

BELLE Time Dependent CP Asymmetries

1. Indirect CP violation in B decay
2. KEKB performance and the Belle detector
3. $\sin(2\phi_1)$ from $b \rightarrow c\bar{c}s$
 - Measuring the time dependence of decays
 - Flavour tagging CP eigenstates
 - CP event selection
4. Asymmetry in $B \rightarrow \pi^+\pi^-$ decays
5. Other emerging CP asymmetries
 - $B \rightarrow \eta'K_S^0$
 - $B \rightarrow K^+K^-K_S^0$
6. Summary



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The CKM Triangle

Unitary CKM matrix governs weak decay of quarks

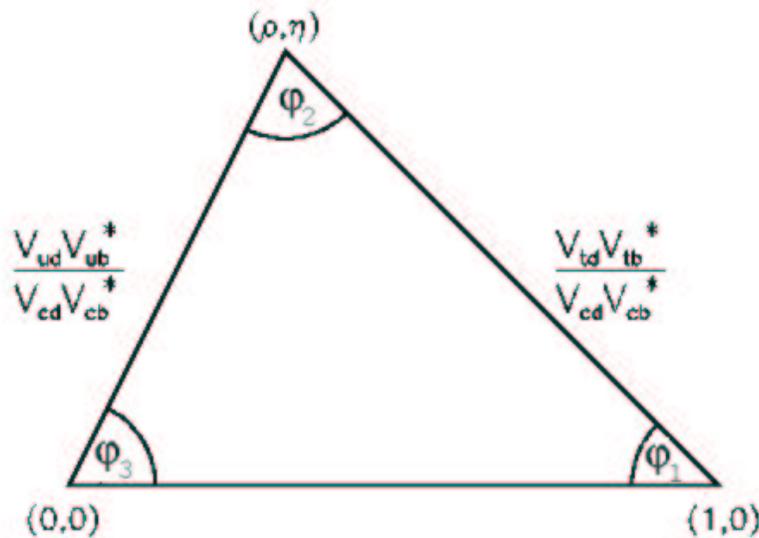
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Wolfenstein parametrisation:

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

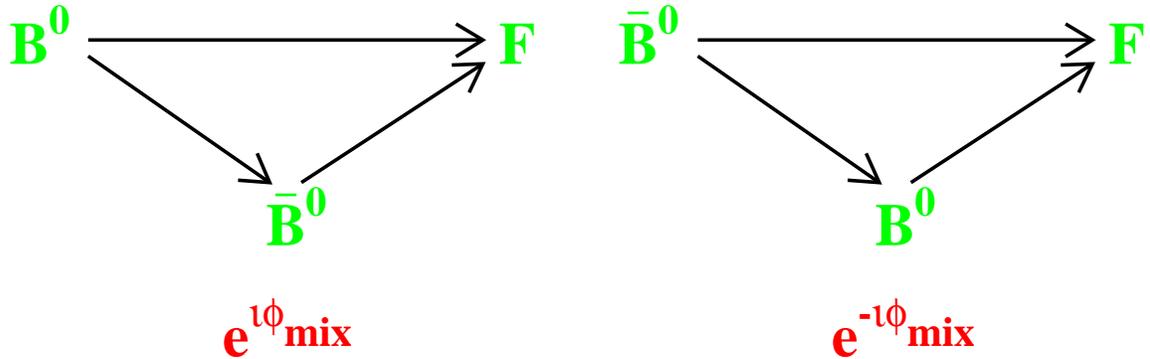
Unitarity $\rightarrow V^\dagger V = 1$ gives:

$$V_{tb}^* V_{td} + V_{cb}^* V_{cd} + V_{ub}^* V_{ud} = 0$$



$$\phi_2 = \arg\left(\frac{-V_{td} V_{tb}^*}{V_{ud} V_{ub}^*}\right) \quad \phi_1 = \arg\left(\frac{-V_{cd} V_{cb}^*}{V_{td} V_{tb}^*}\right) \quad \phi_3 = \arg\left(\frac{-V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}\right)$$

Indirect CP Asymmetry

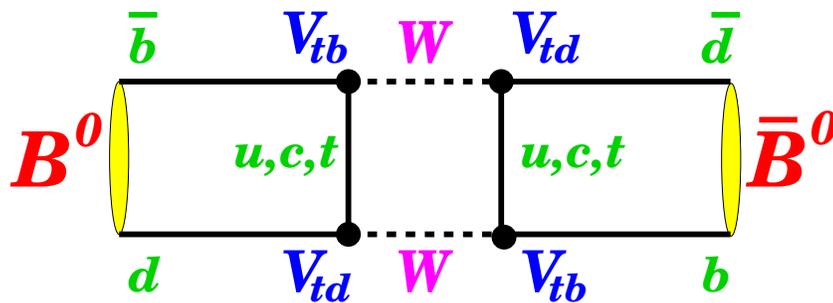


- If no direct CP violation then:

$$\frac{dN}{dt}(B^0 \rightarrow J/\psi K_\xi) \sim 1 + \xi_K \sin 2\phi_1 \sin \Delta m \Delta t$$

$$\frac{dN}{dt}(\bar{B}^0 \rightarrow J/\psi K_\xi) \sim 1 - \xi_K \sin 2\phi_1 \sin \Delta m \Delta t$$

- CP phase easily seen in CKM matrix element V_{td}



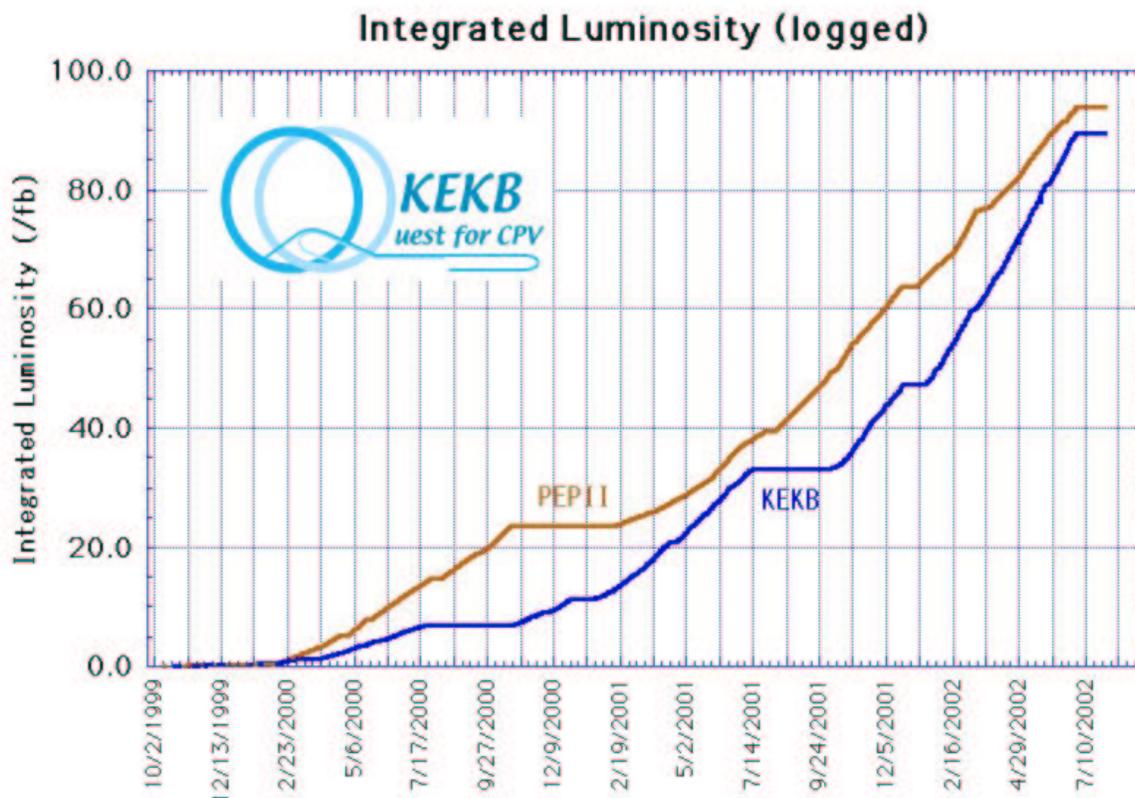
- B^0 and \bar{B}^0 produced at equal rates develop an asymmetry:

$$\begin{aligned}
 A_{CP}(\Delta t) &= \frac{\frac{dN}{dt}(\bar{B}^0 \rightarrow J/\psi K_\xi) - \frac{dN}{dt}(B^0 \rightarrow J/\psi K_\xi)}{\frac{dN}{dt}(\bar{B}^0 \rightarrow J/\psi K_\xi) + \frac{dN}{dt}(B^0 \rightarrow J/\psi K_\xi)} \\
 &= -\xi_K \sin 2\phi_1 \sin \Delta m \Delta t
 \end{aligned}$$

