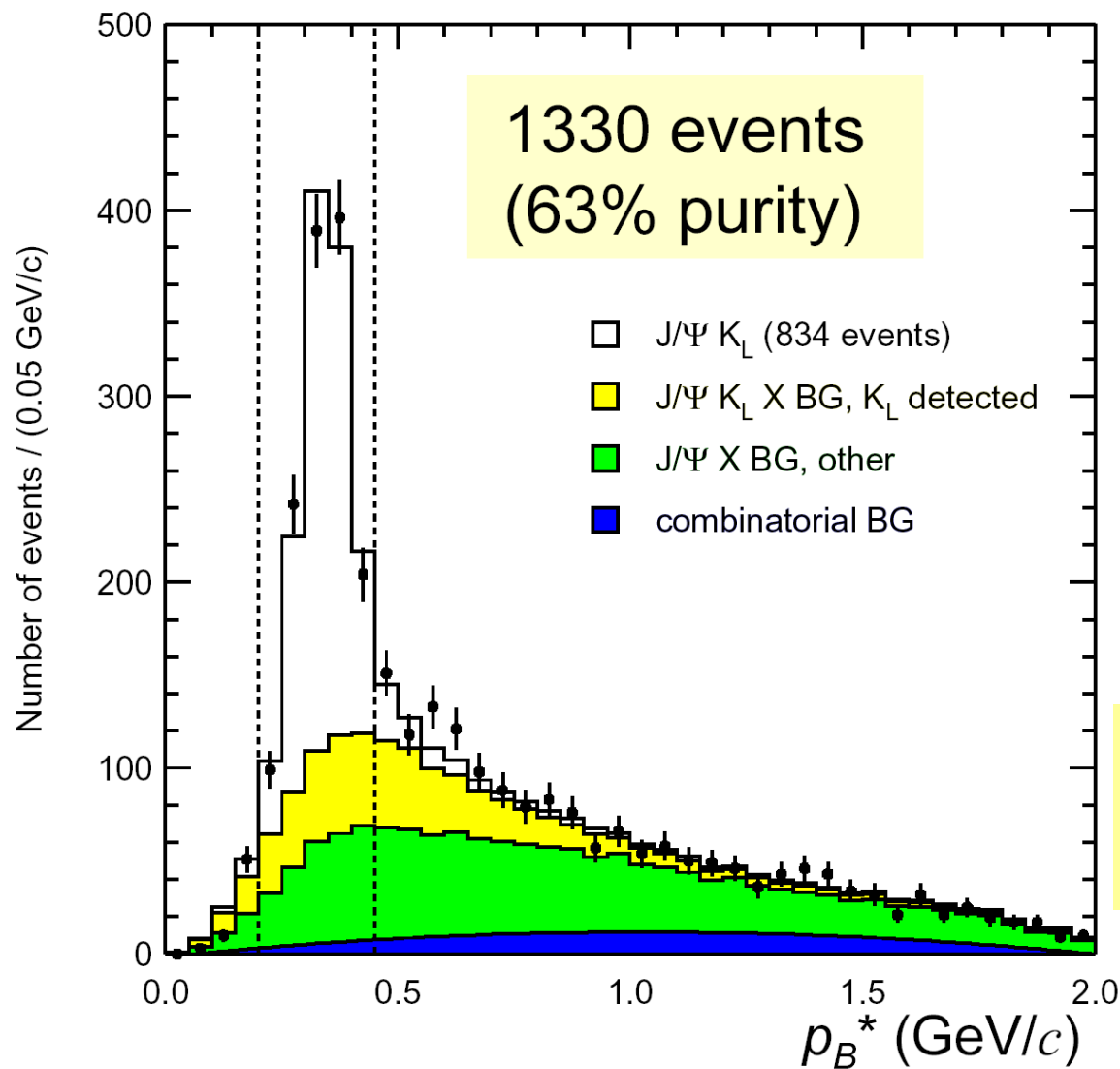
1996 signal  
candidates,  
purity 94%



# CP Eigenstate Sample: $J/\psi K_L$

**BELLE**

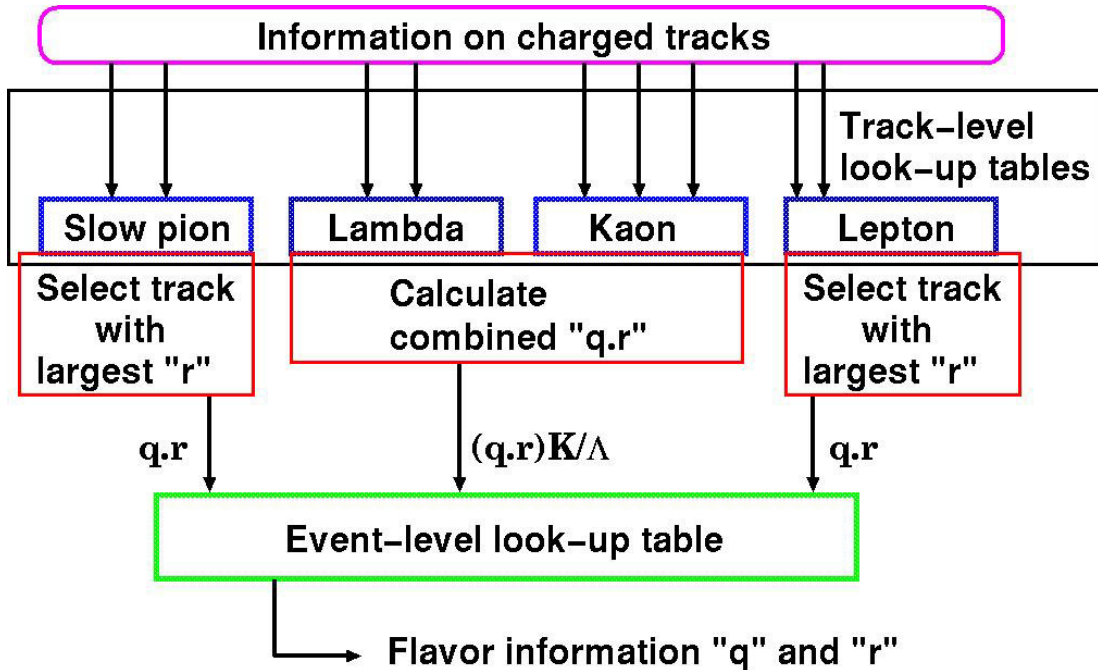
78 fb<sup>-1</sup>





# Tagging at Belle

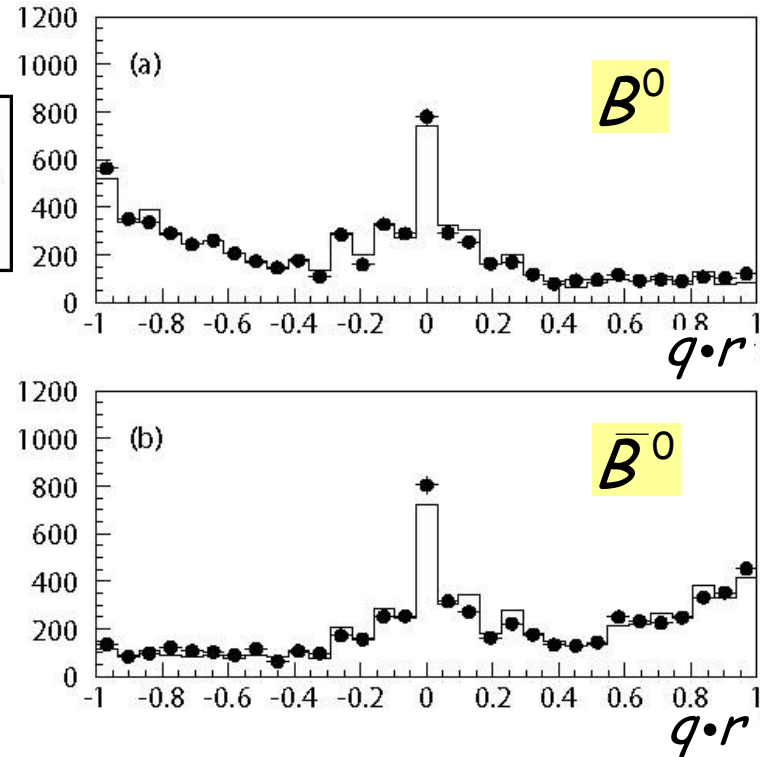
## Track level and event level look-up tables



$q = +1$ :  $B^0$ -like  
 $q = -1$ :  $\bar{B}^0$ -like

Quality factor  $r$  varies from  
 0 = low likelihood  
 1 = high likelihood

## Tagged $B^0 \rightarrow D^{*-} \ell^+ \nu$ sample



## Data vs MC comparison

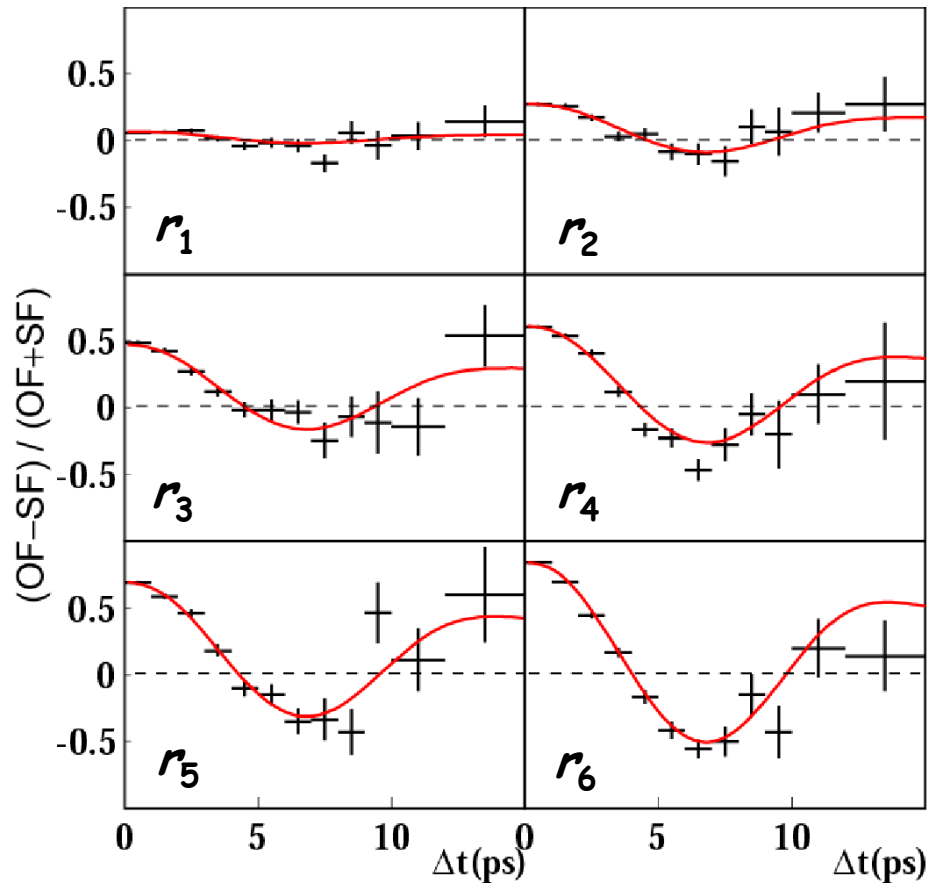
**BELLE**  
 41.8 fb<sup>-1</sup>



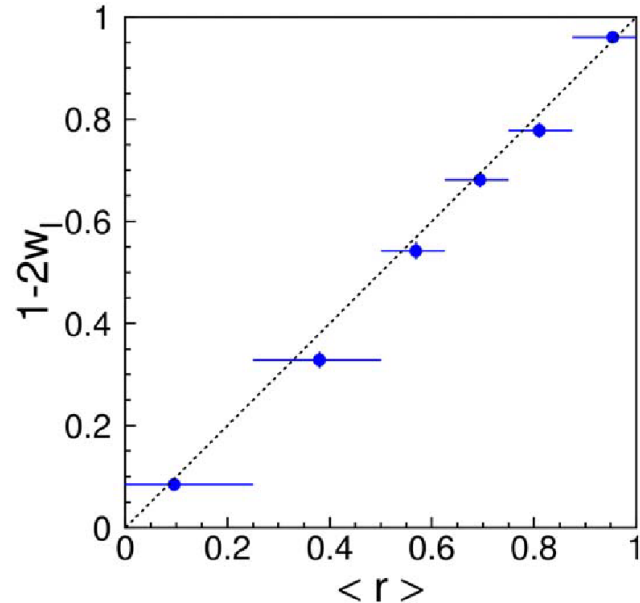
# Measuring Mistag Rate

Mistag rate extracted in six bins  
in  $r$  from mixing fit

Tagged  $B^0 \rightarrow D^{*-} \ell^+ \nu$  sample



Comparison between measured  
( $1-2w$ ) and quality factor  $r$   
obtained in 6 bins in  $r$

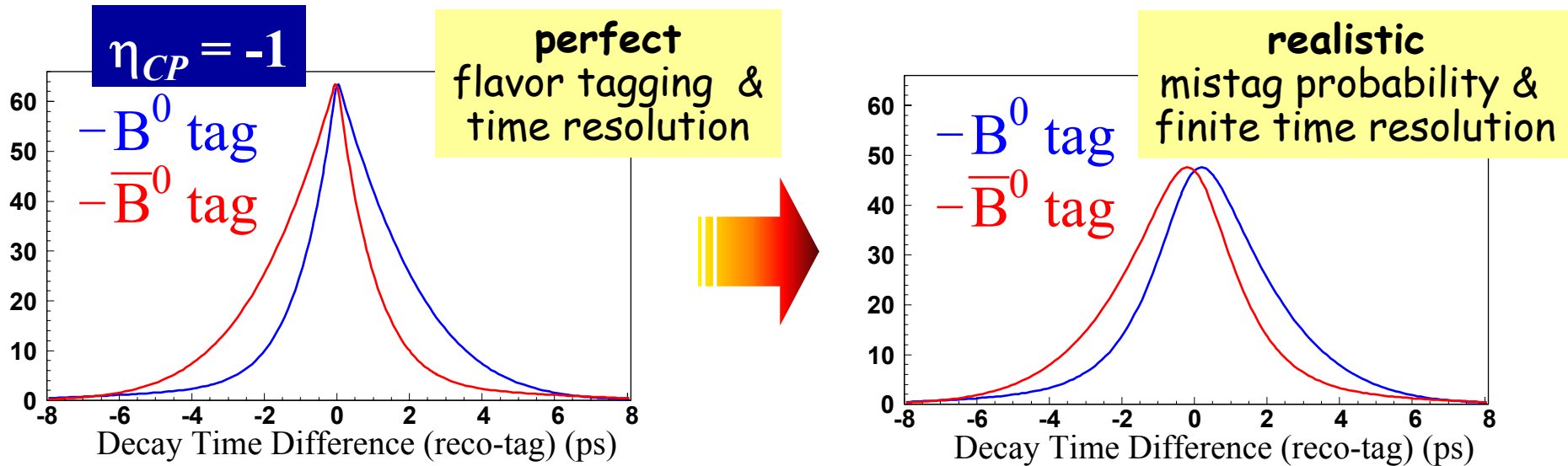


$\epsilon > 99.5\%$ ,  $Q = 28.8 \pm 0.5\%$

**BELLE**  
78 fb<sup>-1</sup>



# CP Analysis: Time Distributions



$$f_{CP,\pm}(\Delta t) \neq \left\{ \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} (1 \mp \eta_f (1 - 2\omega) \sin 2\beta \sin \Delta m_d \Delta t) \right\} \otimes R(\Delta t)$$

$$"f_{CP,+}" \Leftrightarrow B_{tag}^0 = B^0$$

$$"f_{CP,-}" \Leftrightarrow B_{tag}^0 = \bar{B}^0$$

same mistag probability  $\omega$   
 and time-resolution function  $R(\Delta t)$



# Time-Dependent CP Asymmetries

Time-dependence of  
 $B^0 - \bar{B}^0$  mixing

$$A_{\text{mixing}}(\Delta t) = \frac{N(\text{unmixed}) - N(\text{mixed})}{N(\text{unmixed}) + N(\text{mixed})} \approx \text{[redacted]} \cos \Delta m_d \Delta t$$

Time-dependence of  
CP-violating asymmetry in  
 $B_{CP}^0 \rightarrow J / \psi K_S^0$

$$A_{CP}(\Delta t) = \frac{N(B_{\text{tag}} = B^0) - N(B_{\text{tag}} = \bar{B}^0)}{N(B_{\text{tag}} = B^0) + N(B_{\text{tag}} = \bar{B}^0)} \approx \text{[redacted]} \sin 2\beta \sin \Delta m_d \Delta t$$

(Assuming no confusion  
of  $B_{\text{rec}}$  state)



Use the large statistics  $B_{\text{flav}}$  data sample  
to determine the mistag probabilities and the  
parameters of the time-resolution function



# *sin2β Likelihood Fit*

Combined unbinned maximum likelihood fit to  $\Delta t$  spectra of  $B_{\text{flav}}$  and  $CP$  samples

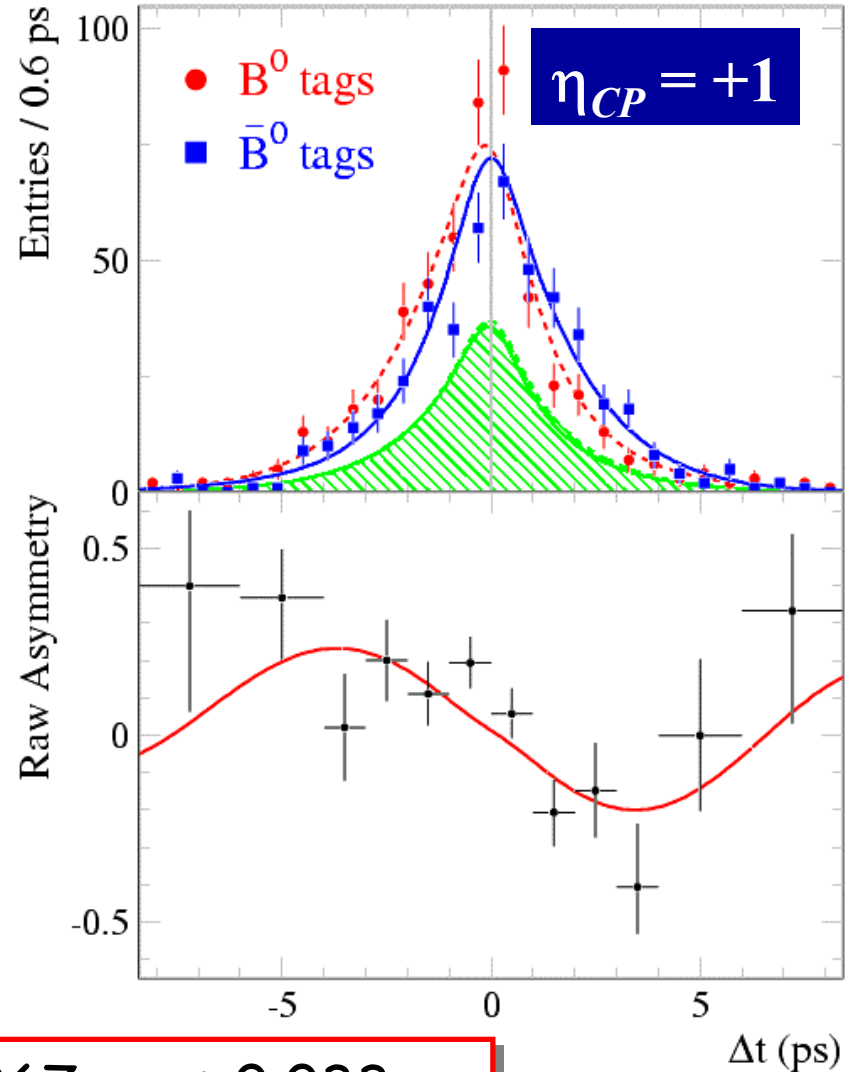
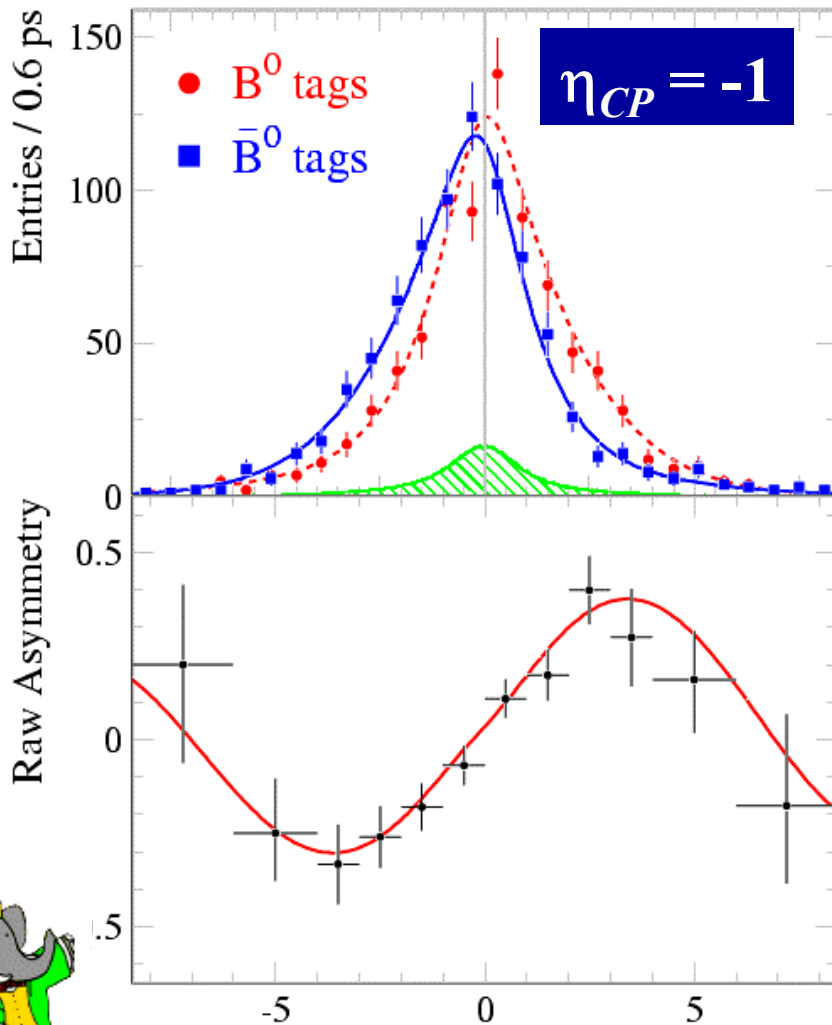
<i>Fit Parameters</i>	<i>#</i>	<i>Main Sample</i>
<i>sin2β</i>	<i>1</i>	<i>Tagged CP sample</i>
<i>Mistag fractions for <math>B^0</math> and <math>\bar{B}^0</math> tags</i>	<i>8</i>	<i>Tagged flavor sample</i>
<i>Signal resolution function</i>	<i>8</i>	<i>Tagged flavor sample</i>
<i>Empirical description of background <math>\Delta t</math></i>	<i>17</i>	<i>Sidebands</i>
<i>B lifetime from PDG 2002</i>	<i>0</i>	$\tau_B = 1.542 \text{ ps}$
<i>Mixing frequency from PDG 2002</i>	<i>0</i>	$\Delta m_d = 0.489 \text{ ps}^{-1}$
<i>Total parameters</i>	<i>34</i>	