The KEK-B Collider

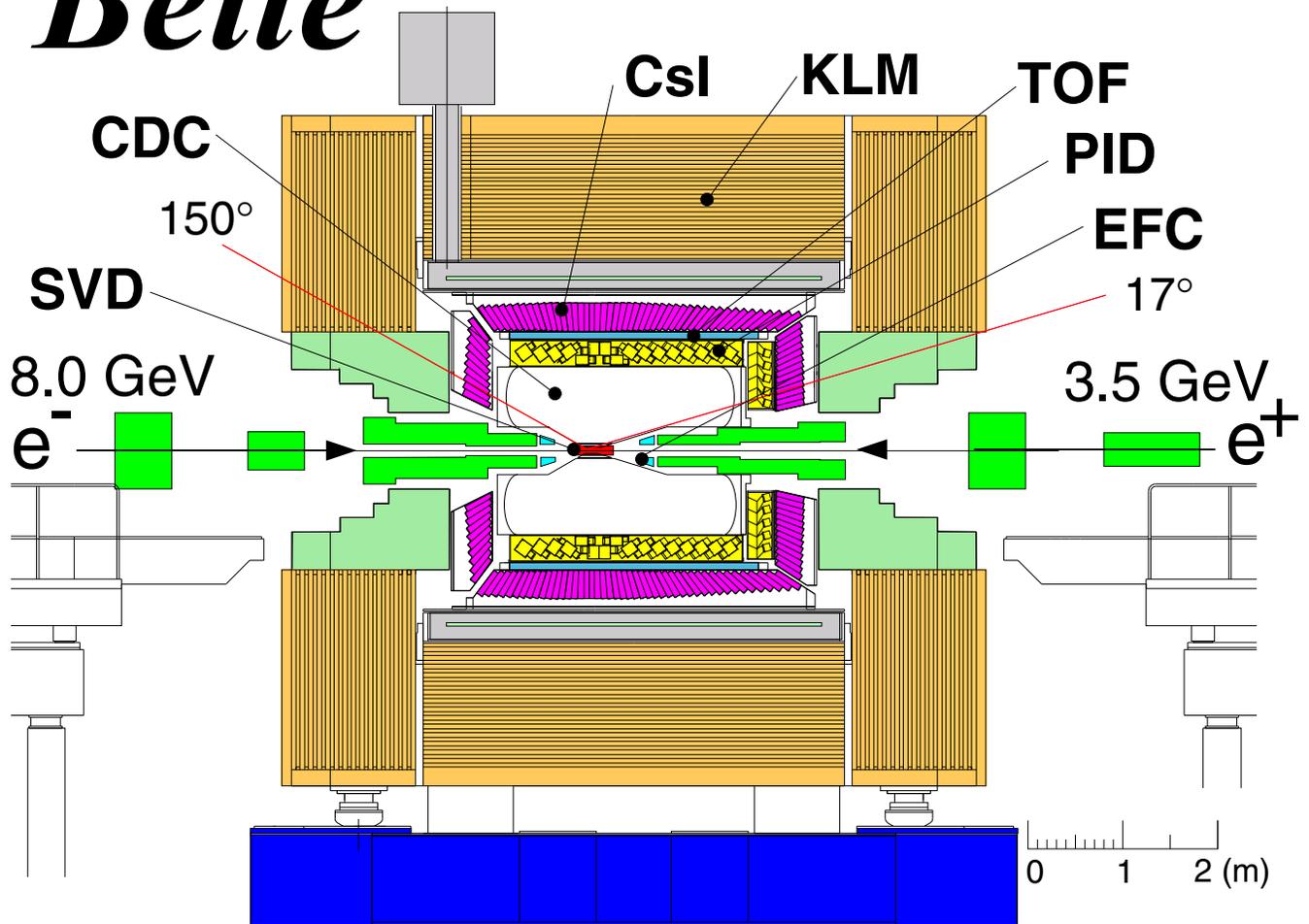
- 8.0 GeV electrons and 3.5 GeV positrons
 - $\sqrt{s} = 10.6$ GeV and $\beta\gamma = 0.425$
- 11 mrad crossing angle \rightarrow reduces backgrounds

\mathcal{L}	KEK-B	PEP-II
Peak ($\times 10^{33}$)	7.4	4.6
Record Day (pb^{-1})	399	303
Record Month (fb^{-1})	8.8	6.7
Total (fb^{-1})	90	94



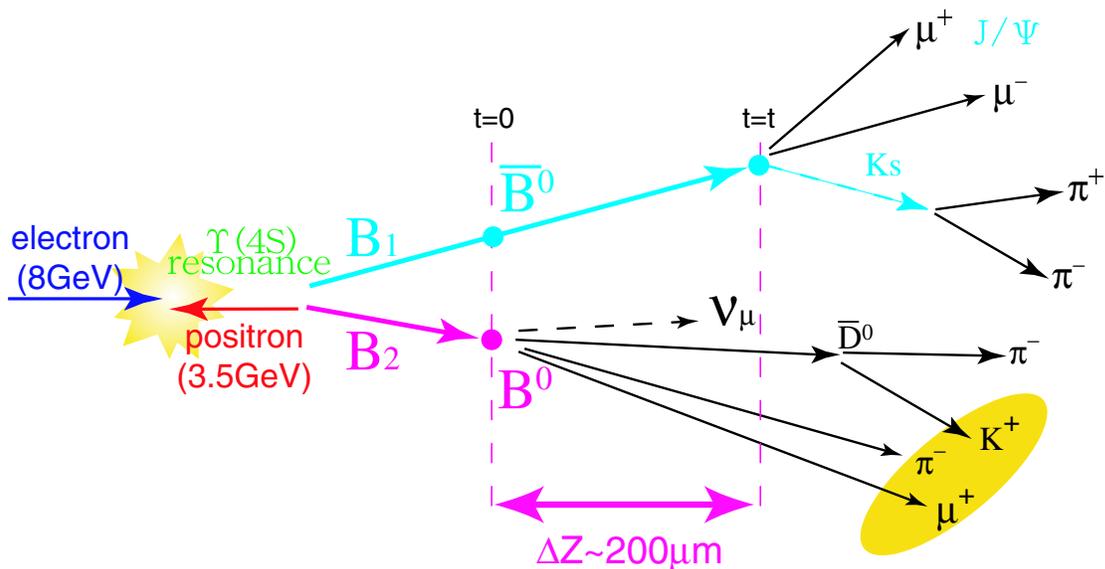
The BELLE Detector

Belle



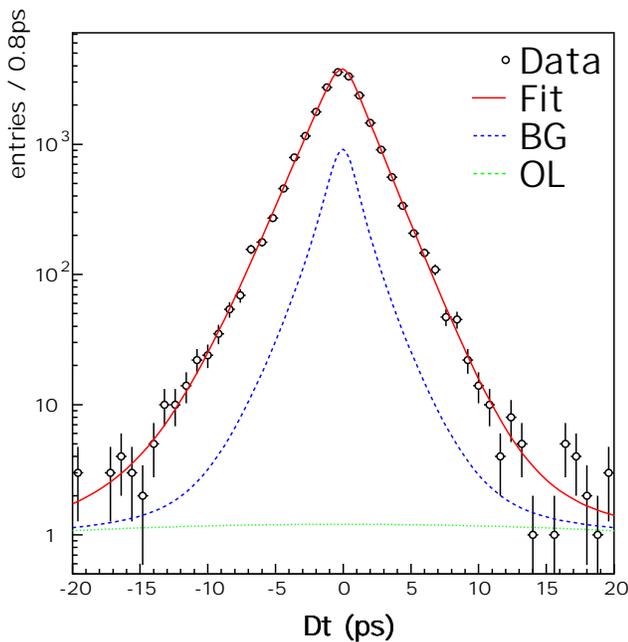
CP Violation Analysis Roadmap

1. Select $B^0 \rightarrow$ CP-eigenstate candidates ($J/\psi K_\xi$)
2. Find decay vertex and measure decay separation (Δt)
3. Tag flavour of "other B "
4. Fit time dependent flavour asymmetry

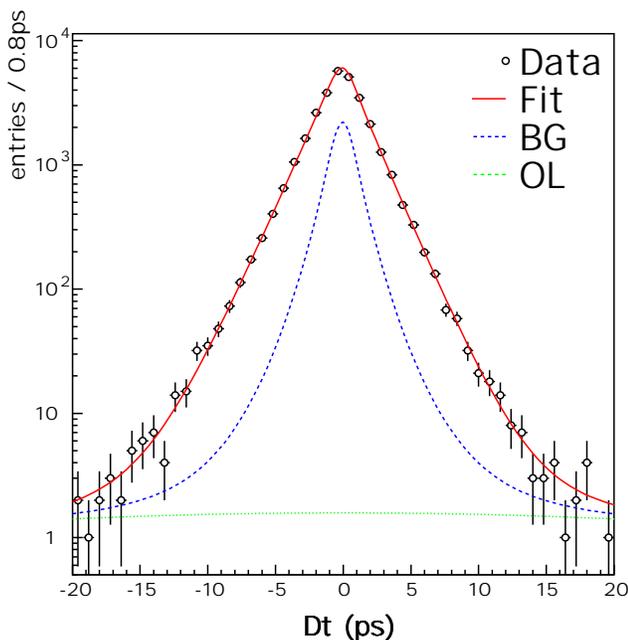


Measuring the Decay Vertices

- Measure the separation in decay vertex
 - Subtle since detector resolution $\approx B$ flight distance
- Parametrise resolution function carefully
 - CP side has $75\mu\text{m}$ rms resolution
 - Tagging side has $140\mu\text{m}$ rms resolution
- Resolutions well understood beyond 10 B lifetimes