Global correlation coefficient for  $\sin 2\beta$ : 13%

- ✓ All  $\Delta t$  parameters extracted from data
- ✓ Correct estimate of the error and correlations



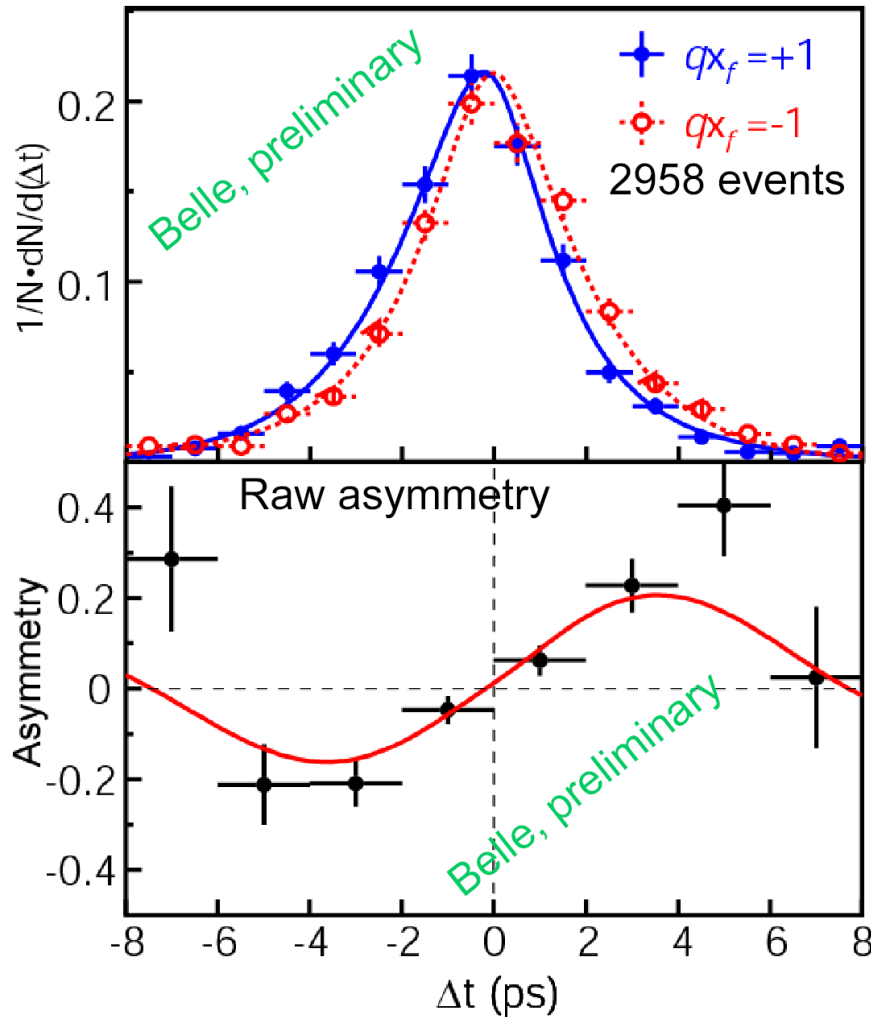
# BABAR Result for $\sin 2\beta$



$$\sin 2\beta = 0.741 \pm 0.067_{(stat)} \pm 0.033_{(syst)}$$



# Belle Result for $\sin 2\beta$



**BELLE**  
78 fb<sup>-1</sup>

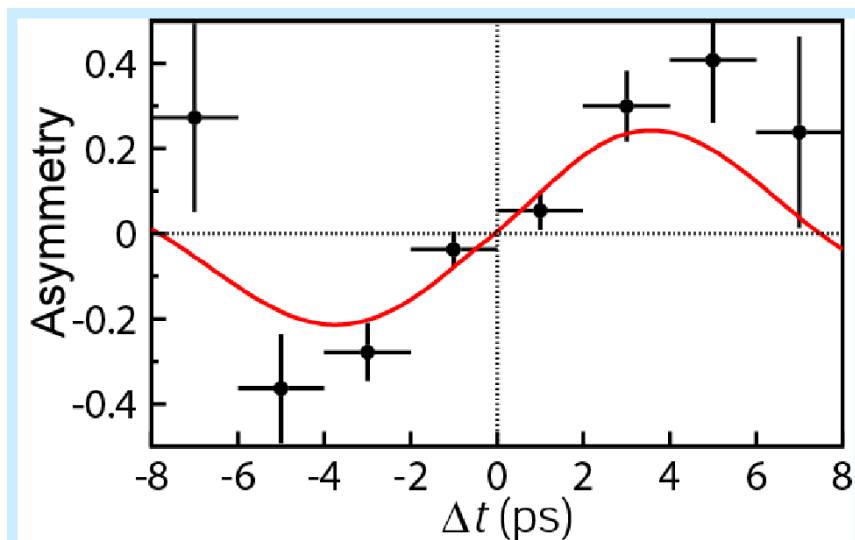
Checks with control samples  
where no asymmetry expected

Sample	" $\sin 2\beta$ "
$B^0 \rightarrow D^{*+} \pi^-$	$0.035 \pm 0.032$
$B^0 \rightarrow J/\psi K^*$	$-0.021 \pm 0.093$
$B^0 \rightarrow D^{*0} \nu$	$0.004 \pm 0.017$

$$\sin 2\beta = 0.719 \pm 0.074_{(stat)} \pm 0.035_{(syst)}$$

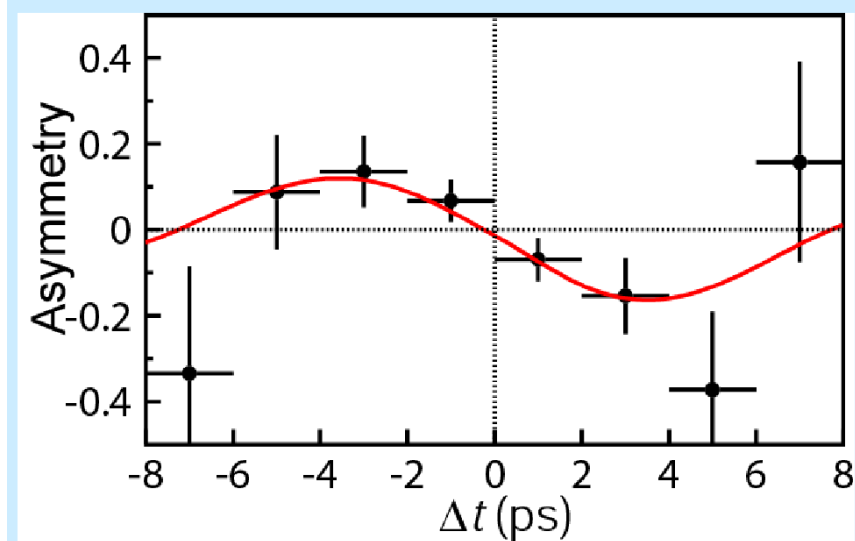


# Belle Result for $\sin 2\beta$



$$\eta_{CP} = -1$$

$$\sin 2\beta = 0.716 \pm 0.083_{(stat)}$$



$$\eta_{CP} = +1$$

$$\sin 2\beta = 0.78 \pm 0.17_{(stat)}$$

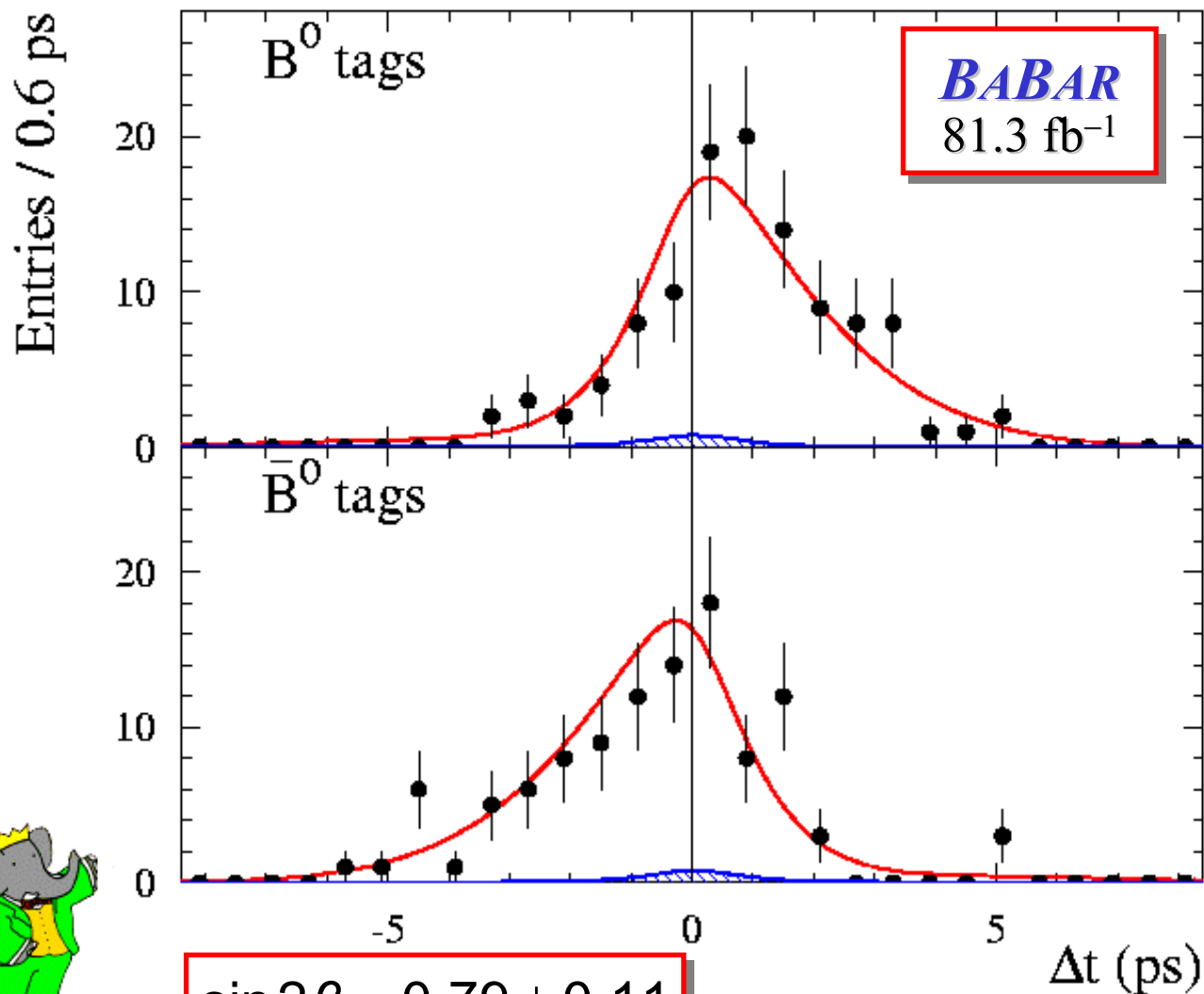
**BELLE**

78 fb<sup>-1</sup>





# Pure Gold: Lepton Tags Alone

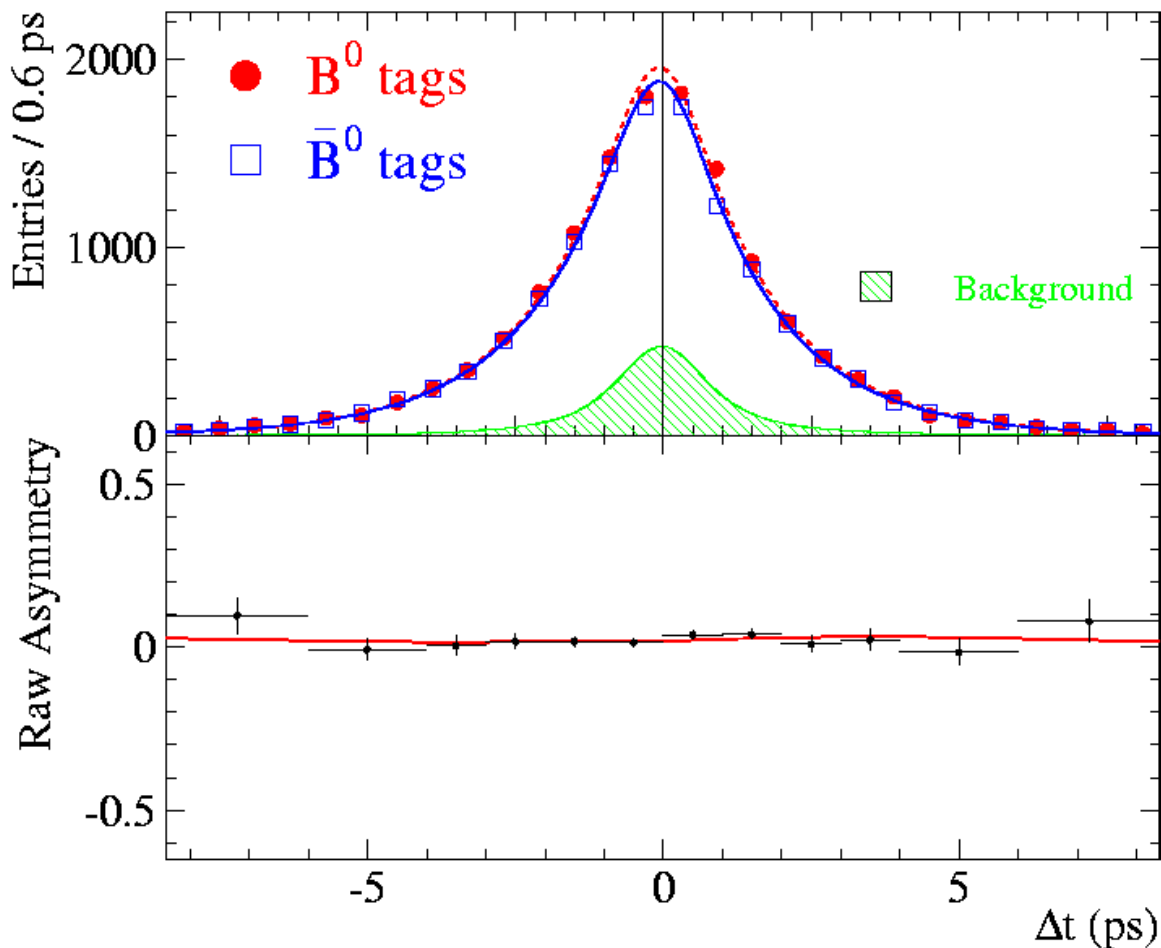


220 lepton-tagged  
 $\eta_f = -1$  events

98% purity  
3.3% mistag rate  
20% better  $\Delta t$   
resolution



# Check "null" Control Sample at BABAR



Input  $B_{flav}$  sample to  $CP$  fit

No asymmetry expected

Sample	" $\sin 2\beta$ "
$B_{flav}$	$0.021 \pm 0.022$
$B^+$	$0.017 \pm 0.025$



# Systematic Errors on $\sin 2\beta$ from BABAR

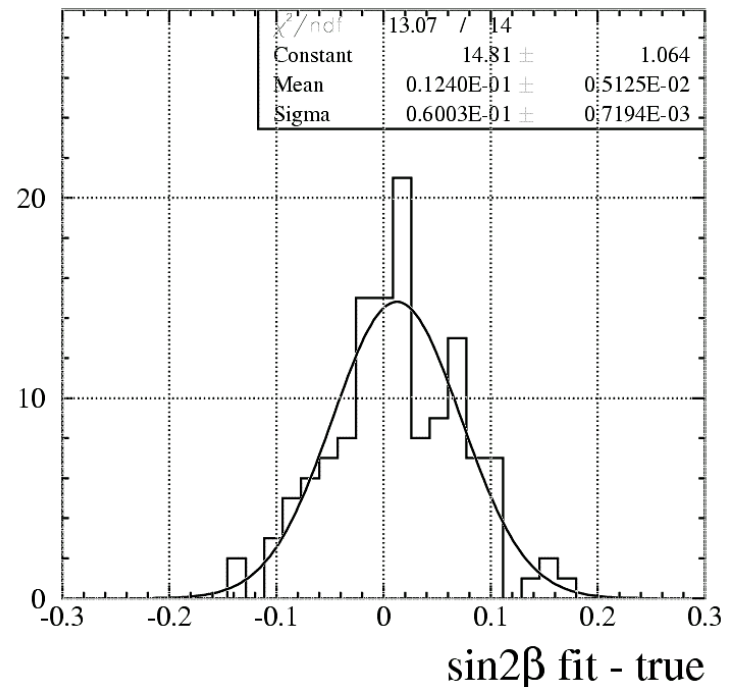
	$\sigma[\sin 2\beta]$
<b>Description of background events</b>	<b>0.017</b>
<i>CP content of background components</i>	
<i>Background shape uncertainties, peaking component</i>	
<b>Composition and CP content of <math>J/\psi K_L</math> background</b>	<b>0.015</b>
<b><math>\Delta t</math> resolution and detector effects</b>	<b>0.017</b>
<i>Silicon detector residual misalignment</i>	
<i><math>\Delta t</math> resolution model (<math>G_{\text{exp}}</math> vs <math>3G</math>, <math>B_{\text{flav}}</math> vs <math>B_{\text{CP}}</math>)</i>	
<b>Mistag differences between <math>B_{\text{CP}}</math> and <math>B_{\text{flav}}</math> samples (MC)</b>	<b>0.012</b>
<b>Fit bias correction and MC statistics</b>	<b>0.010</b>
<b>Fixed lifetime and oscillation frequency</b>	<b>0.005</b>
<b>Total</b>	<b>0.033</b>



# Monte Carlo Correction

## ➤ Potential bias on $\sin 2\beta$ evaluated by fitting full MC in 2 ways:

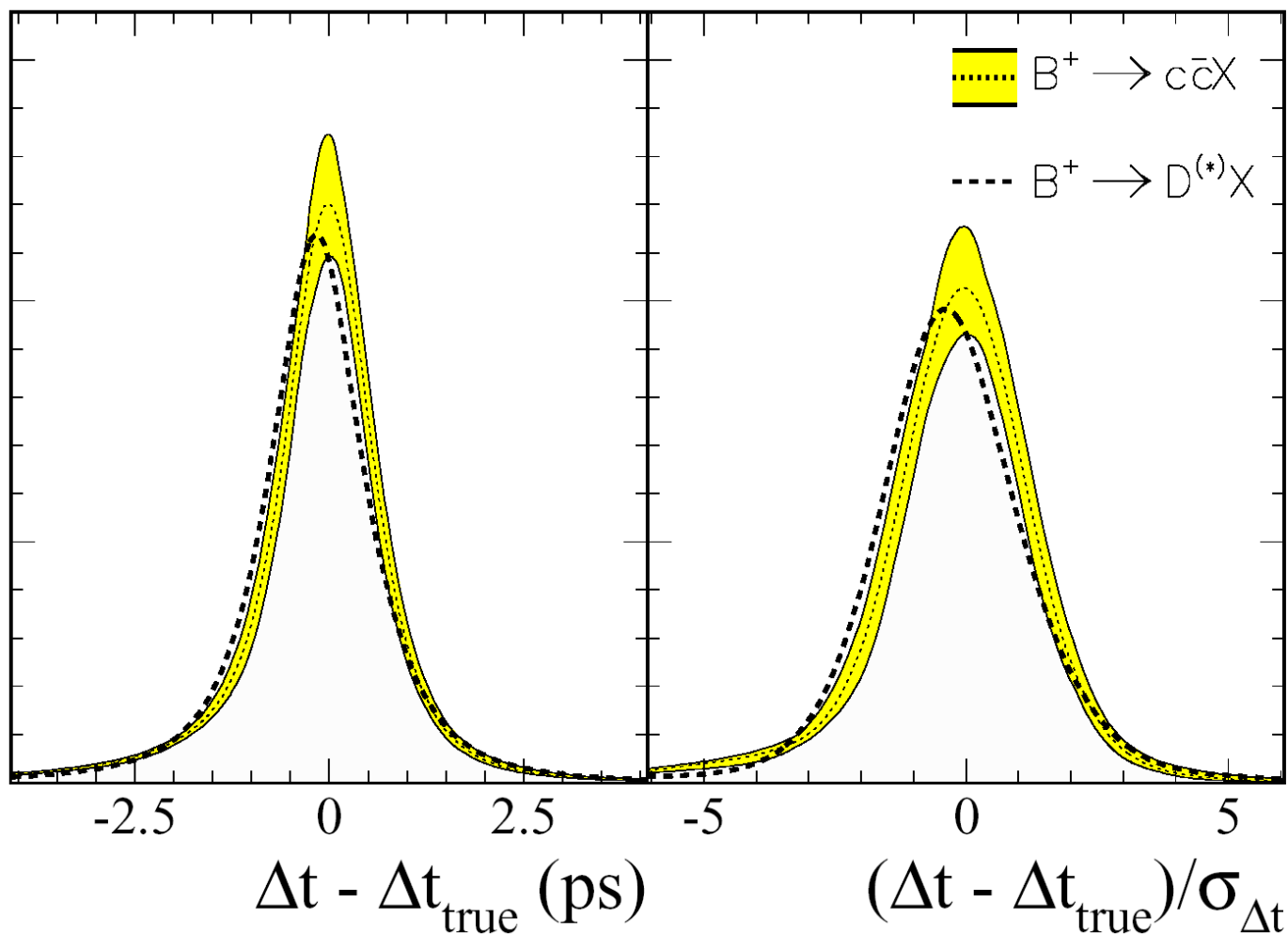
- Fitting data-sized signal MC samples with mistag fractions and  $\Delta t$  resolution fixed to the MC truth values (see plot)
  - Average bias =  $+0.012 \pm 0.005$
- Same as above except mistag fractions and  $\Delta t$  resolution from  $B_{\text{reco}}$  MC
  - Average bias =  $+0.014 \pm 0.005$