$$\tau_{B\bar{0}} = 1.554 \pm 0.030 \pm 0.019 \text{ ps}$$



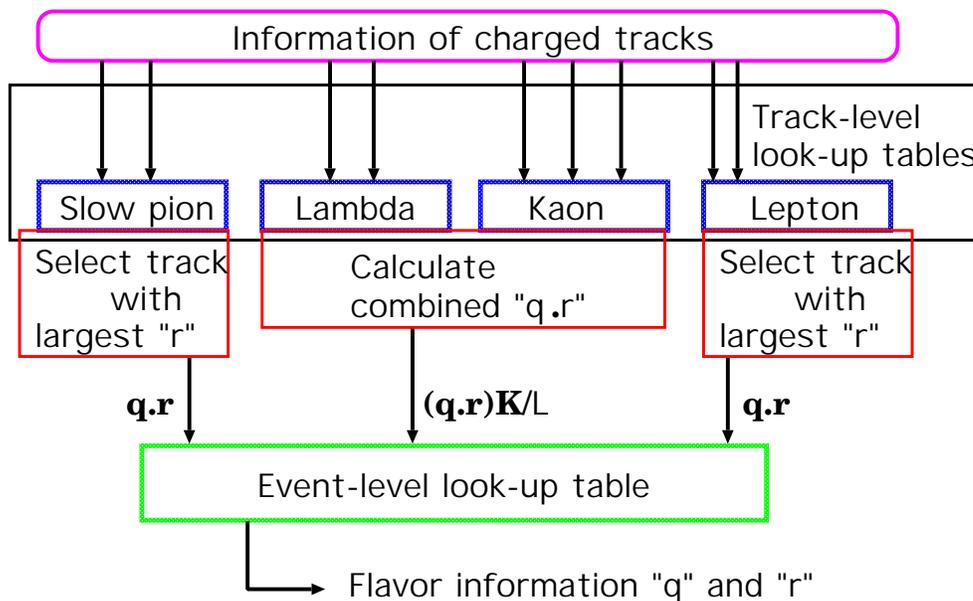
$$\tau_{B^-} = 1.695 \pm 0.026 \pm 0.015 \text{ ps}$$

$$\frac{\tau_{B^-}}{\tau_{B\bar{0}}} = 1.09 \pm 0.03$$

(PRL 88, 171801 (2002))

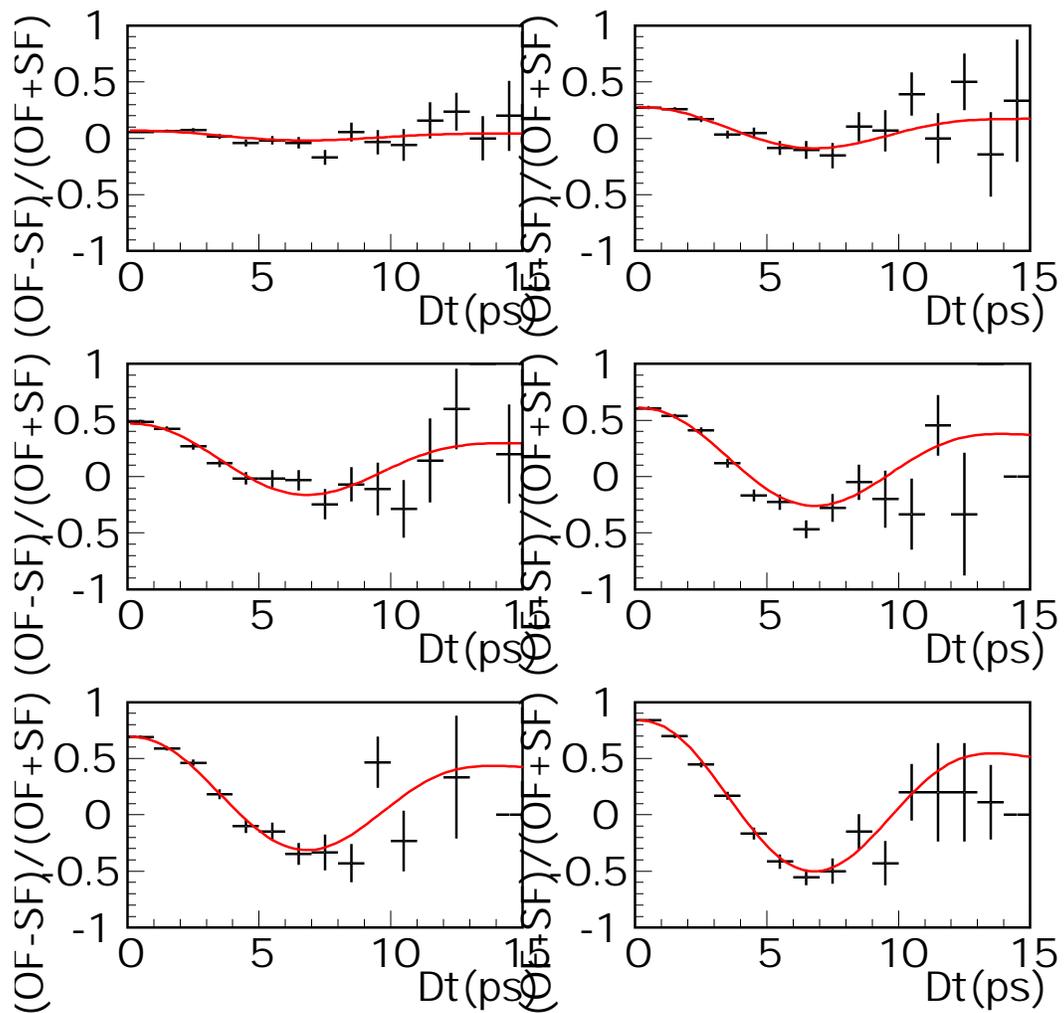
Flavour Tagging Method

- We look for time dependent asymmetry in CP eigenstate
- Must tag “other” B using a combination of:
 - high p_t leptons ($b \rightarrow cl\nu : l^-$)
 - lower p_t leptons ($b \rightarrow c \rightarrow sl\nu : l^+$)
 - Kaons ($b \rightarrow c \rightarrow sX : K^-$)
 - low momentum pions ($B \rightarrow D^* \rightarrow D\pi : \pi^-$)
 - and other information
- Apply tagging criteria to B^0 control samples



Flavour Tagging Calibration

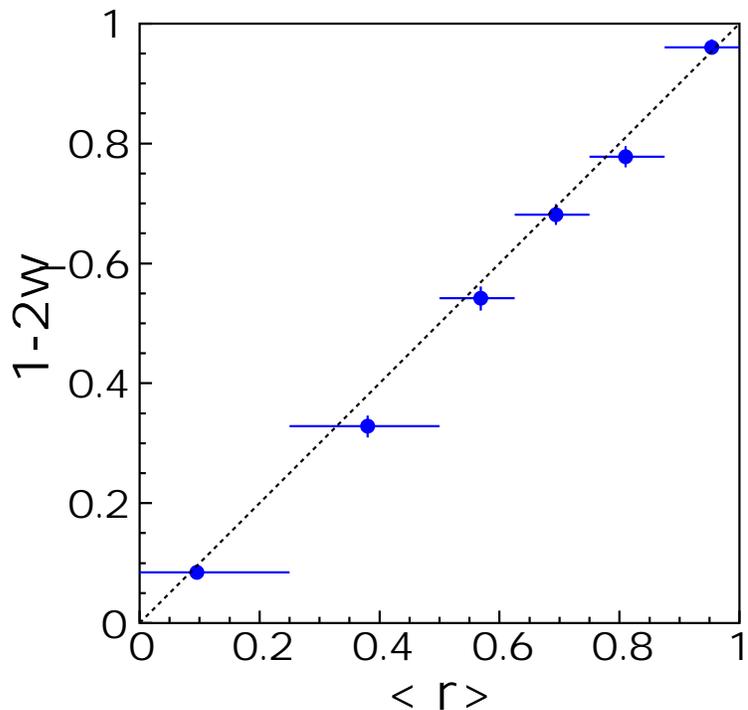
- Calibrate effectiveness on control data samples
- Measure $B^0\bar{B}^0$ (using $D^*l\nu$ sample) mixing in 6 intervals of τ



- Amplitude measures wrong tag fractions (w_r)