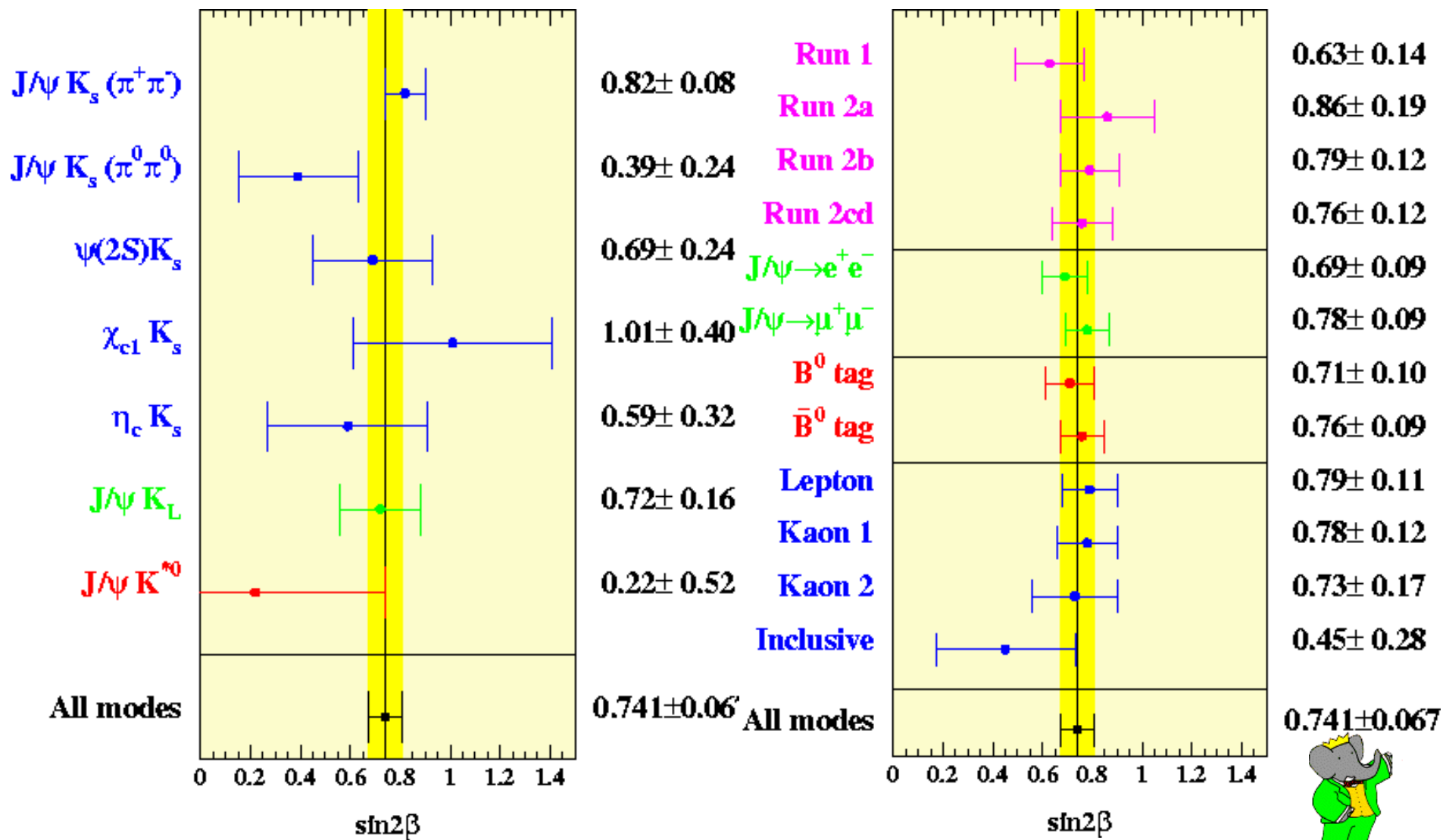
- ## ➤ One possible source of bias comes from neglecting the known correlation between the mistag fractions and $\sigma(\Delta t)$
- Estimates from toy and full MC indicate a bias at the level of  $+0.004$
- ## ➤ We correct the fitted $\sin 2\beta$ by subtracting 0.014 and assign a systematic error of 0.010 to this correction



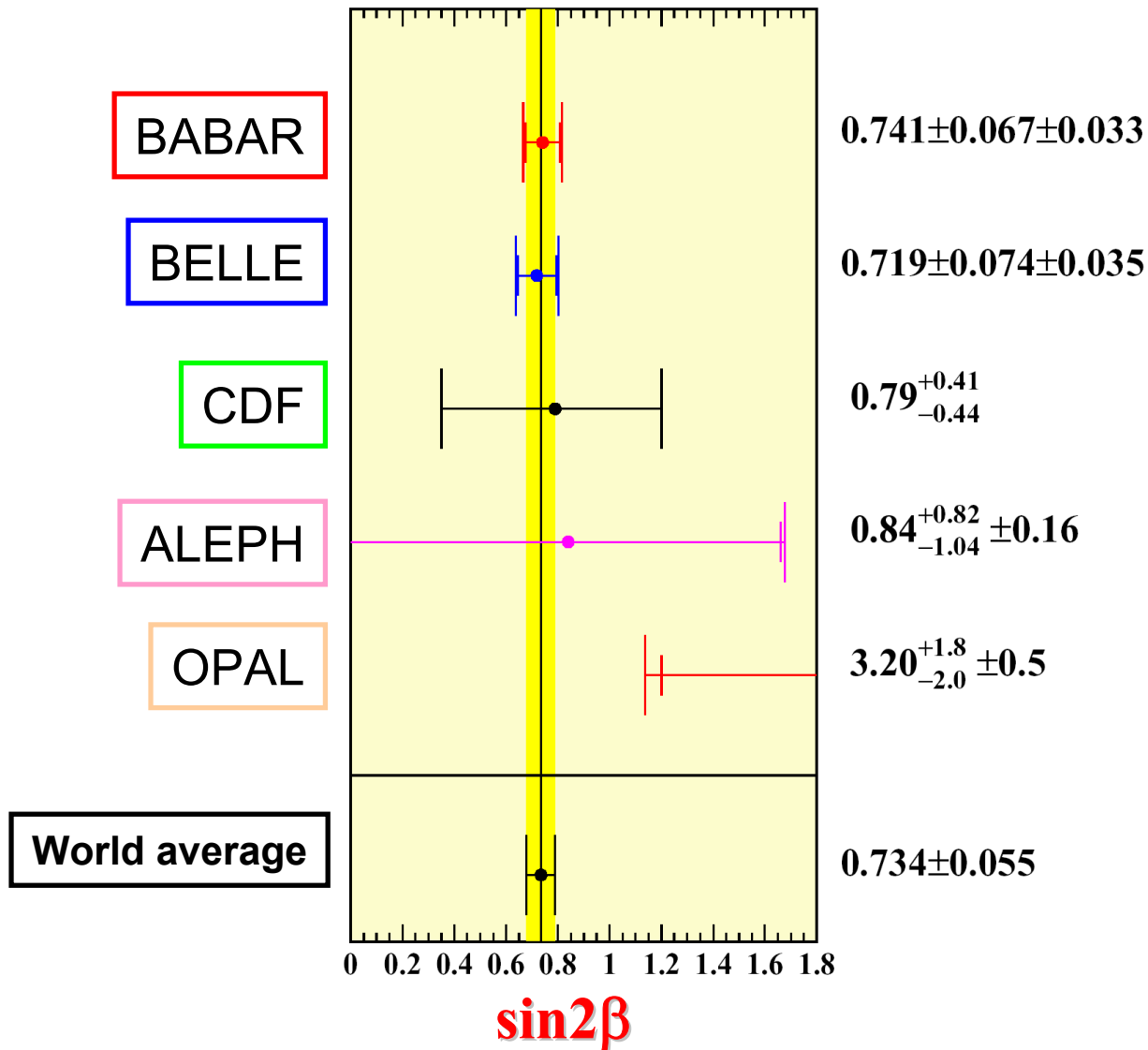
# Comparison of Resolution Functions



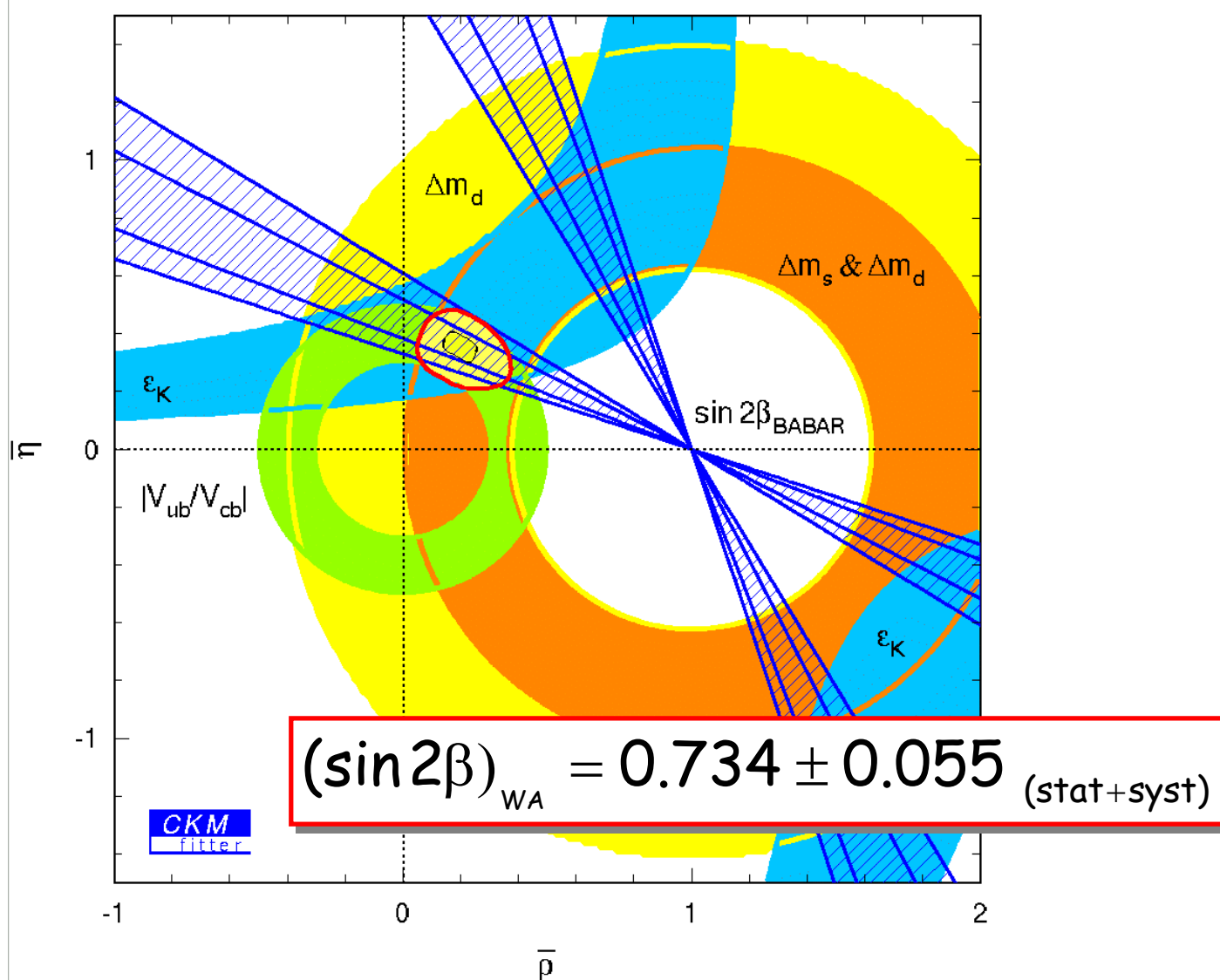
# Subsample Checks



# World Average



# Standard Model Constraints





# Summary of $\sin^2\beta$ from $c\bar{c}s$ modes

- Precision measurements of  $\sin^2\beta$  from charmonium modes now available

$$\sin^2\beta = 0.741 \pm 0.067 \text{ (stat)} \pm 0.033 \text{ (syst)}$$

BABAR-PUB-02/008, hep-ex/0207042,  
submitted to PRL

$$\sin^2\beta = 0.719 \pm 0.074 \text{ (stat)} \pm 0.035 \text{ (syst)}$$

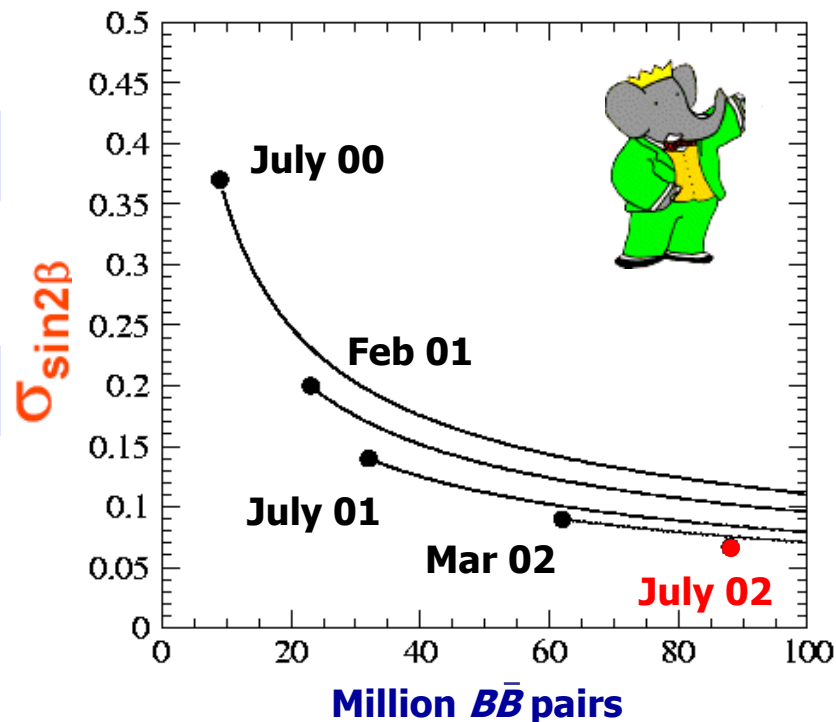
BELLE-CONF-0201, hep-ex/0207098,  
submitted to ICHEP2002

- World average

$$\sin^2\beta = 0.734 \pm 0.055 \text{ (stat+syst)}$$

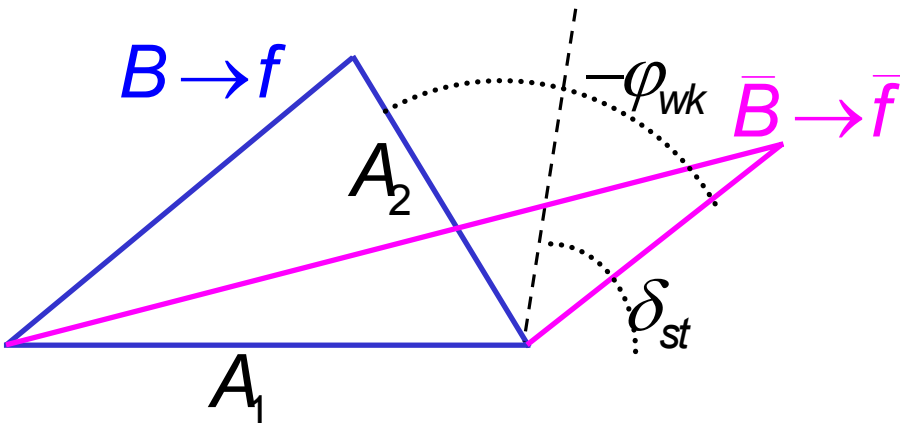
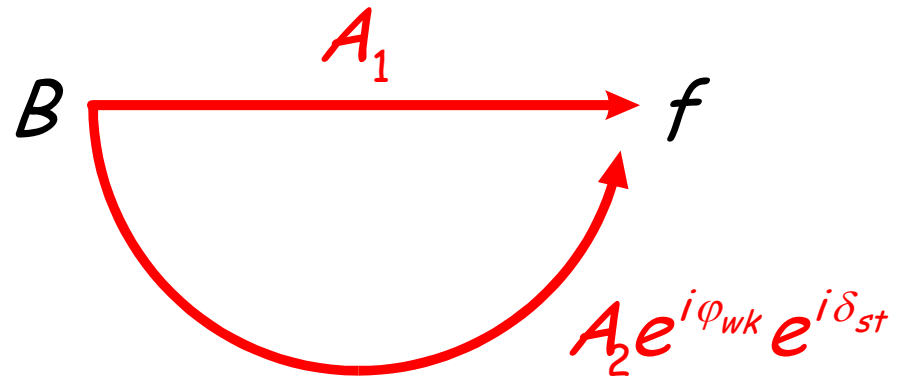
The Standard Model remains unscathed, but the high statistics future of  $B$  Factories will provide further opportunities to challenge the theory

Results have been improving by more than just luminosity gain



# CP Violation in the B System

➤ CPV through interference of decay amplitudes



$$\Gamma(B \rightarrow f) = \left| A_1 + A_2 e^{i\varphi_{wk}} e^{i\delta_{st}} \right|^2$$

$$\Gamma(\bar{B} \rightarrow \bar{f}) = \left| A_1 + A_2 e^{-i\varphi_{wk}} e^{i\delta_{st}} \right|^2$$

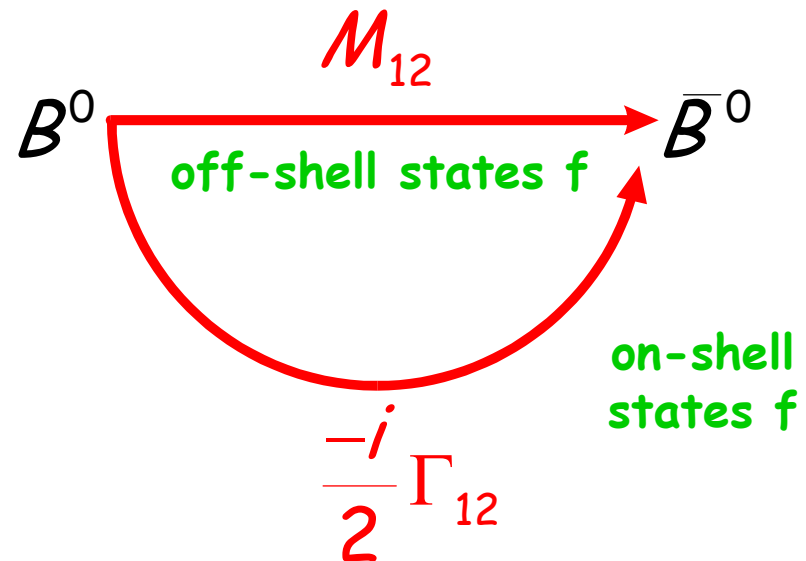
$$\Gamma(B \rightarrow f) \neq \Gamma(\bar{B} \rightarrow \bar{f})$$

for  $\varphi_{wk} \neq 0$  and  $\delta_{st} \neq 0$



# CP Violation in the B System

- CPV through interference of decay amplitudes
- CPV through interference of mixing diagram



Expected to be very small



# Formalism for CP Violation in Mixing

CP (or T) violation in the  $B^0\bar{B}^0$  mixing matrix results from:

Mass eigenstates  $|B_{L,H}\rangle \neq CP$  eigenstates  $|B_{\pm}\rangle$

$$|B_{L,H}\rangle = p|B^0\rangle \pm q|\bar{B}^0\rangle = \frac{1}{\sqrt{1+|\varepsilon_{B_d}|^2}}(|B_{\pm}\rangle + \varepsilon_{B_d}|B_{\mp}\rangle)$$

$$\left| \frac{q}{p} \right| = \left| \frac{1 - \varepsilon_{B_d}}{1 + \varepsilon_{B_d}} \right| \neq 1 \Rightarrow \text{Prob}(B^0 \rightarrow \bar{B}^0) \neq \text{Prob}(\bar{B}^0 \rightarrow B^0)$$

Time-dependent CP Asymmetry:

$$A_T(t) = \frac{\Gamma(\bar{B}_{phys}^0(t) \rightarrow l^+ \nu X) - \Gamma(B_{phys}^0(t) \rightarrow l^- \bar{\nu} X)}{\Gamma(\bar{B}_{phys}^0(t) \rightarrow l^+ \nu X) + \Gamma(B_{phys}^0(t) \rightarrow l^- \bar{\nu} X)} \approx \frac{4\text{Re}(\varepsilon_{B_d})}{1 + |\varepsilon_{B_d}|^2} \quad \begin{array}{l} \text{constant} \\ \text{with} \\ \text{time} \end{array}$$

In the B System,  $\Delta m_d = m_{B_H} - m_{B_L} \gg \Delta\Gamma_d \Rightarrow \varepsilon_d \sim$  purely imaginary

SM:  $A_T \leq 2 \times 10^{-3}$ ; hence  $A_T \approx 10^{-2} \Rightarrow$  New Physics

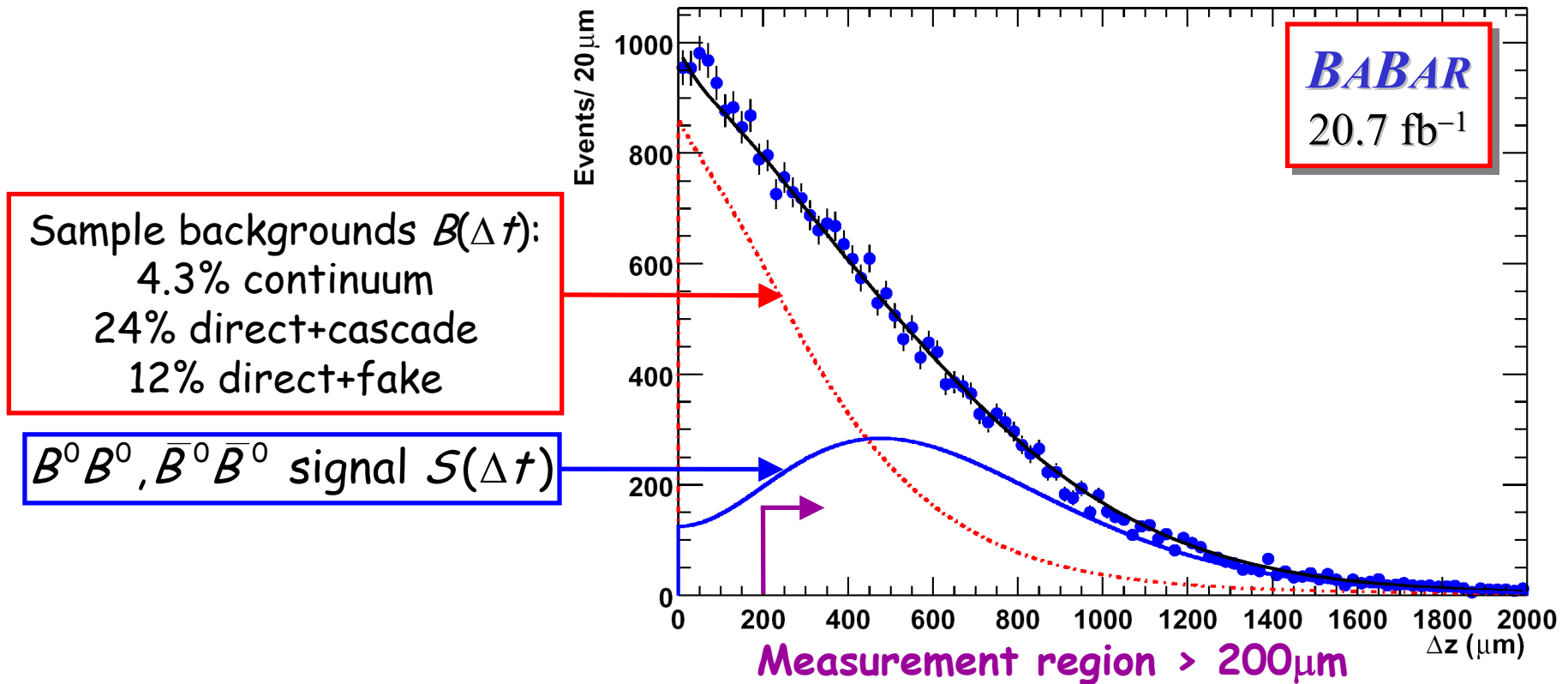
See for instance Bañuls & Bernabéu hep-ph/0005323



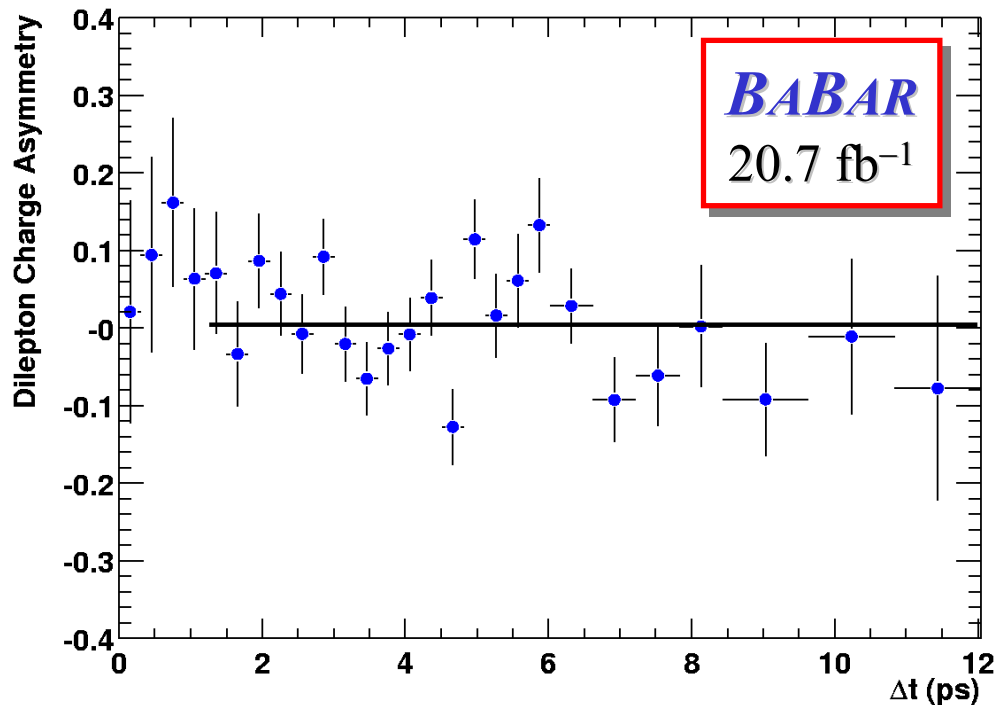
# Characterizing the Dilepton Sample

Search for asymmetry in same-sign dilepton sample containing 20381 events

$$A_T^{obs}(\Delta t) = \frac{N(l^+l^+, \Delta t) - N(l^-l^-, \Delta t)}{N(l^+l^+, \Delta t) + N(l^-l^-, \Delta t)} = A_T \times \frac{S(\Delta t)}{S(\Delta t) + B(\Delta t)}$$



# Determination of $A_T$



Find:  $+0.005 \pm 0.012_{(stat)} \pm 0.014_{(syst)}$

Conclude:  $\text{Re}(\varepsilon_{B_d}) / (1 + |\varepsilon_{B_d}|^2) =$   
 $+0.0012 \pm 0.0029_{(stat)} \pm 0.0036_{(syst)}$   
 $|q/p| = 0.998 \pm 0.006_{(stat)} \pm 0.007_{(syst)}$

**BABAR PRL 88, 231801 (2002)**



So far, no experimental evidence  
of large  $CP$  violation in  $B^0$  mixing

To a good approximation:

$$|q/p| = 1 \text{ and } q/p = e^{-2i\phi_M} = -|M_{12}| / M_{12}$$



# Systematic Errors

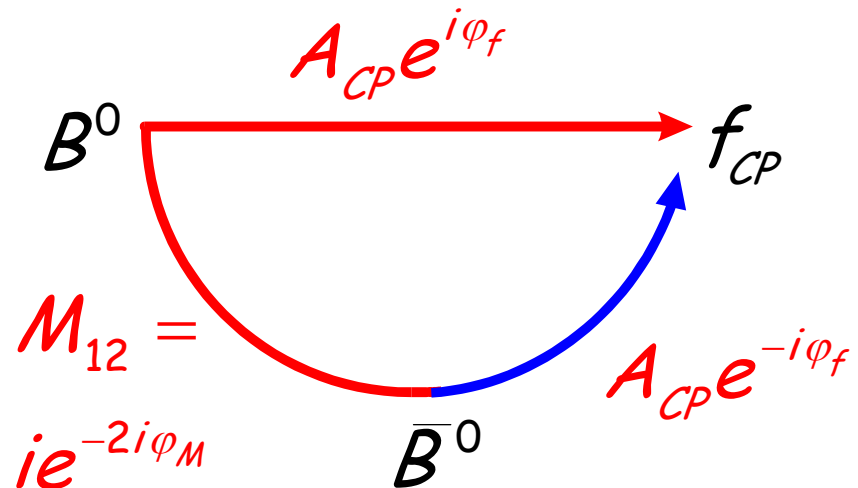
<i>Source</i>	$\sigma(A_T)$ [%]	<i>Sample</i>
<i>Detection asymmetry for electrons</i>	<i>0.5</i>	<i>Direct electrons in semileptonic B decays</i>
<i>Detection asymmetry for muons</i>	<i>0.6</i>	<i>Direct muons in semileptonic B decays</i>
<i>Non-<math>B\bar{B}</math> background asymmetry</i>	<i>0.7</i>	<i>Off-resonance data</i>
<i><math>B\bar{B}</math> background asymmetry</i>	<i>0.9</i>	<i>* On-resonance data with <math>\Delta z &lt; 100\mu\text{m}</math></i>
<i>Total</i>	<i>1.4</i>	
<i>Statistical Error</i>	<i>1.2</i>	

**\*Would be zero if one assumed  $CP$  invariance in cascade decays**



# CP Violation in the B System

- CPV through interference of decay amplitudes
- CPV through interference of mixing diagram
- CPV through interference between mixing and decay amplitudes



Directly related to CKM angles for single decay amplitude





# CP Formalism Revisited

For  $B^0$  decays, allowing for more than one amplitude contributing to the decay to  $f_{CP}$

$$\lambda_{f_{CP}} = \eta_{f_{CP}} \frac{q}{p} \cdot \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}} \leftarrow \text{Amplitude ratio}$$

CP eigenvalue  $\rightarrow$   $\eta_{f_{CP}}$   $\rightarrow$   $\frac{q}{p} \approx e^{-2i\beta}$

Full time-dependent distributions and CP asymmetry:

$$f_{CP,\pm}(\Delta t) = \left\{ \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} \left( 1 \pm S_{f_{CP}} \sin \Delta m_d \Delta t \mp C_{f_{CP}} \cos \Delta m_d \Delta t \right) \right\}$$

$$A_{f_{CP}}(\Delta t) = \frac{\Gamma(\bar{B}_{phys}^0(\Delta t) \rightarrow f_{CP}) - \Gamma(B_{phys}^0(\Delta t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{phys}^0(\Delta t) \rightarrow f_{CP}) + \Gamma(B_{phys}^0(\Delta t) \rightarrow f_{CP})}$$

$$= C_{f_{CP}} \cos(\Delta m_d \Delta t) - S_{f_{CP}} \sin(\Delta m_d \Delta t)$$

$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$$

$$S_{f_{CP}} = \frac{-2 \text{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$$



# Search for Direct CP in Golden Sample

---

Redo fits tagged time distributions of CP sample with sine and cosine terms (assuming  $\Delta\Gamma = 0$ )

If more than one amplitude contributes  
 $|\lambda|$  might be different from 1

Probing new physics: only use  $\eta_{CP} = -1$  sample  
(contains no mixing background)

$$BABAR: |\lambda_{c\bar{c}s}| = 0.948 \pm 0.051_{(stat)} \pm 0.017_{(syst)}$$

$$Belle: |\lambda_{c\bar{c}s}| = 0.950 \pm 0.049_{(stat)} \pm 0.026_{(syst)}$$

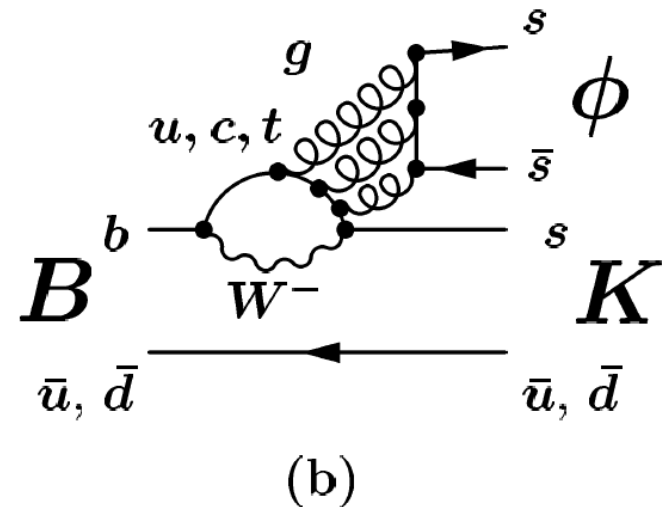
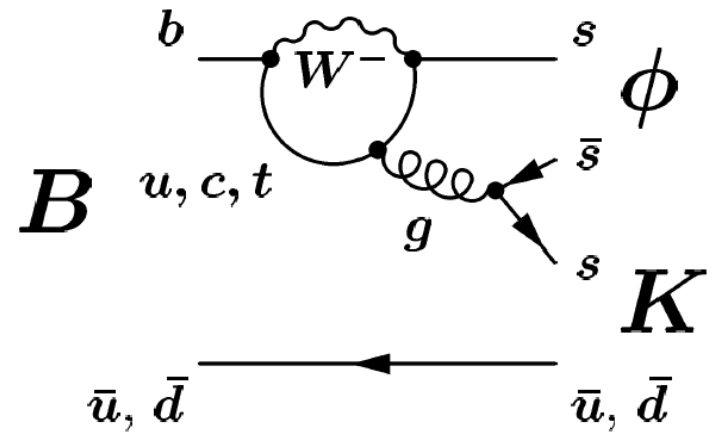
*No evidence of direct CP violation due to decay amplitude interference*

Coefficient of the "sine" term unchanged



# Other Modes for $\sin 2\beta$

- Provide an independent measurement of CP violation
- Some possible  $b \rightarrow s\bar{s}s$  modes
  - $\phi K_S$  is  $CP = -1$  with  $\text{Im}\lambda = -\sin 2\beta$ 
    - Sensitive to new physics in  $b \rightarrow s$  loop diagram
    - Pure  $b \rightarrow s$  penguin process?
  - Other examples
    - $\eta' K_S$  is  $CP = +1$
    - $K^+ K^- K_S$  appears to be mostly  $CP = +1$  according to Belle
- Possible double-charm modes
  - $B \rightarrow D^{*+} D^{*-}$  or  $B \rightarrow D^* D$  channels
    - No  $K_S$  mixing, but penguins?
- Other charmonium modes

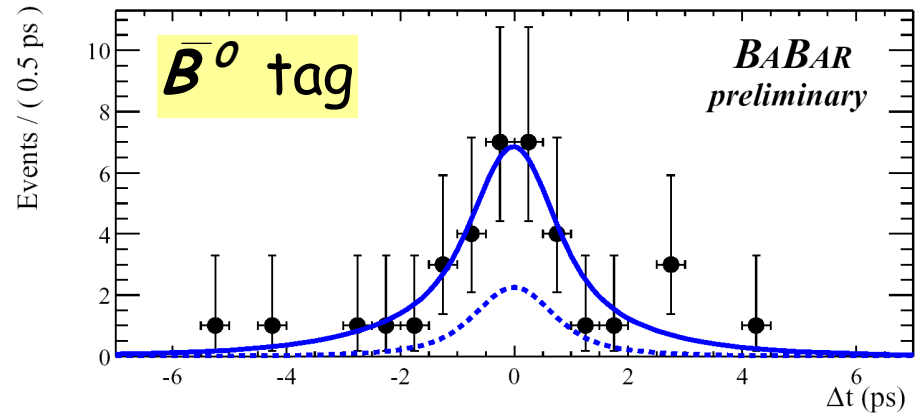
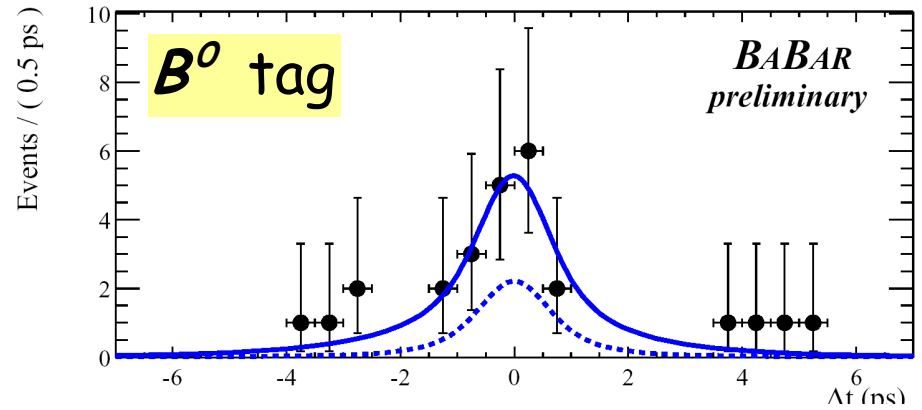
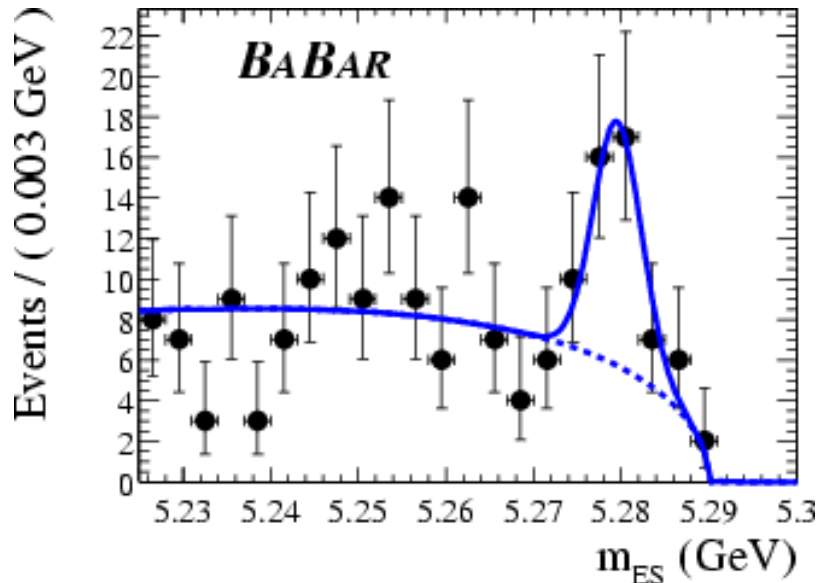


# BABAR Results for $\phi K_S$

**BABAR**

81.3 fb<sup>-1</sup>

$N_{\text{cand}} = 66$   
Purity = 50%



If pure penguin:  $S_{\phi K_S} = \sin 2\beta$

BABAR-CONF-02/016, hep-ex/0207070

Fix  $|\lambda_{\phi K_S}| = 1$

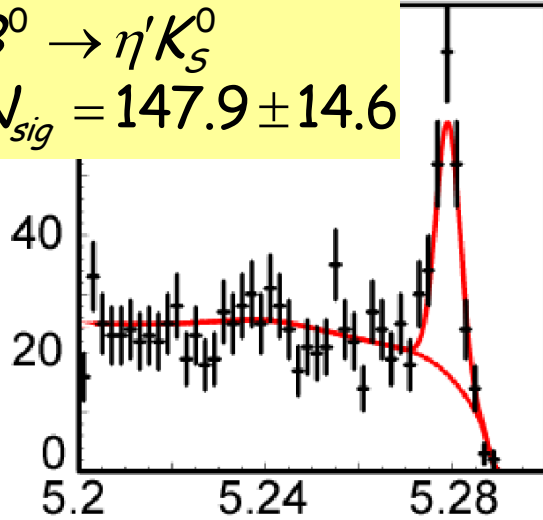
$S_{\phi K_S} = -0.19^{+0.52}_{-0.50}(\text{stat}) \pm 0.09(\text{syst})$



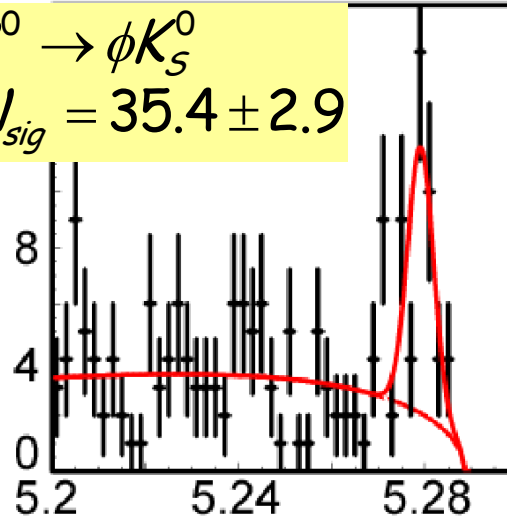
# Belle Results for $b \rightarrow sss$

BELLE-CONF-0225

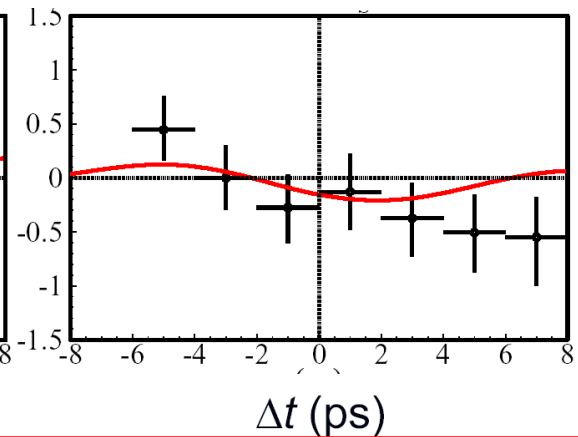
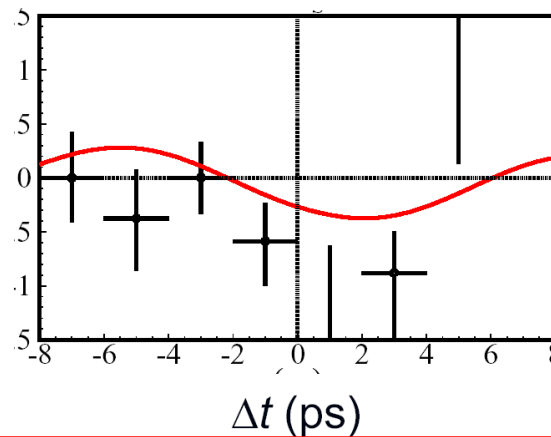
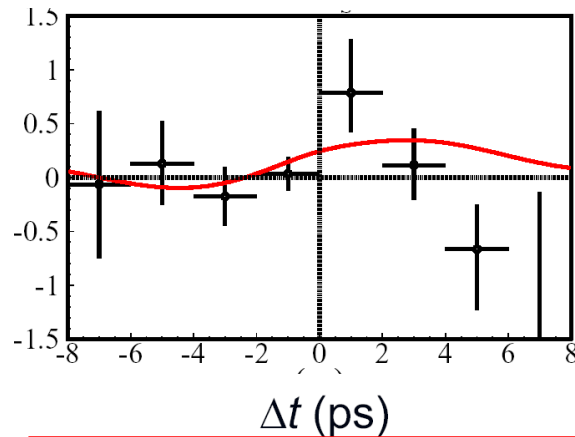
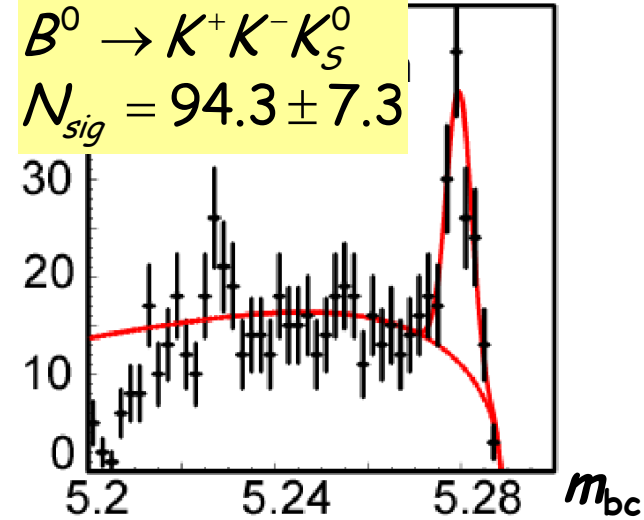
$B^0 \rightarrow \eta' K_S^0$   
 $N_{sig} = 147.9 \pm 14.6$