Flavour Tagging Quality

- $1-2w_r$ gives the correct tag probability

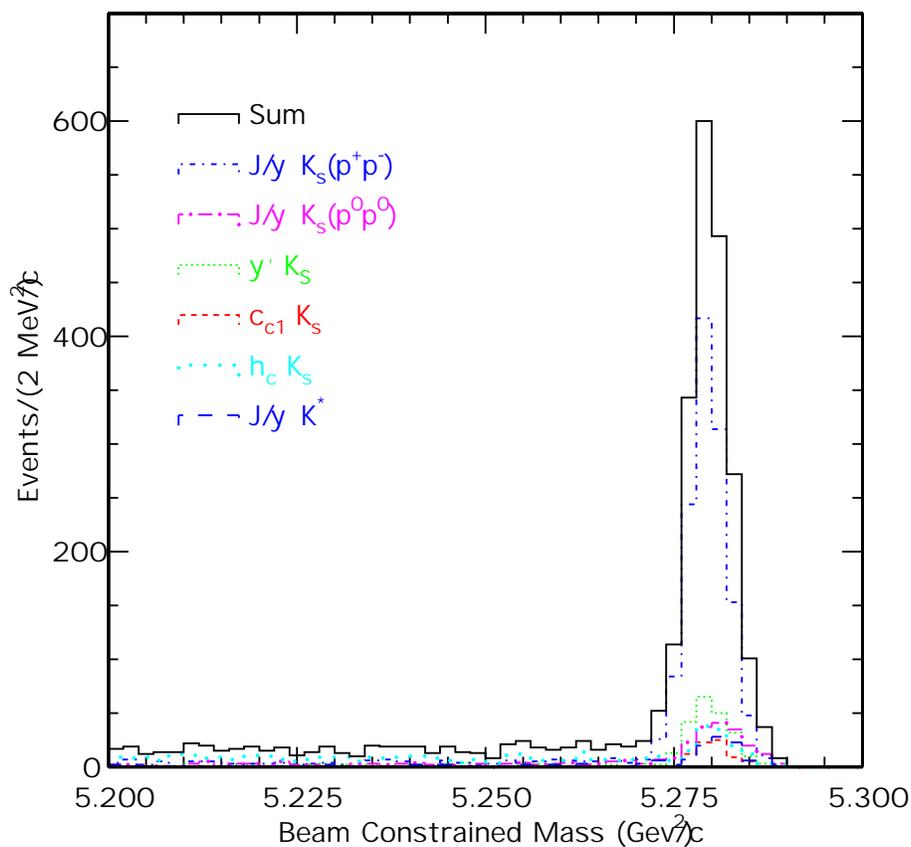


- These are measured from data control samples
- Extract flavour information from 99.5% of candidates
- No tagging bias observed
- Effectively tag 28.8 ± 0.6 % of B^0 decays
 - Improved from $27.0 \pm 1.2\%$ in prior analyses
 - This comes from
 - * improved low momentum tracking
 - * improved silicon alignment

Belle's $c\bar{c}s$ Event Sample

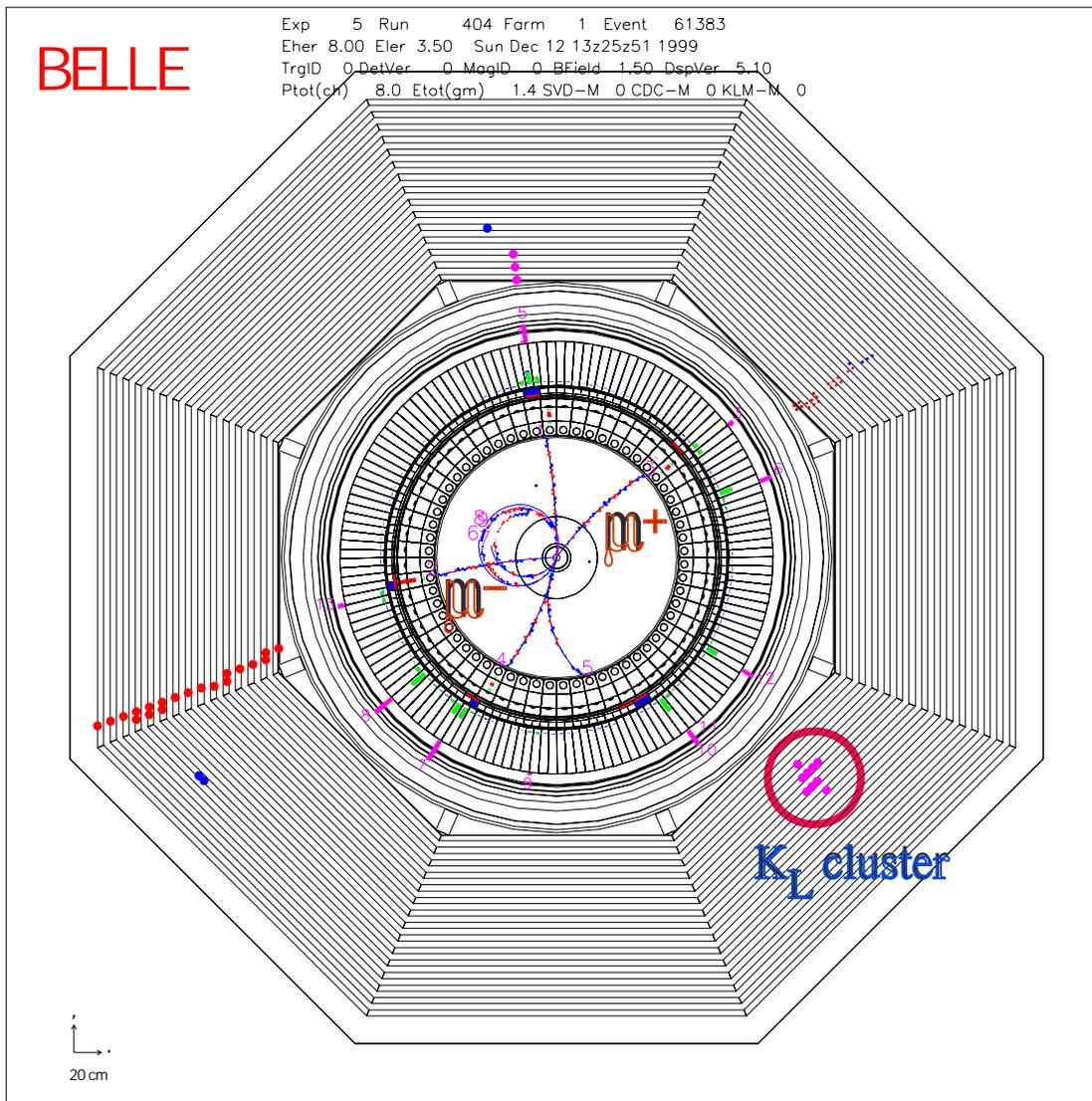
- Sample from $78fb^{-1}$ of $\Upsilon(4S)$ resonance data

Mode	CP (ξ_K)	Candidates	Purity (%)
$J/\psi K_S^0(\pi^+\pi^-)$	-1	1116	98
$J/\psi K_S^0(\pi^0\pi^0)$	-1	162	82
$\psi(2S)K_S^0$	-1	172	93
$\chi_{c1}K_S^0$	-1	67	96
$\eta_c K_S^0$	-1	122	68
$J/\psi K^{*0}(K_S^0\pi^0)$	1(81%)	89	92
$J/\psi K_L^0$	1	1230	63
Total		2958	



Using $J/\psi K_L^0$ Candidates

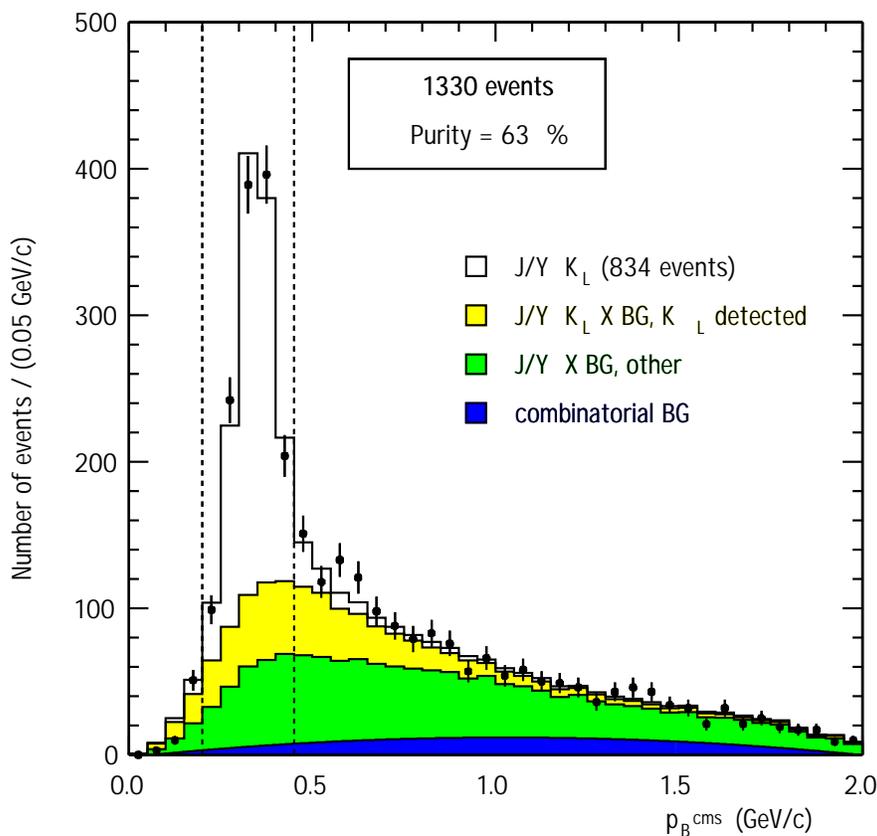
- Less information from detector to reconstruct K_L^0 candidates