$B^0 \rightarrow \phi K_S^0$   
 $N_{sig} = 35.4 \pm 2.9$



$B^0 \rightarrow K^+ K^- K_S^0$   
 $N_{sig} = 94.3 \pm 7.3$



$-S_{\eta'K} = +0.76 \pm 0.36^{+0.05}_{-0.06}$	$S_{\phi K_S} = -0.73 \pm 0.64 \pm 0.18$	$-S_{\eta'K} = +0.52 \pm 0.46 \pm 0.11^{+0.27}_{-0.03}$
$C_{\eta'K} = -0.26 \pm 0.22 \pm 0.03$	$C_{\phi K_S} = +0.56 \pm 0.41 \pm 0.12$	$C_{\eta'K} = +0.42 \pm 0.36 \pm 0.09^{+0.03}_{-0.22}$

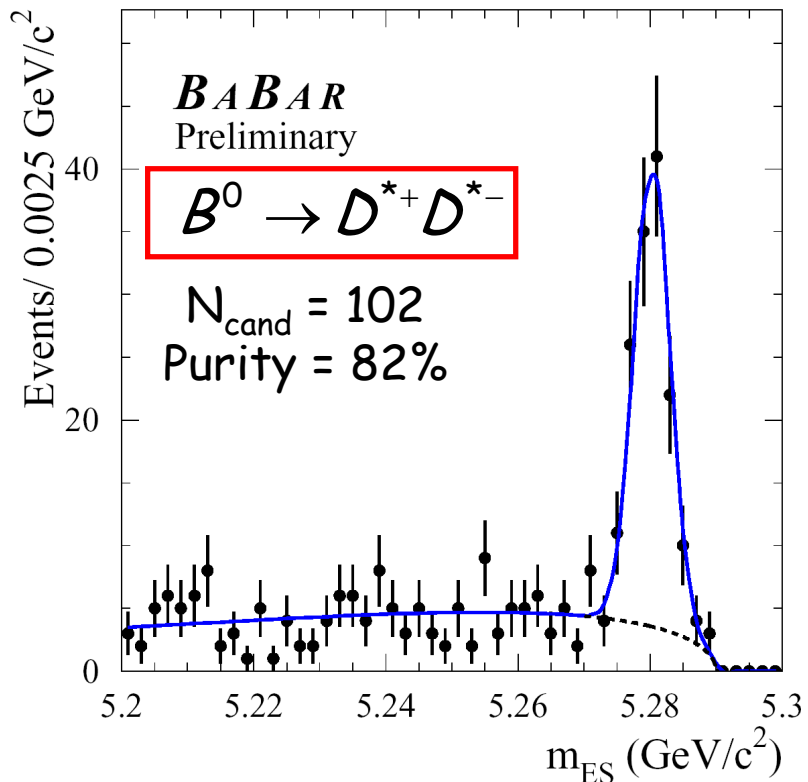


# More CP channels: $B \rightarrow D^{*+} D^{*-}$

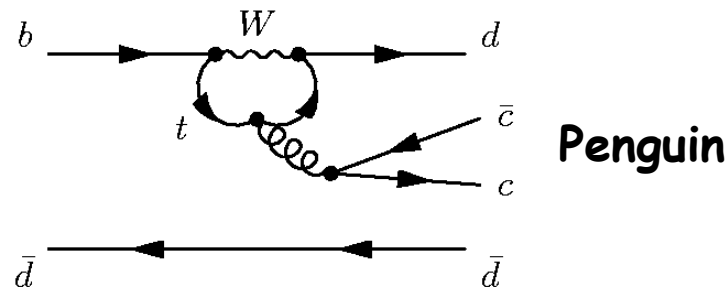
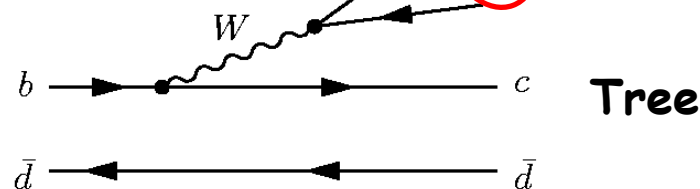
$b \rightarrow c\bar{c}d$



**BABAR**  
81.3 fb<sup>-1</sup>



**Cabibbo suppressed**



- No  $K_S$  mixing contribution
- Potential for significant Penguin contamination

$\text{Im } \lambda_{c\bar{c}d} \sim \sin 2\beta$

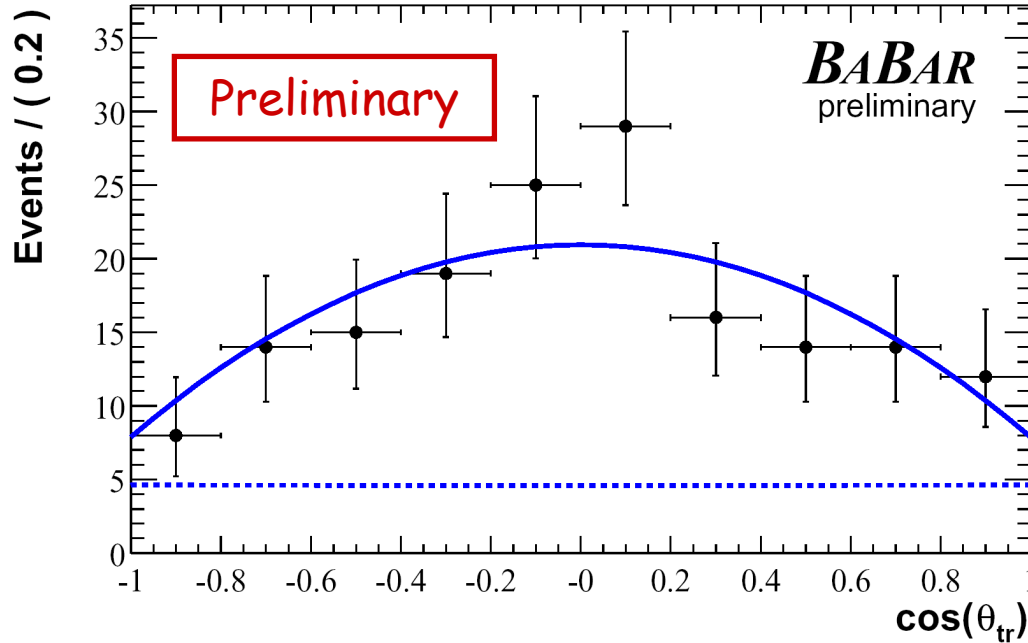
BABAR-CONF-02/014, hep-ex/0207072



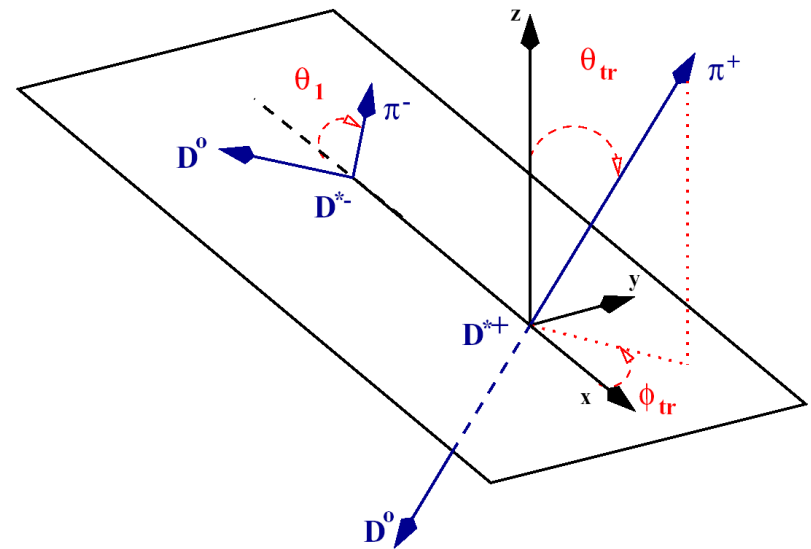
# CP Composition of $B^0 \rightarrow D^{*+}D^{*-}$

➤ Measure small CP odd fraction (corrected for acceptance):

$$R_{\perp} = 0.07 \pm 0.06 \text{ (stat)} \pm 0.03 \text{ (syst)}$$



$P \rightarrow VV$ : mixture of CP states



$$\frac{d\Gamma}{\Gamma d\cos\vartheta_{tr}} = \frac{3}{4}(1 - R_{\perp})\sin^2\vartheta_{tr} + \frac{3}{2}R_{\perp}\cos^2\vartheta_{tr}$$



**BABAR**  
81.3 fb<sup>-1</sup>



# The PDF

➤ The decay rate  $f_+(f_-)$  for a  $B$  tagged as a  $\bar{B}^0$  ( $B^0$ )

$$f_{\pm}(\Delta t) = \frac{\Gamma}{2} e^{-\Gamma|\Delta t|} \{ O_{\mp} [S \sin \Delta m_d \Delta t + C \cos \Delta m_d \Delta t] \}$$

$$O = \frac{3}{4} (1 + K) \sin^2 \theta_{tr} + \frac{3}{2} (1 - K) \cos^2 \theta_{tr}$$

$$C = \frac{3}{4} (1 + K) \sin^2 \theta_{tr} \frac{1 - |\lambda_+|^2}{1 + |\lambda_+|^2} + \frac{3}{2} (1 - K) \cos^2 \theta_{tr} \frac{1 - |\lambda_{\perp}|^2}{1 + |\lambda_{\perp}|^2}$$

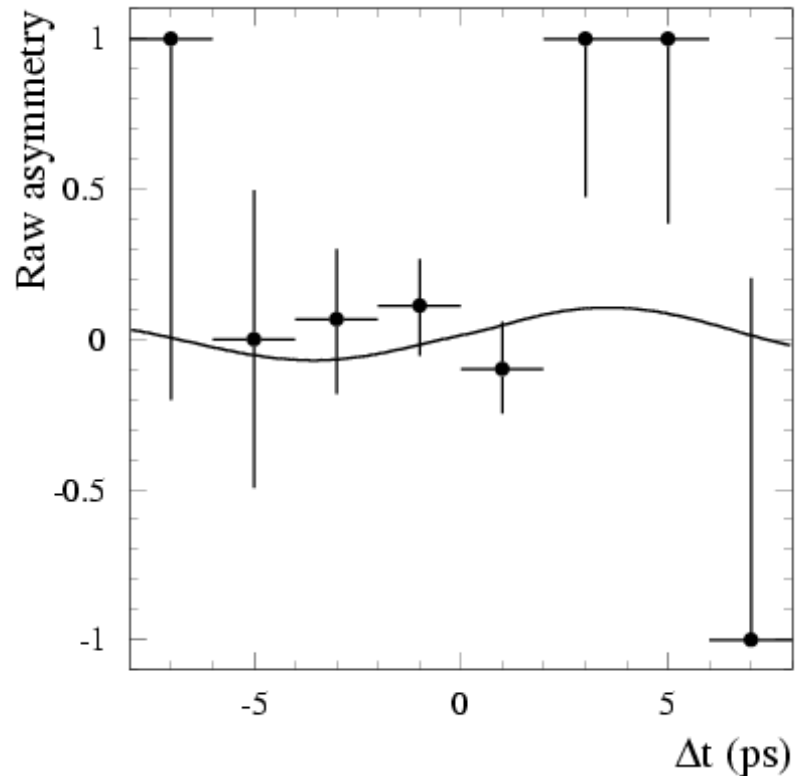
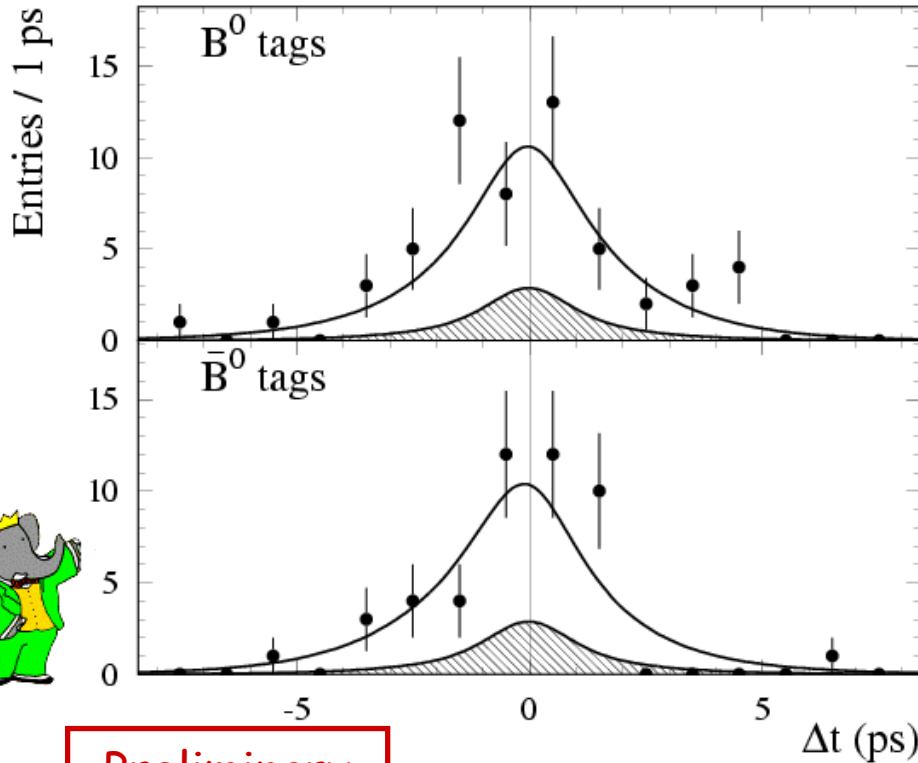
$$S = - \left[ \frac{3}{4} (1 + K) \sin^2 \theta_{tr} \frac{2 \operatorname{Im}(\lambda_+)}{1 + |\lambda_+|^2} - \frac{3}{2} (1 - K) \cos^2 \theta_{tr} \frac{2 \operatorname{Im}(\lambda_{\perp})}{1 + |\lambda_{\perp}|^2} \right]$$

3 parameters:  $|\lambda_+|, \operatorname{Im} \lambda_+, |\lambda_{\perp}| = 1, \operatorname{Im} \lambda_{\perp} = -0.741, K$   
since  $CP$ -odd component small





# CP Asymmetry Fit Results



Preliminary

$$|\lambda_+| = 0.98 \pm 0.25_{(stat)} \pm 0.09_{(syst)}$$

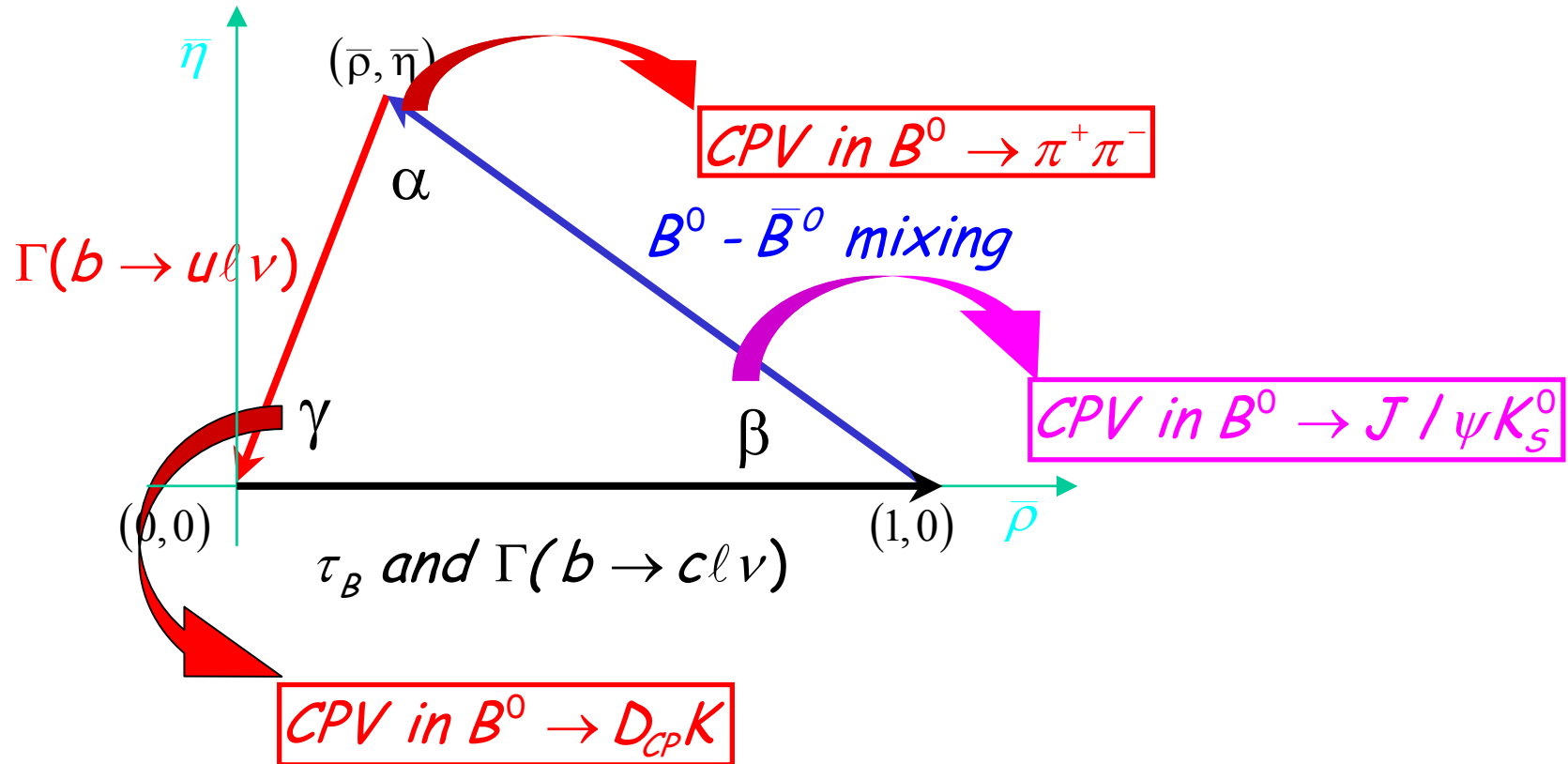
$$\text{Im } \lambda_+ = 0.31 \pm 0.43_{(stat)} \pm 0.10_{(syst)}$$

If Penguins are negligible

$|\lambda_+| = 1$  and  $\text{Im } \lambda_+ = -\sin 2\beta$   
i.e., about  $2.7\sigma$  difference



# Testing the Origins of CPV



# CP Violation in $B^0 \rightarrow \pi^+ \pi^-$ Decays

Decay distributions  $f_+(f_-)$  when tag =  $B^0(\bar{B}^0)$

$$f_{\pm}(\Delta t) = \frac{\Gamma}{4} e^{-\Gamma \Delta t} [1 \pm S_{f_{CP}} \sin \Delta m_d \Delta t \mp C_{f_{CP}} \cos \Delta m_d \Delta t]$$

For single weak phase from tree diagram

$$\lambda \equiv \frac{q \bar{A}_f}{p A_f} = \eta_f e^{-2i(\beta+\gamma)} = \eta_f e^{2i\alpha}$$

$$C_{\pi\pi} = 0, S_{\pi\pi} = \sin 2\alpha$$

With additional weak phase from penguin diagram

$|\lambda| \neq 1 \Rightarrow$  must fit for direct CP  
 $\text{Im}(\lambda) \neq \sin 2\alpha \Rightarrow$  need to relate asymmetry to  $\alpha$

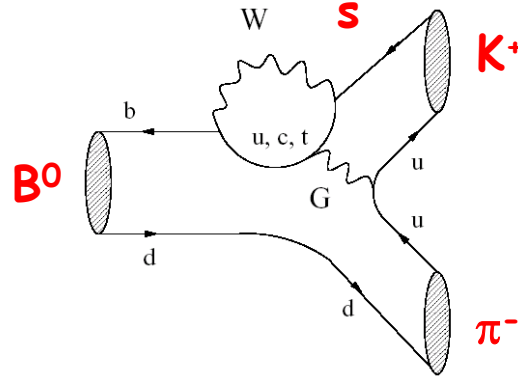
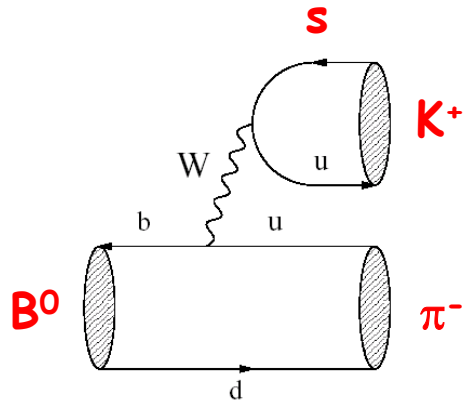
$$C_{\pi\pi} \neq 0, S_{\pi\pi} = \sin 2\alpha_{\text{eff}}$$