- Muons leave continuous tracks in KL/muon detector
- K_L^0 leave a hadronic shower (cluster of hits)
- Only measure K_L^0 direction, not its energy/momentum

Identifying K_L^0 Candidates

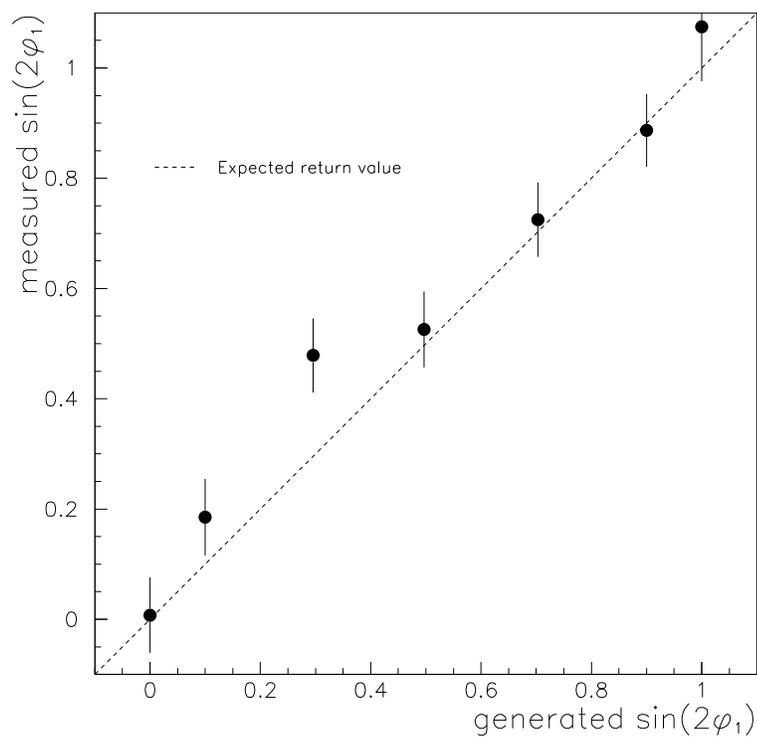
- Constrain K_L^0 momentum to give B mass. Know:
 - $\vec{p}_B^* = \vec{p}_{J/\psi}^* + \vec{p}_{K_L^0}^*$
 - $E_{J/\psi}^* + E_{K_L^0}^* = \frac{1}{2}m_\gamma$
 - Given $\hat{p}_{K_L^0}$ this gives a unique $|\vec{p}_{K_L^0}^*|$
- Look for signal (peak near 330 MeV/c²) in p_B^* distribution



- Veto all other $J/\psi X$ candidates found
- B decay backgrounds (K_L^0 detected, No K_L^0 detected)
- Select 1330 events ($0.2 \leq p_B^* \leq 0.45$ GeV/c) with 63% purity

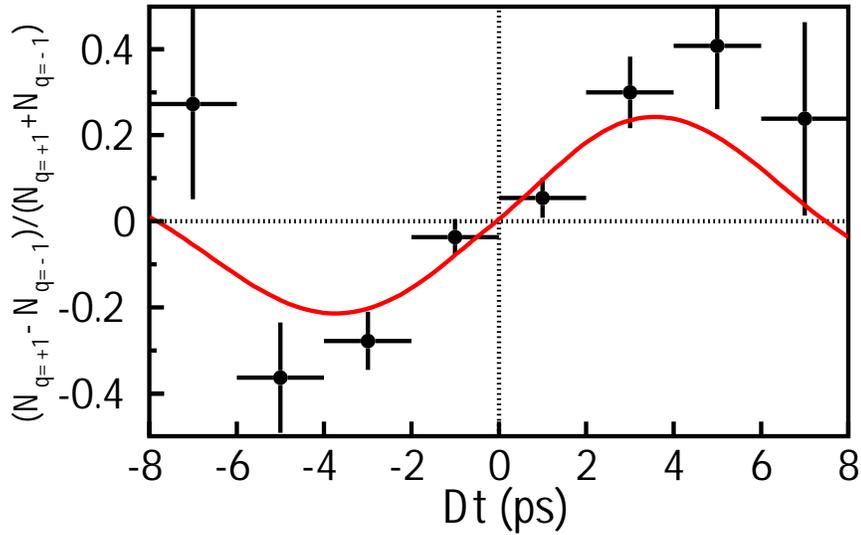
Cross-check $J/\psi K_L^0$ Background Treatment

- Eight charmonium background classes according to CP
- Predict CP asymmetry from *EVTGEN* simulation
- Fit includes these asymmetries
- Test validity of these corrections

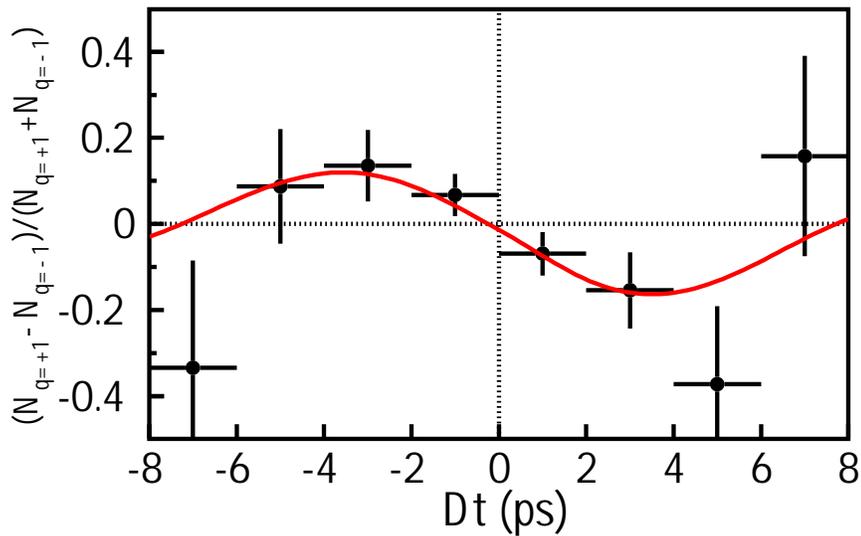


- Variations included in background systematic

CP fit Comparison ($c\bar{c}K_S^0$ vs. $J/\psi K_L^0$)



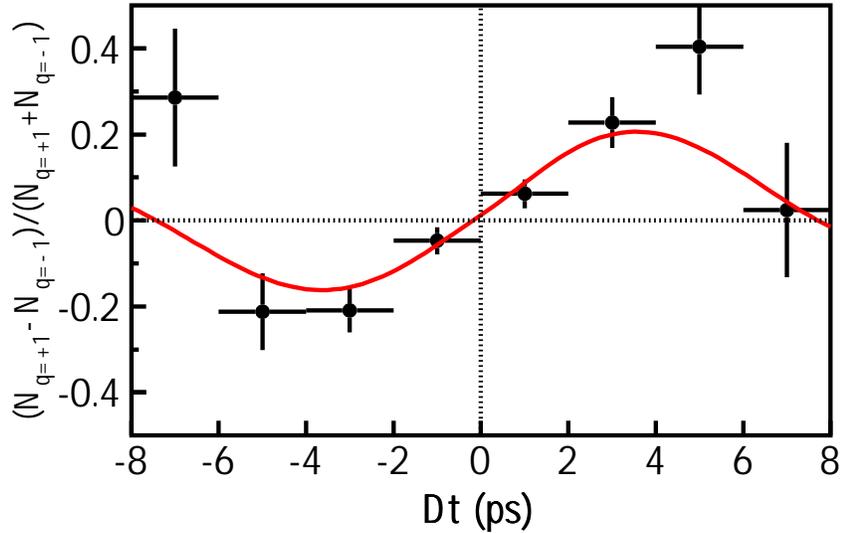
$$\sin 2\phi_1 = 0.716 \pm 0.083(\text{stat})$$



$$\sin 2\phi_1 = 0.781 \pm 0.167(\text{stat})$$

Combined Fit for $\sin 2\phi_1$

Preliminary result from $78fb^{-1}$



$$\sin 2\phi_1 = 0.719 \pm 0.074(\text{stat}) \pm 0.035(\text{sys})$$

Uncertainty Source	Value
Vertexing Reconstruction	0.022
Flavour Tagging	0.015
Vertex Resolution	0.014
Fit parametrisation	0.011
$J/\psi K_L^0$ Background	0.010
$\Delta m_d, \tau_B$	≤ 0.010
Total	0.035

Cross checks for $c\bar{c}s$ Asymmetry

- We test for direct CP-violation by generalising:

$$A_{CP}(\Delta t) = \frac{-\xi_K 2\text{Im}\lambda}{|\lambda|^2+1} \sin(\Delta m \Delta t) + \frac{|\lambda|^2-1}{|\lambda|^2+1} \cos(\Delta m \Delta t)$$

- we find:

$$|\lambda| = 0.950 \pm 0.049(\text{stat}) \pm 0.025(\text{sys})$$

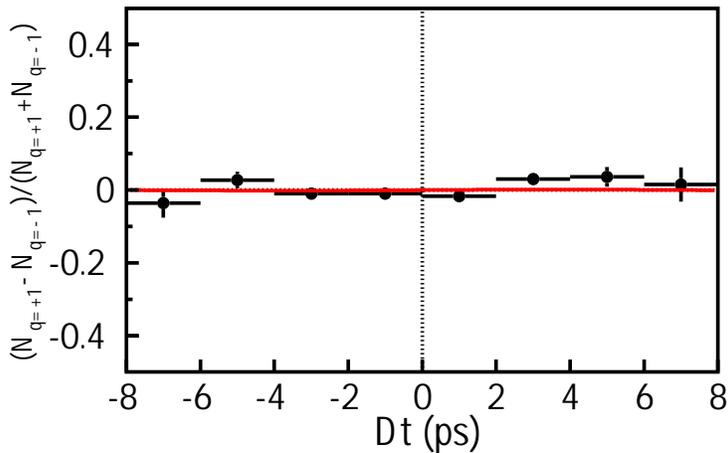
$$-2 \xi_K \text{Im}\lambda/|\lambda| \equiv \sin(2\phi_1) = 0.720 \pm 0.074(\text{stat})$$

- We see no evidence for direct CP violation in these decays
- Other cross-checks

Subsample (stat error only)	
$J/\psi K_S^0(\pi^+\pi^-)$	0.73 ± 0.10
$(c\bar{c})K_S^0$ (except $J/\psi K_S^0(\pi^+\pi^-)$)	0.67 ± 0.17
$J/\psi K_L^0$	0.78 ± 0.17
$f_{tag} = B^0$	0.65 ± 0.12
$f_{tag} = \bar{B}^0$	0.77 ± 0.09
$r \leq 0.5$	1.26 ± 0.36
$0.5 \leq r \leq 0.75$	0.62 ± 0.15
$0.75 \leq r$	0.72 ± 0.09
All	0.72 ± 0.07

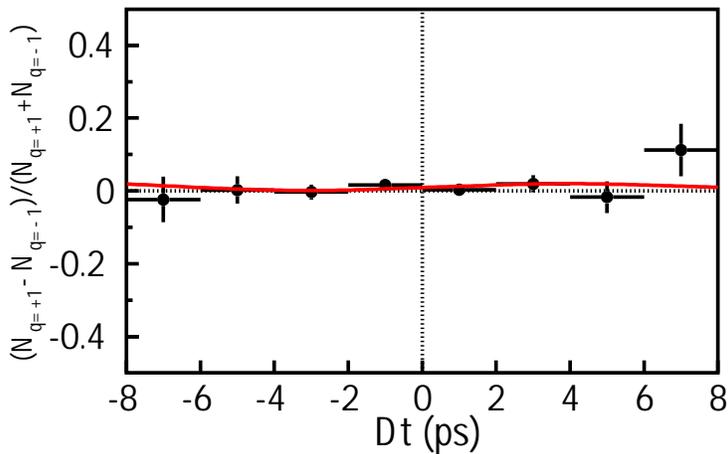
Fits to Control Samples

- Non-CP eigenstates should not exhibit asymmetry

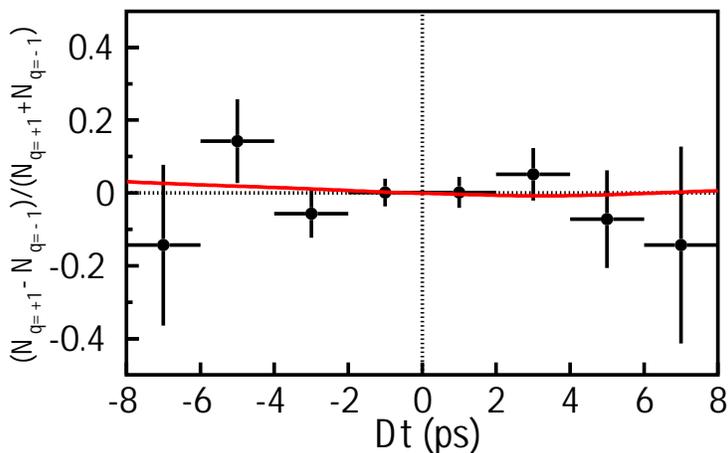


"sin $2\phi_1$ "

$D^*l\nu :$
 -0.004 ± 0.017

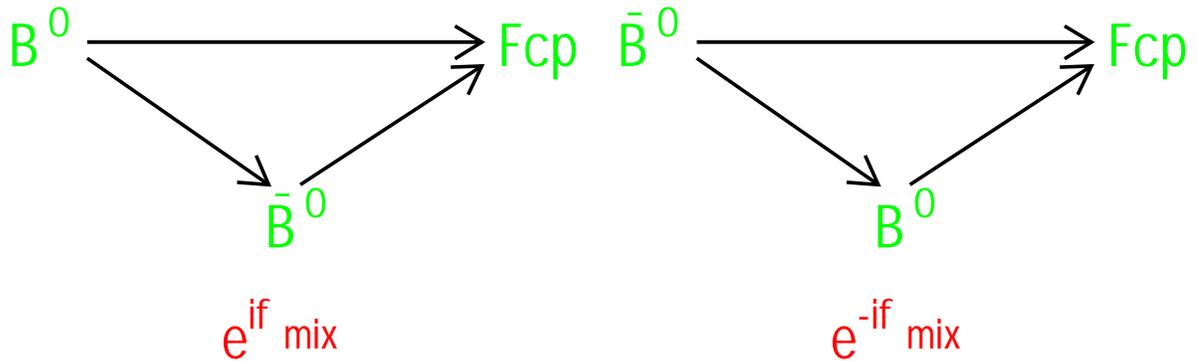


$D^{(*)}(\pi, \rho) :$
 0.035 ± 0.032



$J/\psi K^*(K^+\pi^-) :$
 -0.021 ± 0.093

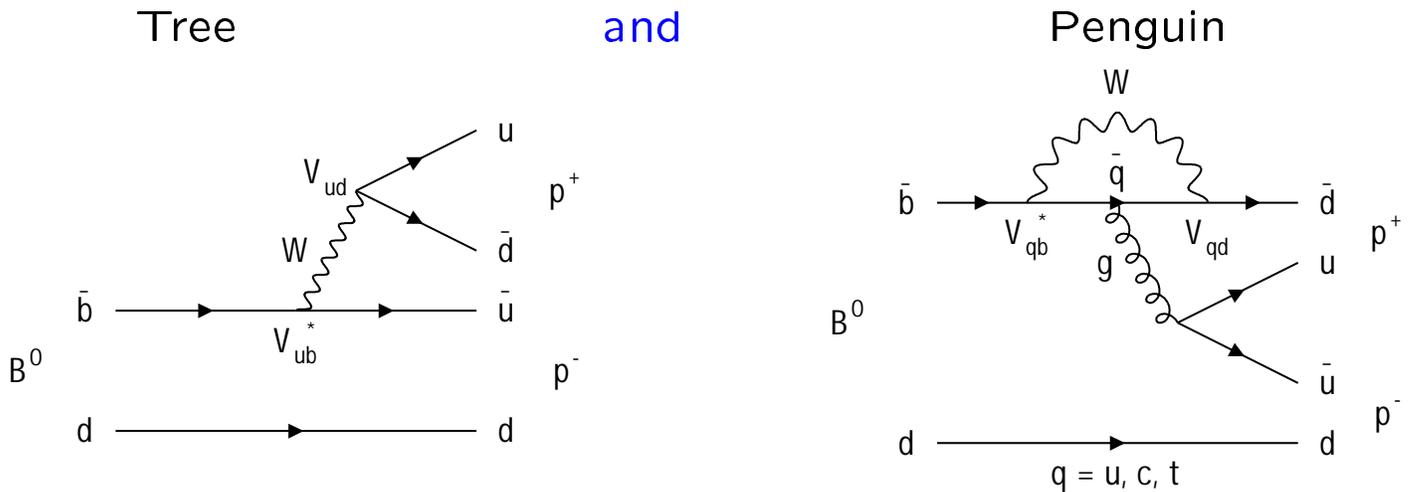
Direct and Indirect CP Asymmetry



- More than one path for $B^0 \rightarrow F_{CP}$ direct CP violation possible:

$$\begin{aligned}
 A_{CP}(\Delta t) &= \frac{\frac{dN}{dt}(\bar{B}^0 \rightarrow F_{CP}) - \frac{dN}{dt}(B^0 \rightarrow F_{CP})}{\frac{dN}{dt}(\bar{B}^0 \rightarrow F_{CP}) + \frac{dN}{dt}(B^0 \rightarrow F_{CP})} \\
 &= S_F \sin \Delta m \Delta t + A_F \cos \Delta m \Delta t
 \end{aligned}$$