# Competing Amplitudes for $B \rightarrow h^+ h^-$

Tree diagrams

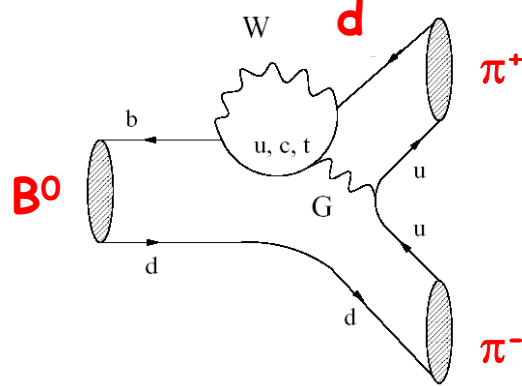
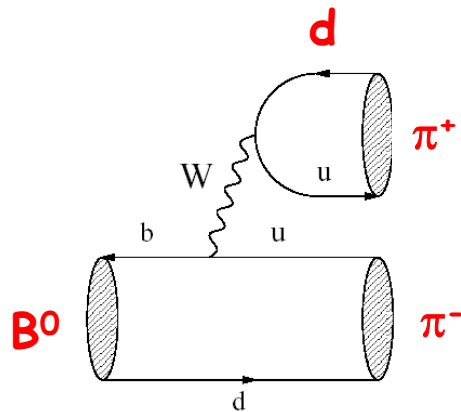
Penguin diagrams



$$BF(B^0 \rightarrow K^+ \pi^-) = (17.8 \pm 1.1 \pm 0.8) \times 10^{-6}$$

Penguin dominated:  
 $A_{K\pi} = \lambda^2 e^{i\gamma} T + P$

Potential direct  $CPV$  and constraints on  $\gamma$



$$BF(B^0 \rightarrow \pi^+ \pi^-) = (5.4 \pm 0.7 \pm 0.4) \times 10^{-6}$$

$|Penguin| \sim 0.3 |Tree|$

Complicates extraction of  $\alpha$  from mixing induced  $CPV$



# Analysis Overview

---

## ➤ *Analysis issues: charmless two-body B decays*

- Rare decays!  $BR \sim 10^{-5}-10^{-6} \rightarrow$  need lots of data ( $B$  Factories)
- Large background from  $e^+e^- \rightarrow q\bar{q} \rightarrow$  need background suppression
- Ambiguity between  $\pi$  and  $K \rightarrow$  need excellent PID (DIRC or ACC)

## ➤ *CP analysis issues:*

- Need to determine vertex position of both  $B$  mesons  $\rightarrow$  standard vertex separation algorithms
- Need to know the flavor of "other"  $B \rightarrow$  standard tagging algorithms

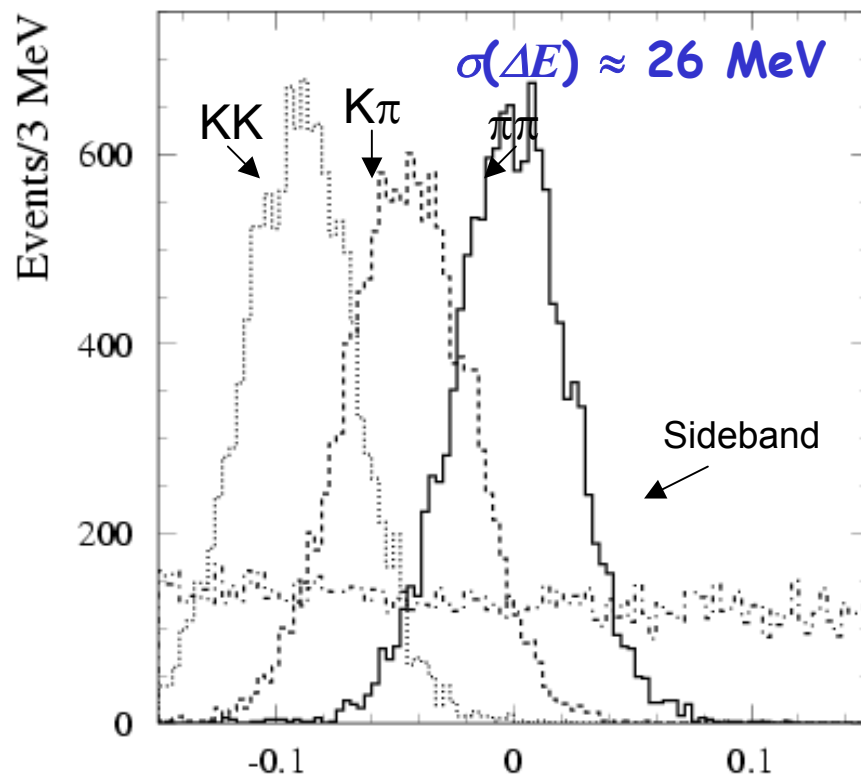
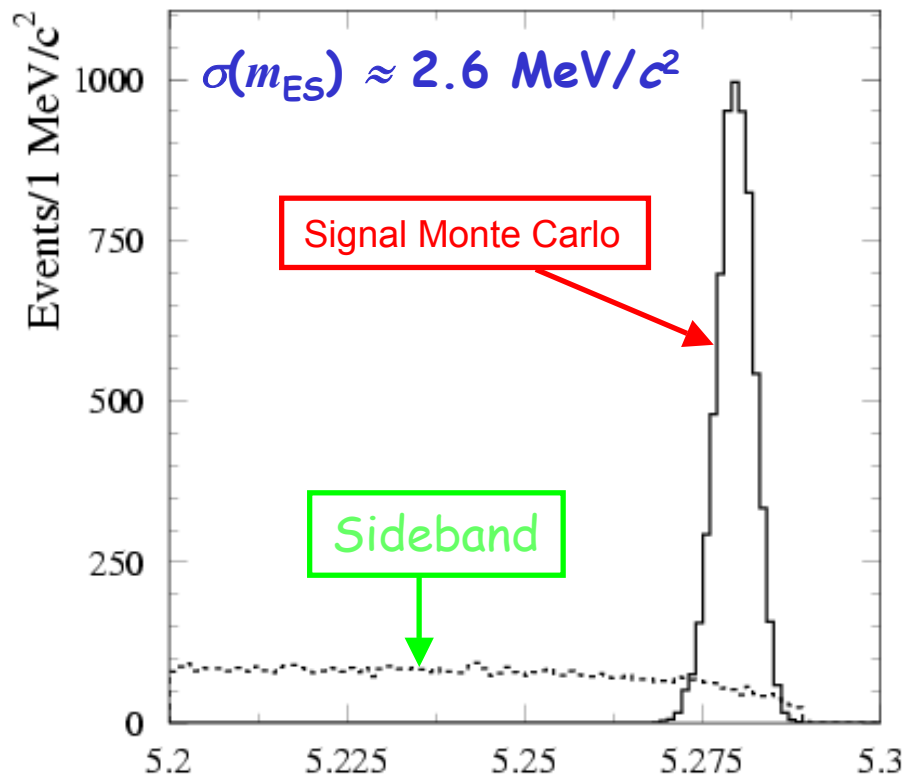
## ➤ *Analysis proceeds at BABAR in two steps:*

- Use kinematic, topological, and PID information in a global ML fit to extract yields for  $\pi\pi$ ,  $K\pi$ , and  $KK$  decays, as well as the asymmetry  $A_{K\pi}$ 
  - Exclude vertexing & tagging information to avoid systematic error
- Add vertexing and tagging information to extract  $S_{\pi\pi}$  and  $C_{\pi\pi}$ 
  - Yields and  $A_{K\pi}$  fixed to result of the first fit



# Kinematics

Pion mass assumed for all tracks, so shift in  $\Delta E$  for  $K\pi$  and  $KK$  decays



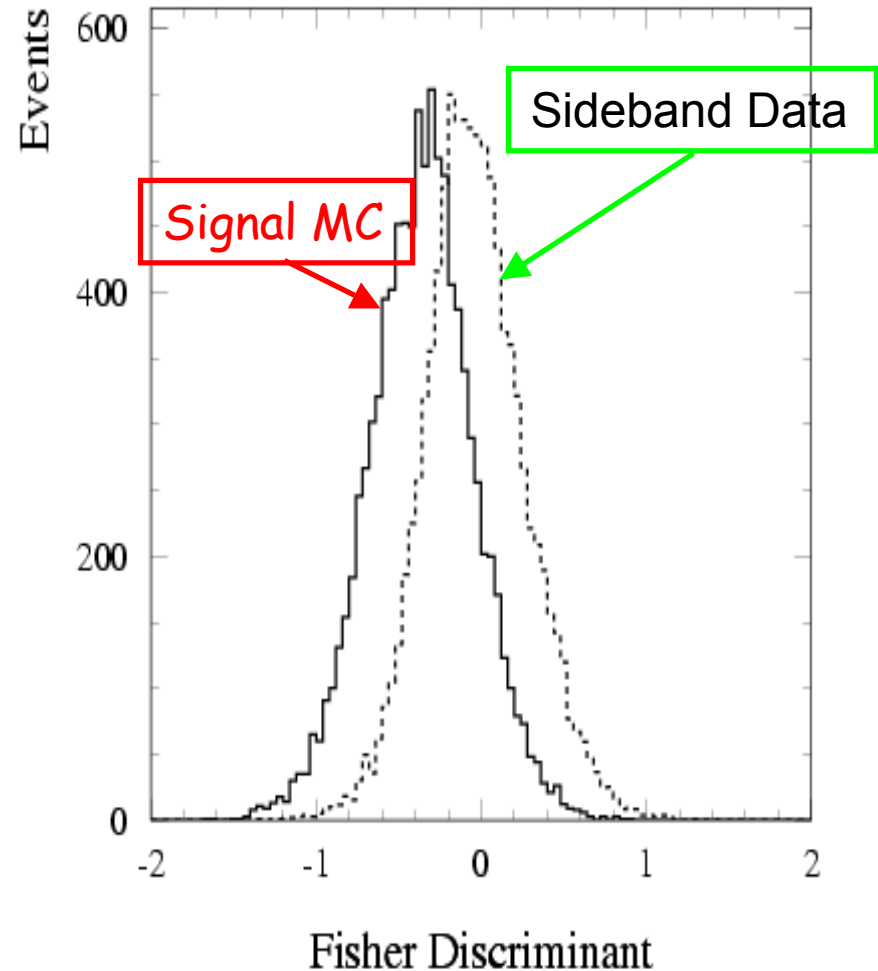
$$m_{ES} = \sqrt{(E_{beam}^*)^2 - (\mathbf{p}_B^*)^2} \text{ GeV}/c^2$$

$$\Delta E = E_B^* - E_{beam}^* \text{ GeV}$$



# Background Suppression

- *Background is due to light-quark production  $e^+e^- \rightarrow qq$  ( $q=u, d, s, c$ )*
  - Jetty topology, distinct from spherical B decays
- *Cut on angle  $\theta_S$  between sphericity axes of B candidate and the remaining particles in the event:*
  - $|\cos(\theta_S)| < 0.8$ , removes 83% bkg, 20% signal
- *Define Fisher discriminant  $F$  derived from momentum flow in the event*
  - Used directly in the ML fit



# Branching Fraction Fits

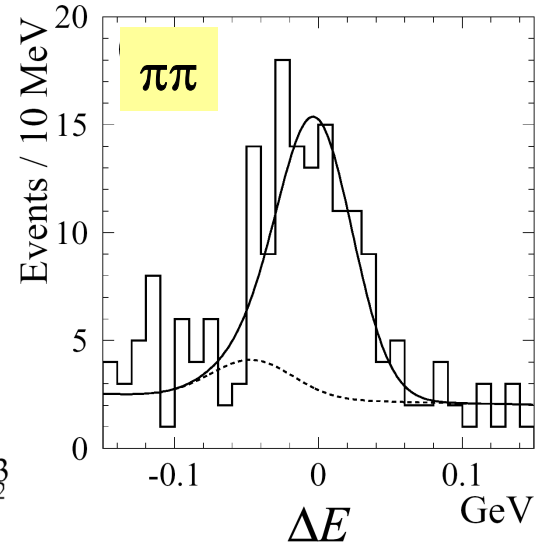
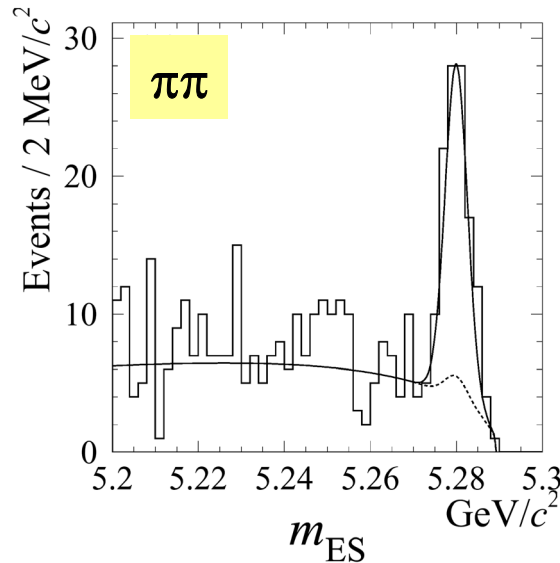
Projections in  
 $m_{ES}$  and  $\Delta E$

26070 two-prong  
candidates (97%  
background, mostly  
continuum)

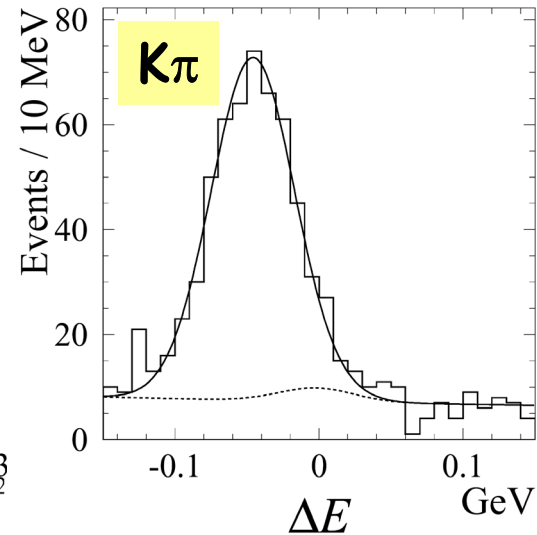
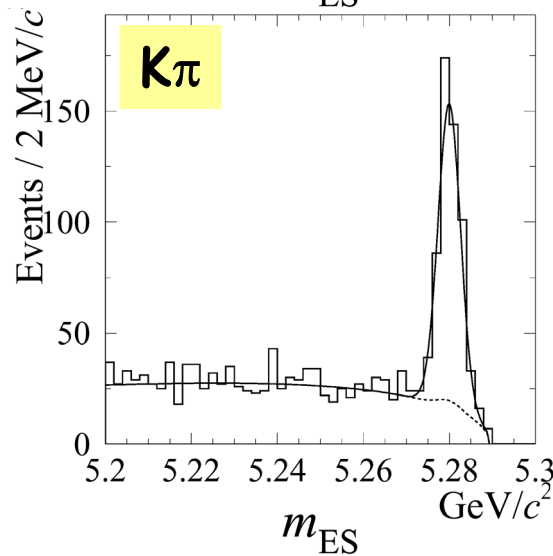
BF Likelihood  
includes PDFs for:  
 $m_{ES}$ ,  $\Delta E$ , Fisher,  $\theta_c$   
for + & - tracks



**BABAR**  
81.3 fb<sup>-1</sup>



Proj eff:  
52%



Proj eff:  
79%





# Branching Fraction Results

Preliminary

Mode	Yield	BR [ $10^{-6}$ ]	$A_{CP}(K\pi)$
$B^0 \rightarrow \pi^+ \pi^-$	$157 \pm 19$	$4.7 \pm 0.6 \pm 0.2$	
$B^0 \rightarrow K^+ \pi^-$	$589 \pm 30$	$17.9 \pm 0.9 \pm 0.7$	$-0.102 \pm 0.050 \pm 0.016$
$B^0 \rightarrow K^+ K^-$	$1 \pm 8$	$< 0.6$ [90%CL]	

$$A_{K\pi} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) - \Gamma(B^0 \rightarrow K^+ \pi^-)}{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) + \Gamma(B^0 \rightarrow K^+ \pi^-)} \sim \left| \frac{P}{T} \right| \sin \gamma \sin \delta$$



**BABAR**  
81.3 fb<sup>-1</sup>

BABAR-PUB-02/009, hep-ex/0207055



Aug 5-7, 2002

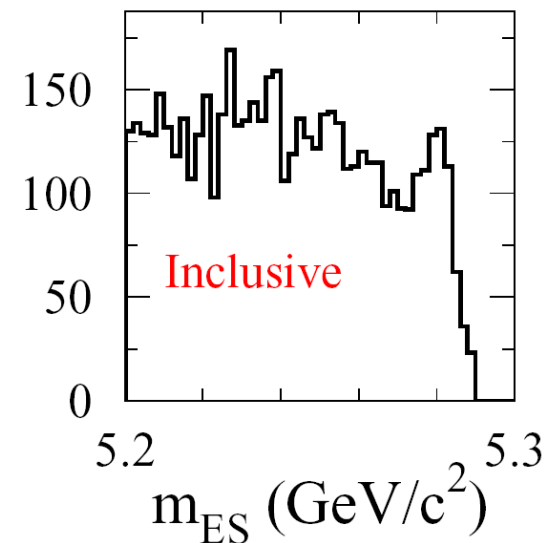
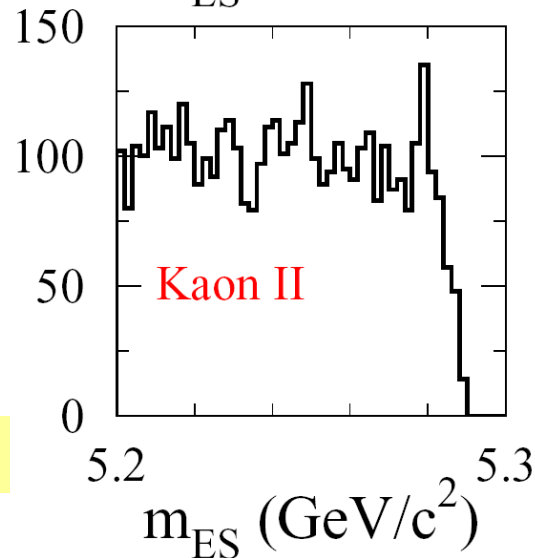
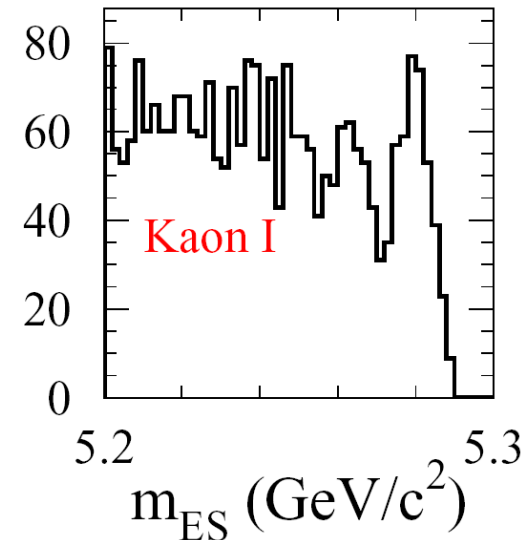
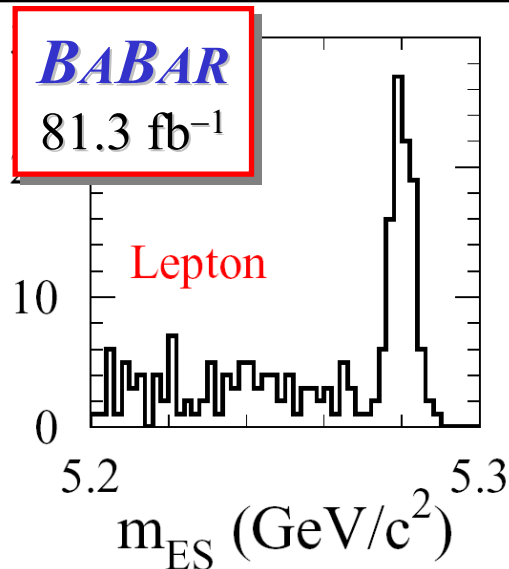
D.MacFarlane at SSI 2002

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# Two-Body Tagged Sample

- o Tagging efficiency is very different for signal and bkg
  - Strong bkg suppression in lowest mistag categories (Lepton/Kaon)
  - Different bkg tagging efficiencies for  $\pi\pi$ ,  $K\pi$ ,  $KK$
- o Sum of  $\pi^+\pi^-/K^+\pi^-$ : No particle ID used until the fit is performed

Untagged category also used



# CP Asymmetry Results from BABAR



Fit projection in sample of  $\pi\pi$ -selected events

For CP asymmetry add tagging and  $\Delta t$  measurement to likelihood but fix yields and  $A_{K\pi}$