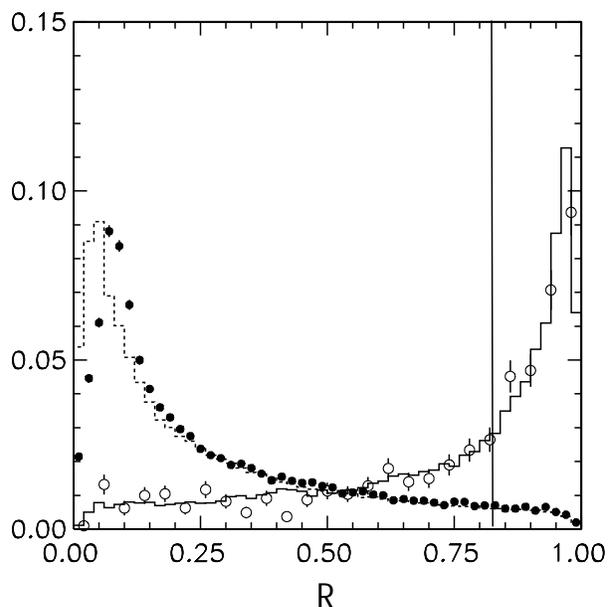
- $B^0 \rightarrow \pi^+ \pi^-$ final states have contributions from:



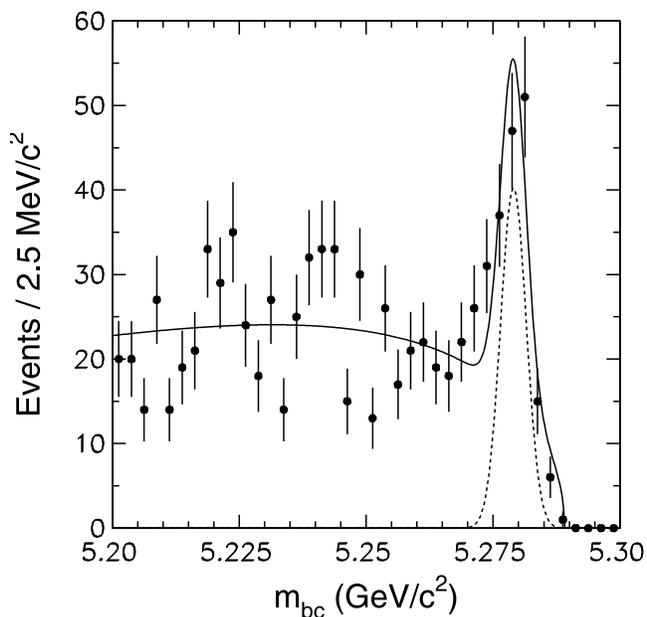
- In general this leads to
 - $S_{\pi\pi} = \sin(2\phi_2 + \theta) \neq \sin(2\phi_2)$
 - Direct CP violation: $A_{\pi\pi}$ different from 0

Selection of $B^0 \rightarrow h^+h^-$

- Select pairs of oppositely charged high momentum tracks
- Reject leptons, select π with particle ID
- Suppress continuum background with
 - Fox-Wolfram moments, “ B^0 ” direction



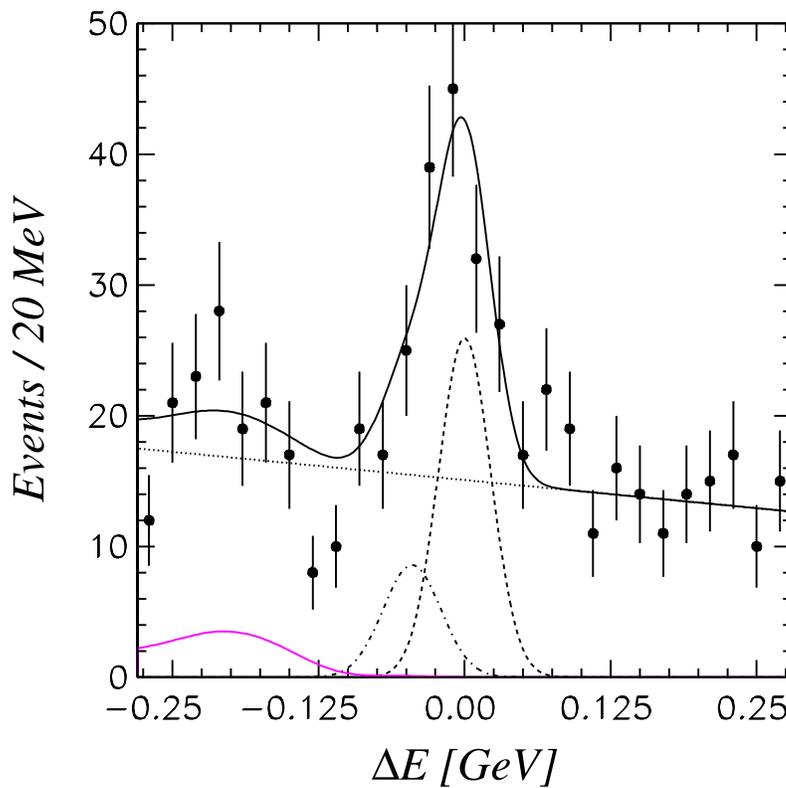
- Require $M_{bc} = \sqrt{(E_{cm}/2)^2 - (\vec{p}_{h^+} + \vec{p}_{h^-})^2}$ above $5.2 \text{ GeV}/c^2$



- $\pi^+\pi^-$ not distinguished from $K^+\pi^-$ in M_{bc}

Final Selection of $B^0 \rightarrow \pi^+\pi^-$

- $K^+\pi^-$ can be distinguished by
 - $\Delta E = E_{h^+} + E_{h^-} - E_{\text{cm}}/2$
 - Assume pion mass for both tracks \Rightarrow
 - * $K^+\pi^-$ shifted (down) by 45 MeV in ΔE

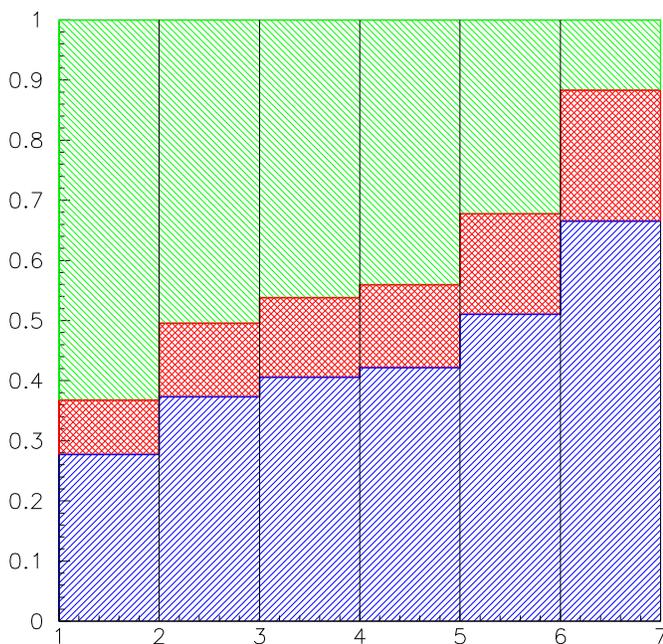


- Signal region: $5.271 \leq M_{\text{bc}} \leq 5.287 \text{ GeV}/c^2$
- In $|\Delta E| \leq 0.067 \text{ GeV}$
 - $N_{\pi^+\pi^-} = 74 \pm 14$ signal
 - $N_{K^+\pi^-} = 28 \pm 12$ feed-across background
 - $N_{q\bar{q}} = 99$ continuum background (total constrained)

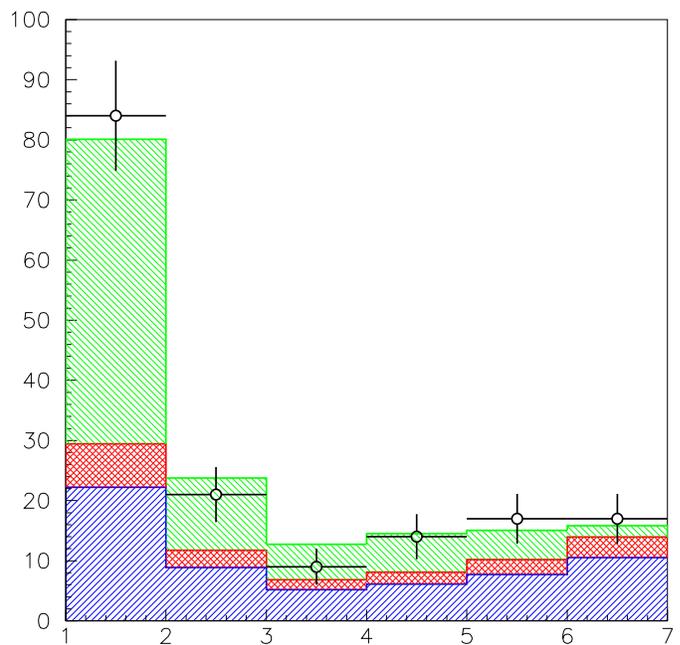
Asymmetry Fit for $B^0 \rightarrow \pi^+\pi^-$

- Flavour-tag B^0 and measure Δt as for $J/\psi K_S^0$
- Events weighted in fit depending on
 - Continuum rejection likelihood
 - tag reliability, r
 - decay time difference, Δt
 - ΔE