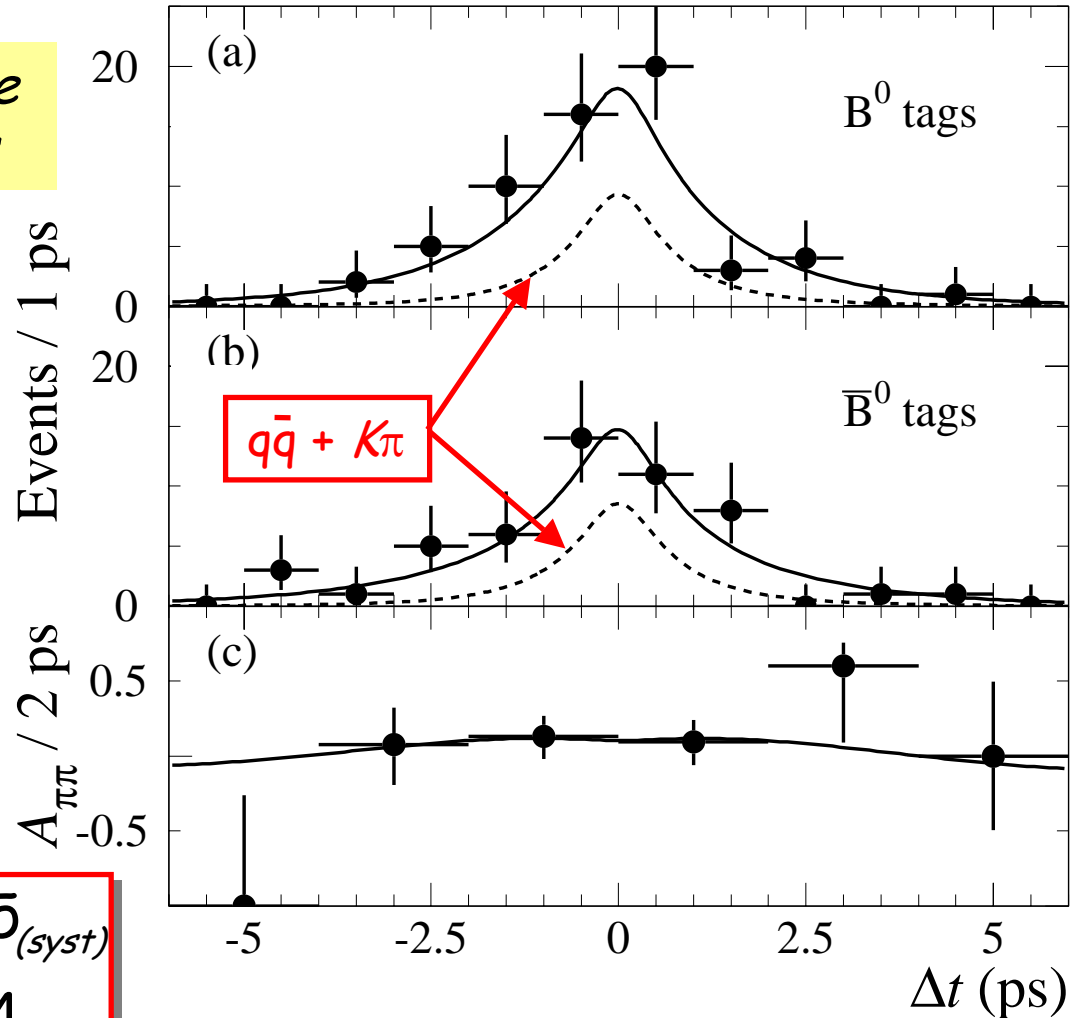
Preliminary

**BABAR**

81.3 fb<sup>-1</sup>

$$S_{\pi\pi} = +0.02 \pm 0.34_{(stat)} \pm 0.05_{(syst)}$$

$$C_{\pi\pi} = -0.30 \pm 0.25_{(stat)} \pm 0.04_{(syst)}$$

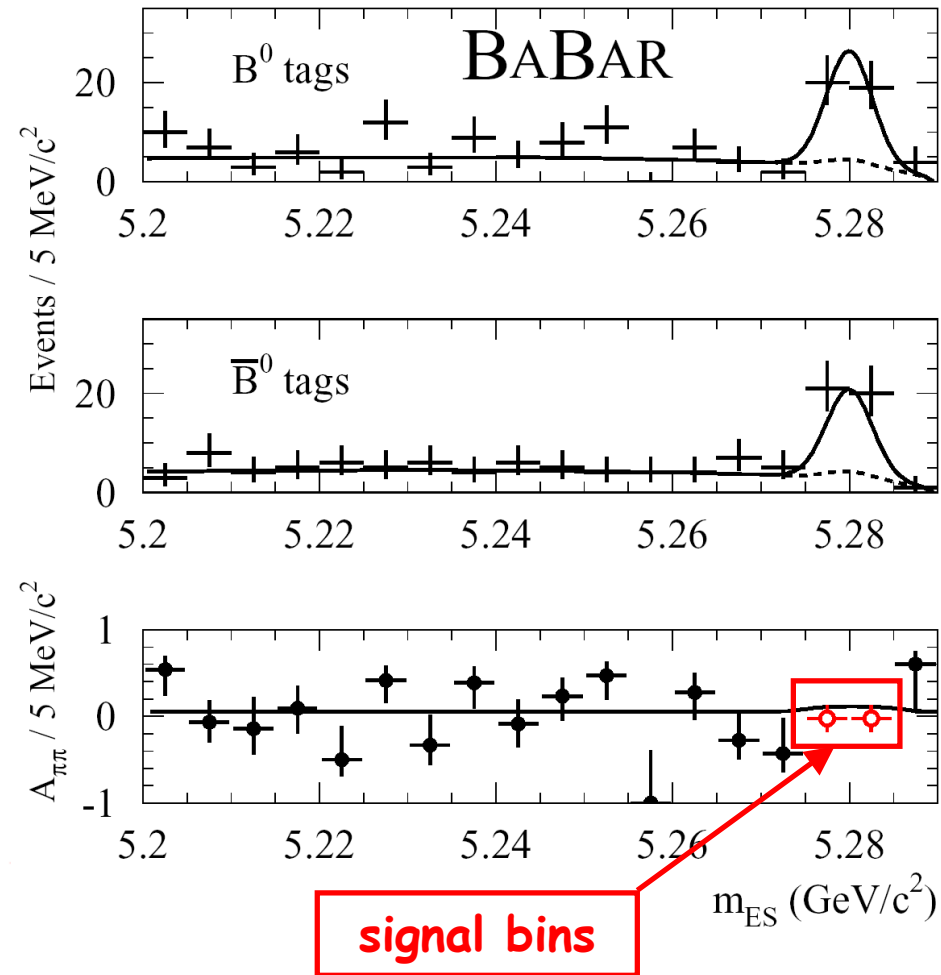


# Crosschecks

- *Inspect  $\pi\pi$ -selected sample*
  - 2-param fit consistent with full fit
  - Asymmetry vs.  $m_{ES}$ 
    - Yields consistent with measured value of  $C_{\pi\pi}$ , which do not suggest large direct  $CP$  violation
  - Toy MC generated over all allowed values of  $S_{\pi\pi}$  and  $C_{\pi\pi}$ 
    - Expected errors consistent with data
    - No significant bias observed
- *Validated in large samples of signal and background MC events*
- *Systematic errors dominated by uncertainty in PDF shapes*

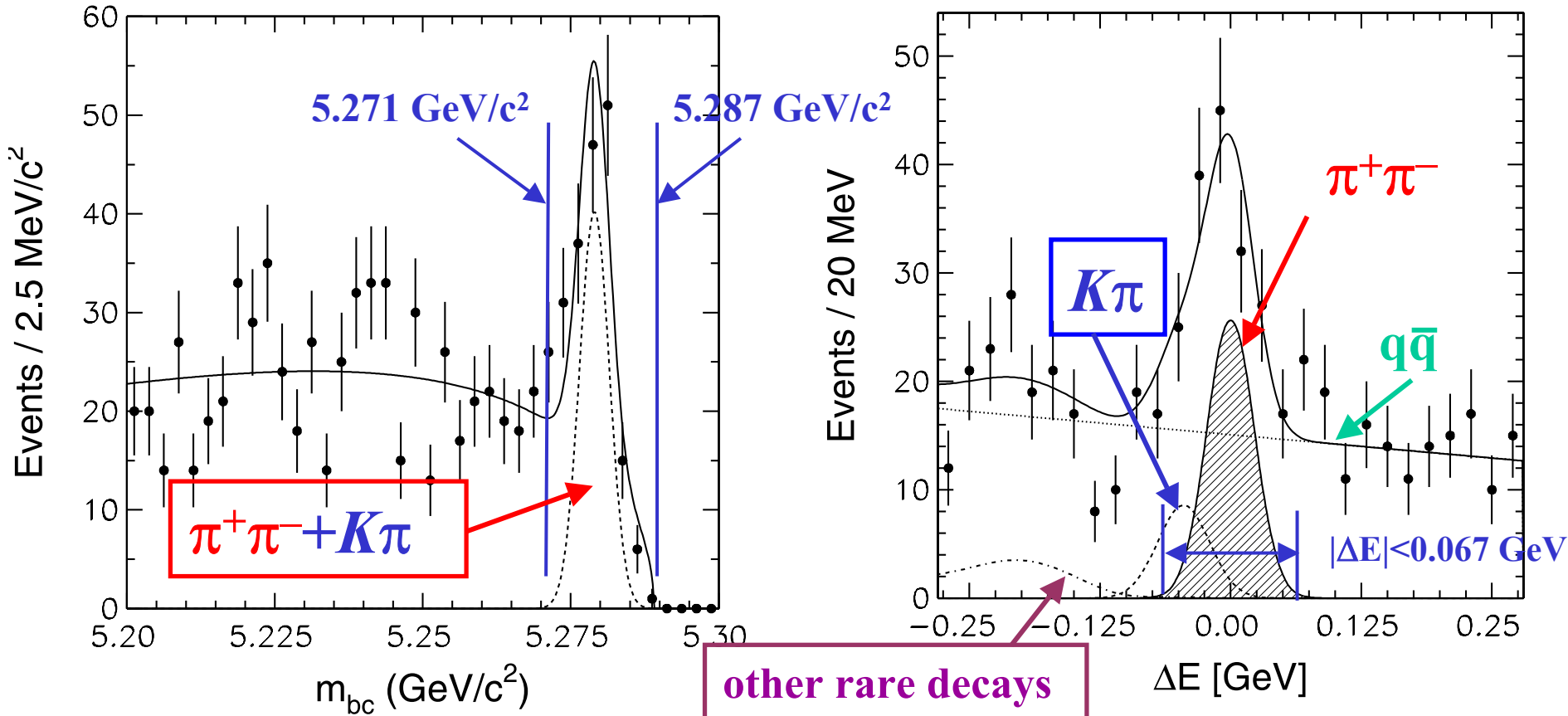


$A_{\pi\pi}$  vs.  $m_{ES}$  in sample of  $\pi\pi$ -selected events



# Belle Signal for $B \rightarrow \pi^+ \pi^-$

Reject most of  $K\pi$  feedthrough with PID systems



$$N(\pi\pi) = 73.5 \pm 13.8$$

$$N(K\pi) = 28.4 \pm 12.5$$

BELLE, hep-ex/0204002

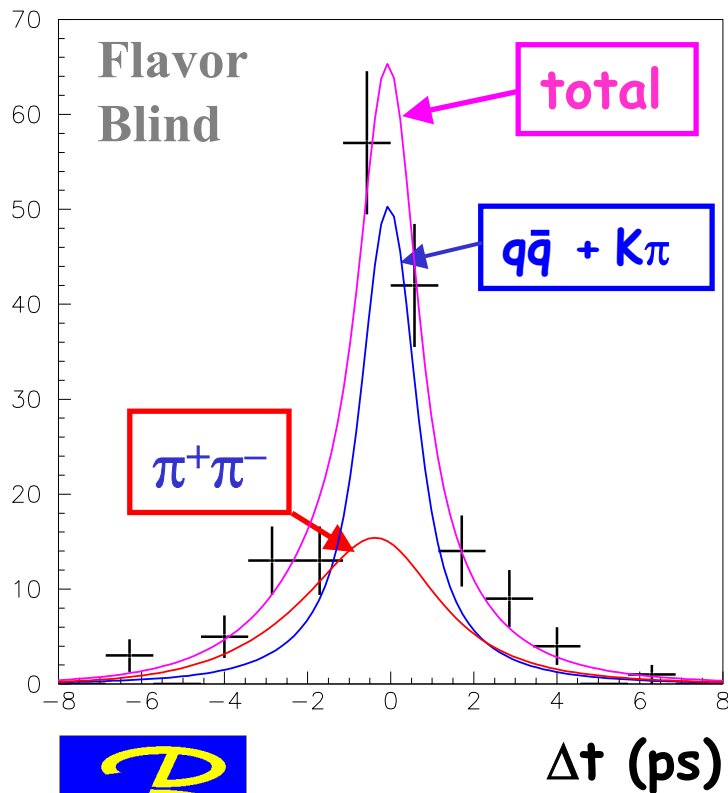


**BELLE**  
41.8  $\text{fb}^{-1}$

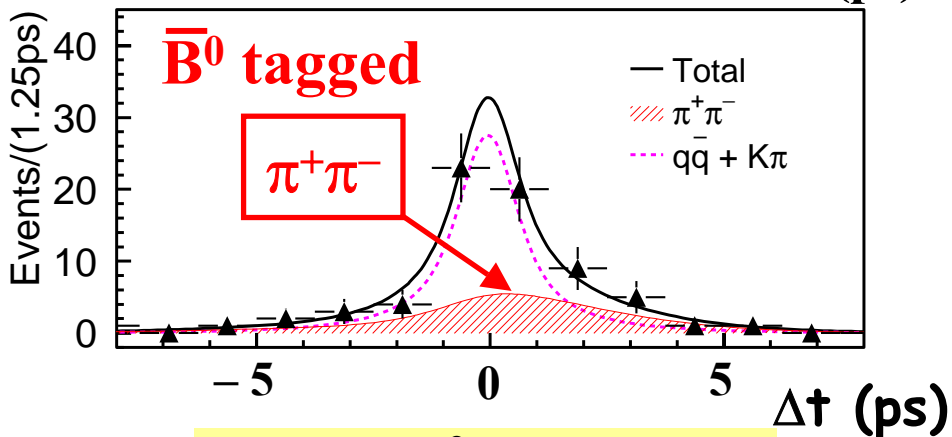
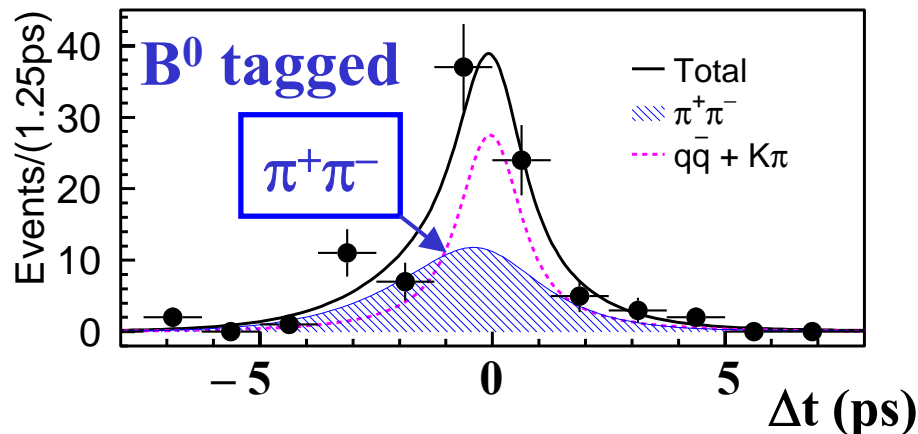


# $B \rightarrow \pi^+ \pi^-$ Time Distributions

162 events after vertexing and flavor tagging  
 $|\Delta E| < 0.067$  GeV



92  $B^0$  events  
 39.9  $B^0 \rightarrow \pi^+ \pi^-$  events



70  $\bar{B}^0$  events  
 23.4  $\bar{B}^0 \rightarrow \pi^+ \pi^-$  events



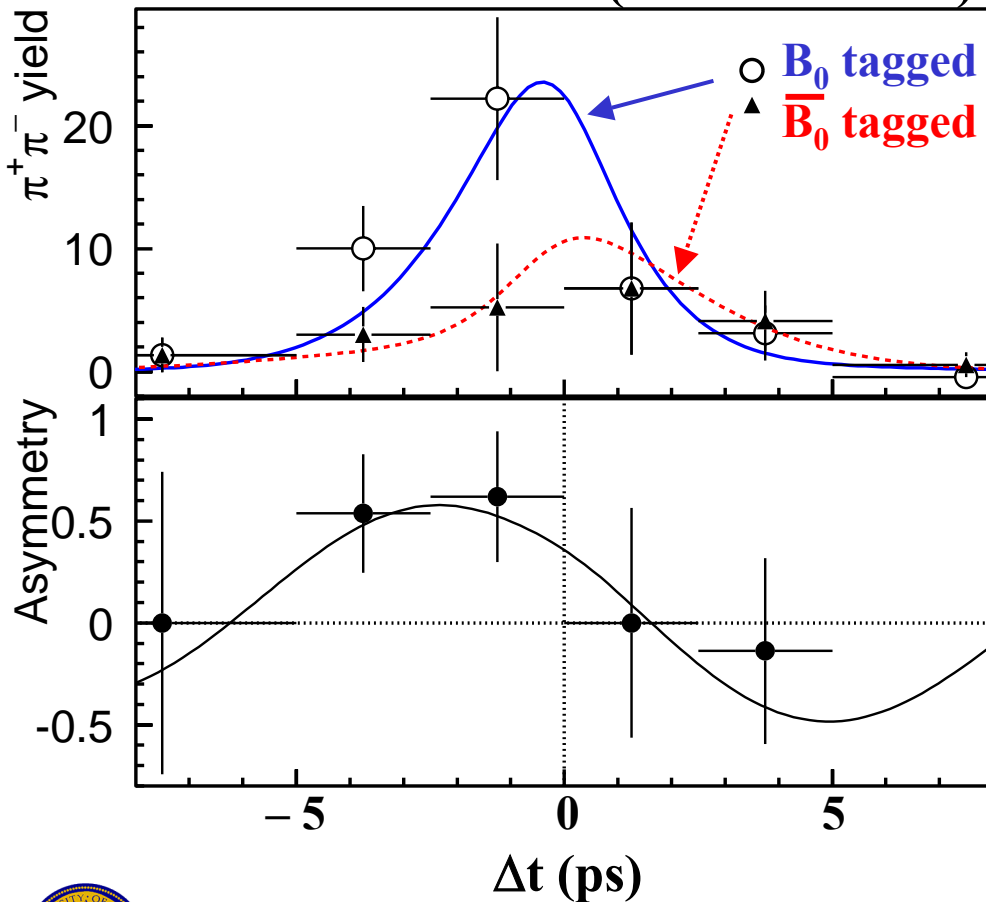
# $B \rightarrow \pi^+ \pi^-$ Fit Result

BELLE  
41.8 fb<sup>-1</sup>



$\pi^+ \pi^-$  sample

(BG subtracted)

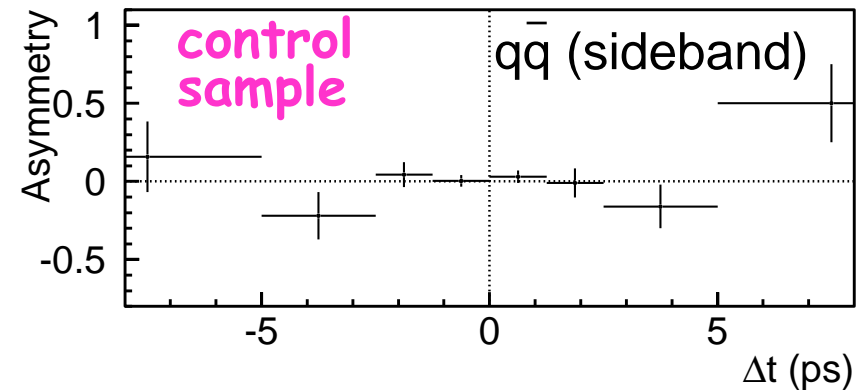


$$A_{\pi\pi} = -C_{\pi\pi}$$

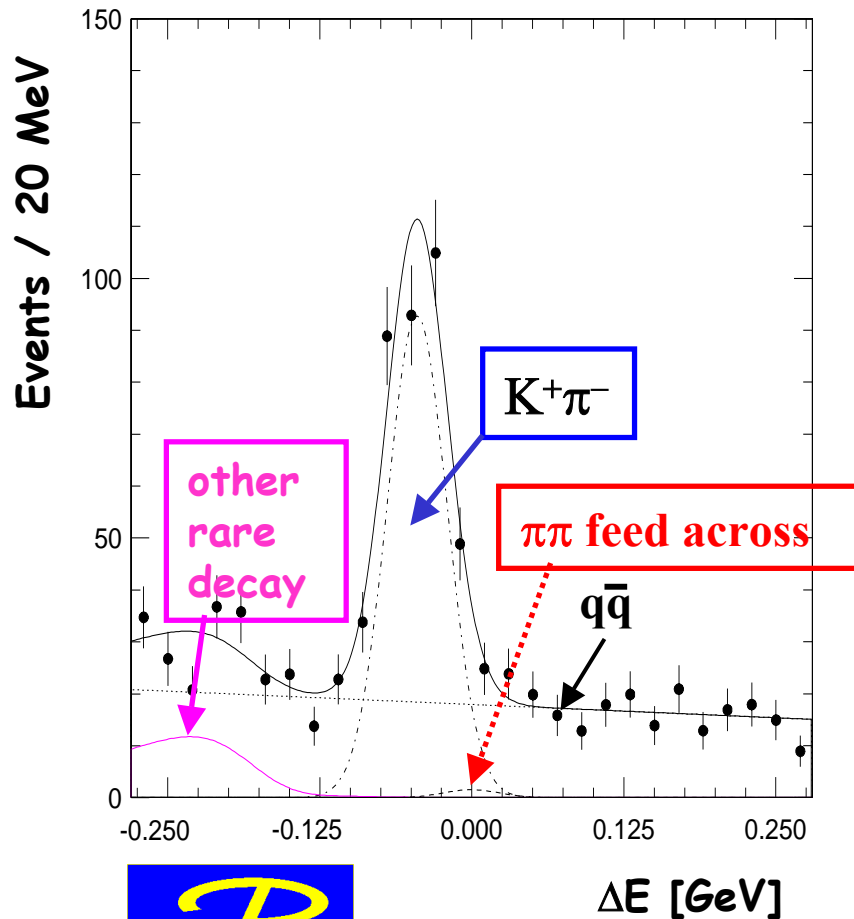
$$A_{\pi\pi} = +0.94^{+0.25}_{-0.31} (stat) \pm 0.09 (syst)$$

$$S_{\pi\pi} = -1.21^{+0.38}_{-0.17} (stat) \pm 0.16^{+0.16}_{-0.13} (syst)$$

BELLE, hep-ex/0204002



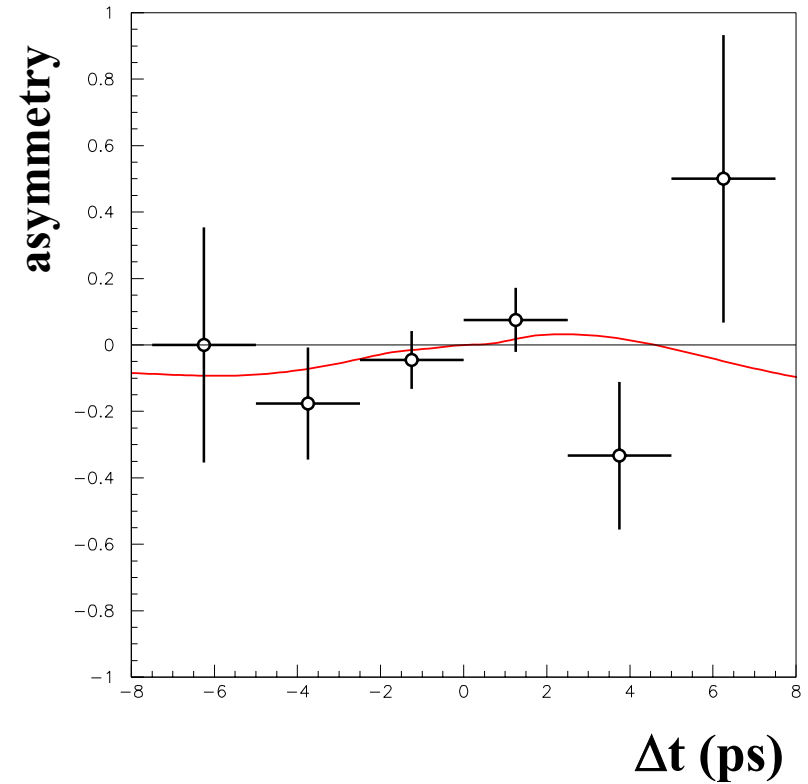
# Crosscheck with $B \rightarrow K^+\pi^-$ Sample



Null Asymmetry

$$A_{K\pi} = 0.07 \pm 0.17$$

$$C_{\pi\pi} = 0.15 \pm 0.24$$

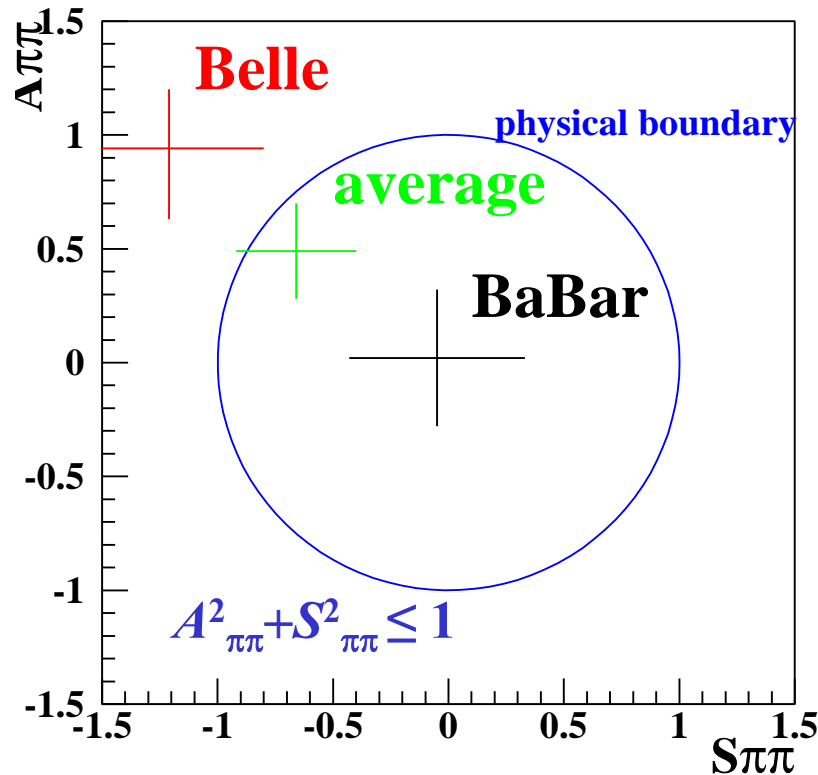




# Comparison of Results

$$A_{\pi\pi} = -C_{\pi\pi}$$

	<i>BABAR</i>	<i>Belle</i>
$A_{\pi\pi}$	$+0.30 \pm 0.25 \pm 0.04$	$+0.94_{-0.31}^{+0.25} \pm 0.09$
$S_{\pi\pi}$	$+0.02 \pm 0.34 \pm 0.05$	$-1.21_{-0.17}^{+0.38} \pm_{-0.13}^{+0.16}$



# Interpretation?

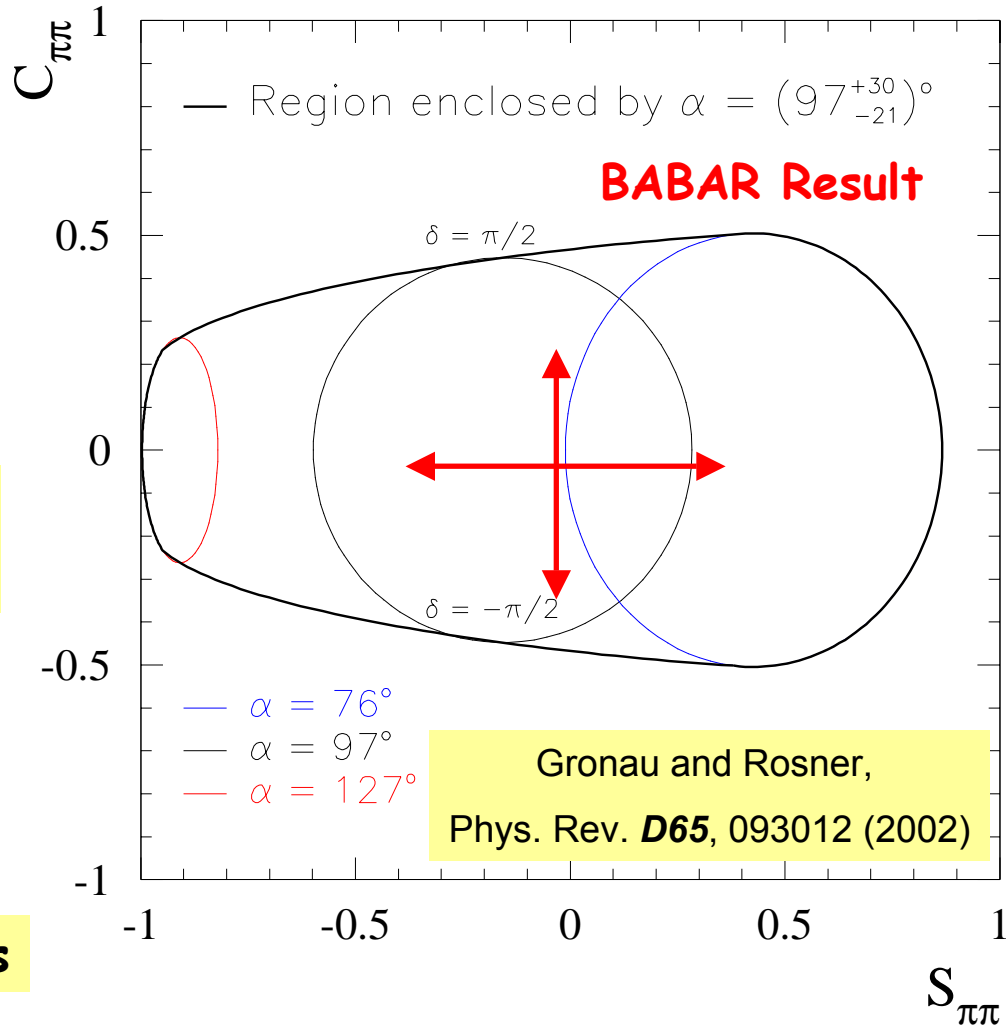


$S_{\pi\pi}$  and  $C_{\pi\pi}$  are determined by  $\alpha$ ,  $\beta$ ,  $|P/T|$ , and  $\delta$ .

e.g.  $\alpha = (97^{+30}_{-21})^\circ$ ,  $\beta = 26^\circ$ ,

$$|P/T| = -.28, -\frac{\pi}{2} < \delta < +\frac{\pi}{2}$$

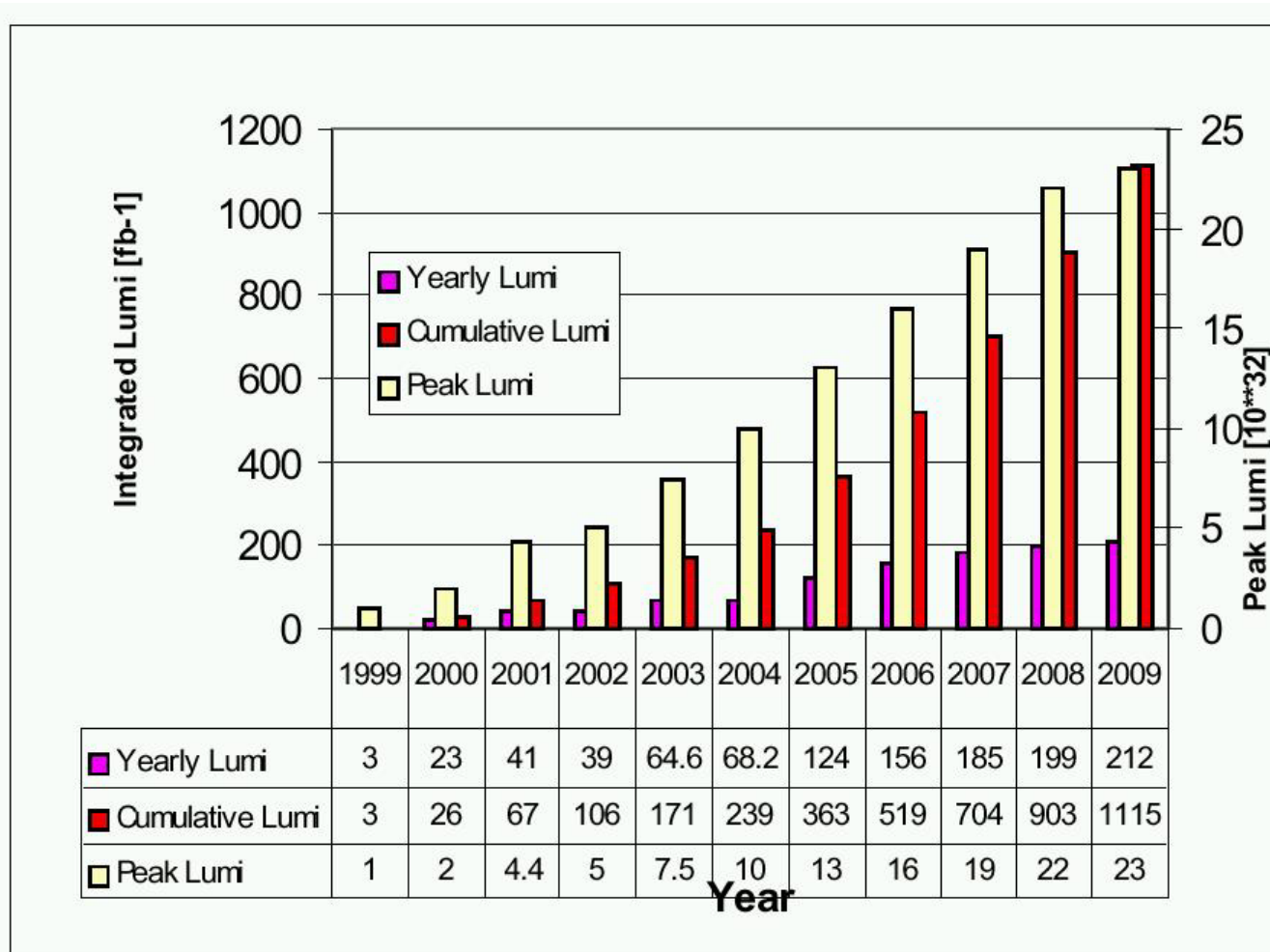
Consistent with SM expectations



# PEP-II Luminosity Projections

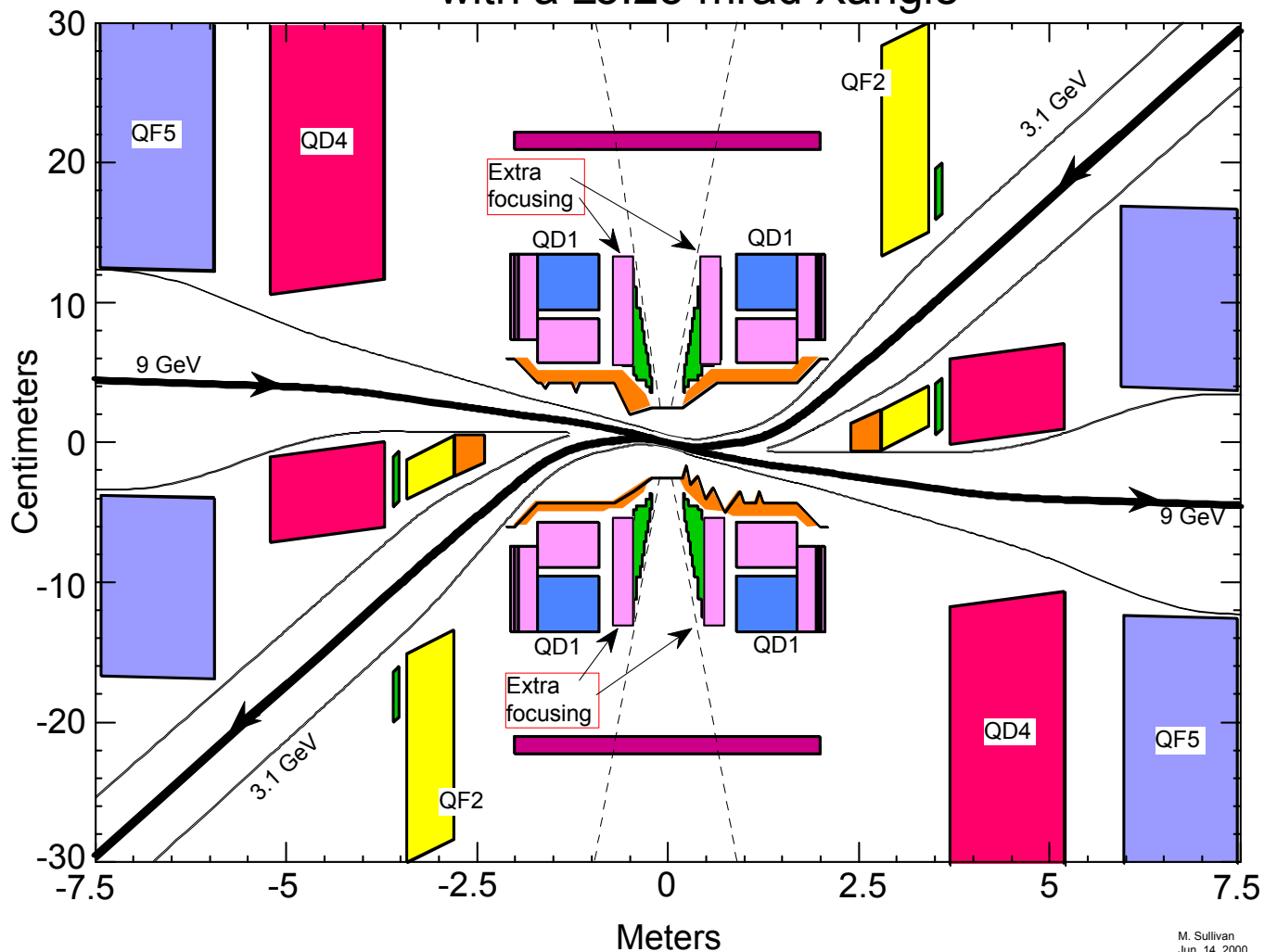


Equivalent expectation for Belle



# Possible PEP-II upgrade

Possible  $3 \times 10^{34}$  Interaction Region  
with a  $\pm 3.25$  mrad Xangle



# Projections for CP Asymmetry Measurements

Some rough estimates

Param.	Channel	$\sigma(\text{stat})/\sigma(\text{syst})$ 56 fb <sup>-1</sup>	$\sigma(\text{stat})/\sigma(\text{syst})$ 0.5 ab <sup>-1</sup>	$\sigma(\text{stat})/\sigma(\text{syst})$ 2.0 ab <sup>-1</sup>	$\sigma(\text{stat})/\sigma(\text{syst})$ 10 ab <sup>-1</sup>
$\sin 2\beta$	J/ $\psi$ K <sub>S</sub>	0.11 / 0.04	0.037 / 0.015	0.018 / 0.015	0.009 / 0.015
	Golden	0.09 / 0.04	0.030 / 0.015	0.015 / 0.015	0.007 / 0.015
	D*D*	0.45 / 0.06	0.15 / ?	0.08 / ?	0.034 / ?
$\sin 2\alpha_{\text{eff}}$	$\pi^+\pi^-$	0.37 / 0.07	0.12 / 0.03	0.06 / ?	0.03 / ?
$C_{\pi\pi}$		0.29 / 0.07	0.10 / 0.03	0.05 / ?	0.02 / ?

- o Expression of Interest at KEK for 10<sup>35</sup> machine in spring 2002
- o Ongoing workshops to examine this or higher luminosity options
- o Snowmass 2001 study of 10<sup>36</sup> concept and physics capability
  - Aim to be competitive and complementary to LHCb, BTeV on time scale of end of the decade
  - Physics case still being explored; still very early days in the exploration of these possibilities
  - Requires completely new vacuum and rf system, mostly new detector (current technologies cannot handle backgrounds)



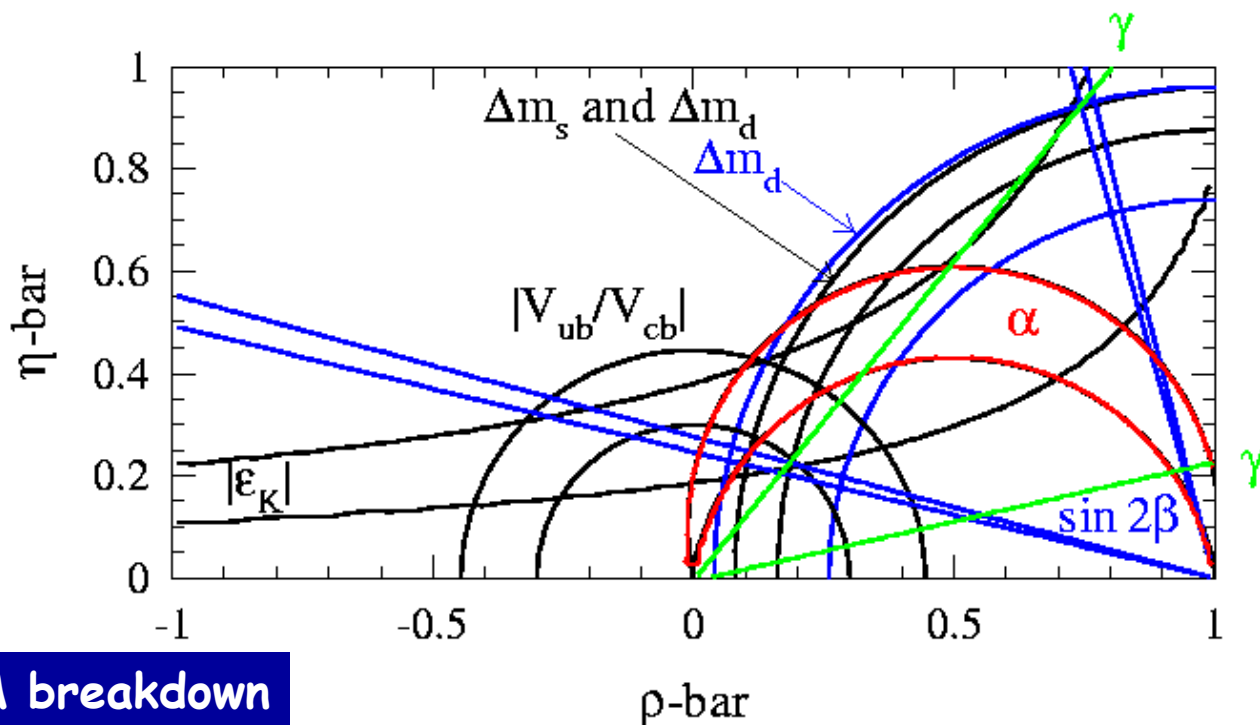
# Future Tests of the Standard Model

- Assumes  $|V_{cb}| \sim 3\%$  and  $|V_{ub}| \sim 10\%$ 
  - Much experimental and theoretical work underway to achieve this
    - New results on inclusive/exclusive semileptonic decays
    - Will be entering an era of very large tagged samples
- Assumes  $\Delta m_s$  known to  $<1\%$  from Tevatron in 2004?

ca. 2007:

$\sigma(\sin 2\beta) \sim 1\%$   
 $\alpha \sim 5^\circ, \gamma \sim 10^\circ$

**CKM**  
fitter



**Illustration of SM breakdown**



# Summary

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- *Now in the era of B Factories, with a renaissance of experimental and theoretical activity in B physics*
  - Data samples are 5 times larger than CLEO; will be 10 times larger within a few years

*Motivation for these and upcoming facilities is to provide a definitive test of CP violation in the Standard Model*

- *July 2001 saw the beginnings of this program*

*Unambiguous observation of CP violation in the B system*

$$\sin 2\beta = 0.734 \pm 0.055$$

**July 2002: Textbook plots!**

World average dominated by BELLE and BABAR

- *But...still working towards a definitive systematic test of Standard Model expectations and constraints*



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