Event Fractions



Yields

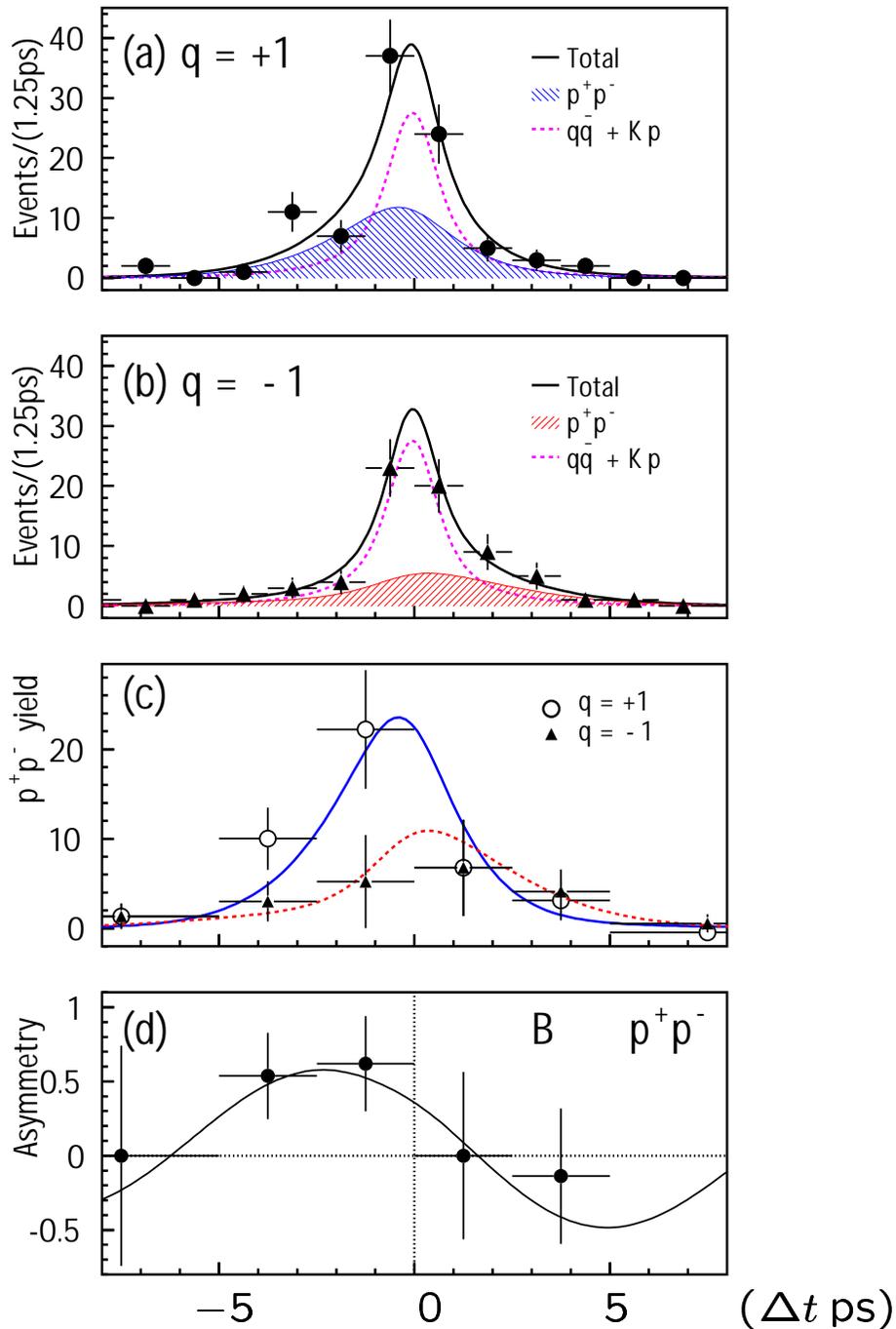


- $\pi^+\pi^-$ signal, • $K^+\pi^-$ background, • $q\bar{q}$ background

- Consciously select a clean $\pi^+\pi^-$ sample

CP Asymmetry in $\pi^+\pi^-$

PRL 89, 071801 (2002).



- Event-by-event likelihood fit gives

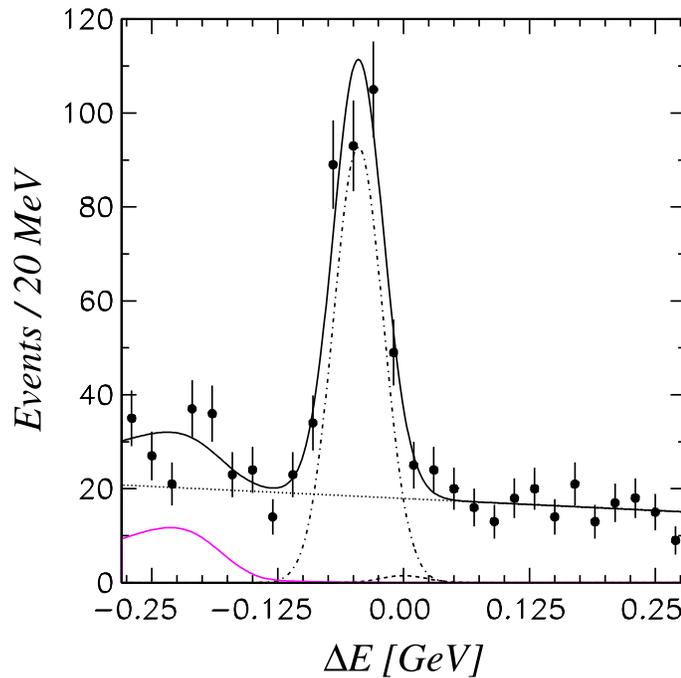
$$S_{\pi\pi} = -1.21^{+0.38}_{-0.27}(\text{stat})^{+0.16}_{-0.13}(\text{sys})$$

$$A_{\pi\pi} = 0.94^{+0.25}_{-0.31}(\text{stat}) \pm 0.09(\text{sys})$$

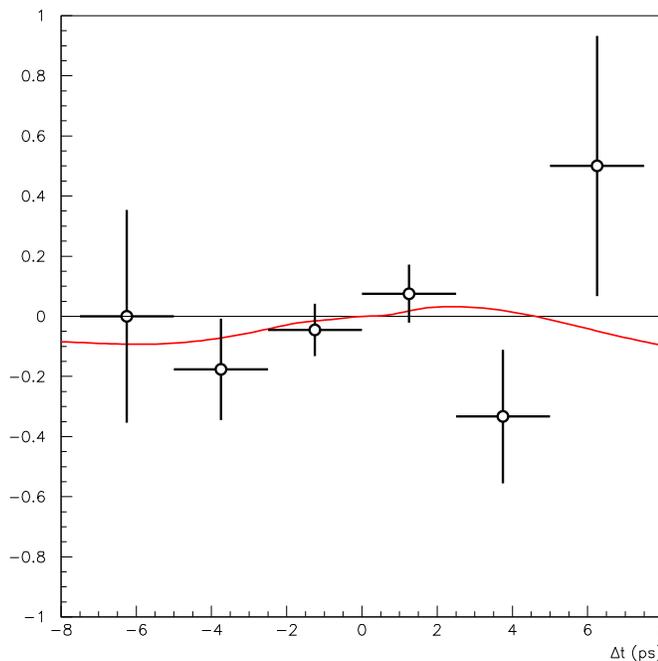
- Evidence for direct CP and large $\sin(2\phi_2)$

Cross-checks with $K^+\pi^-$ Sample

- Invert particle ID to enhance $K\pi$ fraction (290 ± 22 candidates)



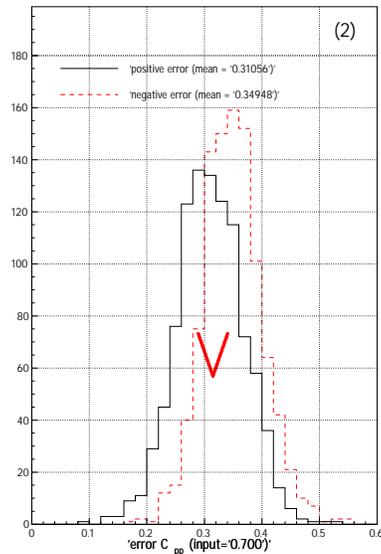
- Extract asymmetries from this sample



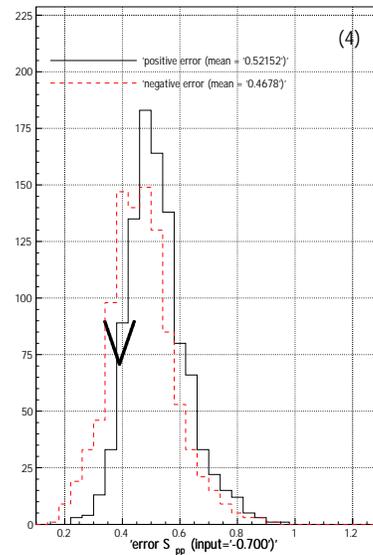
- Fit yields:
 - " $S_{K\pi}$ " = 0.15 ± 0.24 " $A_{K\pi}$ " = 0.07 ± 0.17

Statistical Cross-checks

- It has been noticed:
 - Has “smallish” uncertainties given our statistics

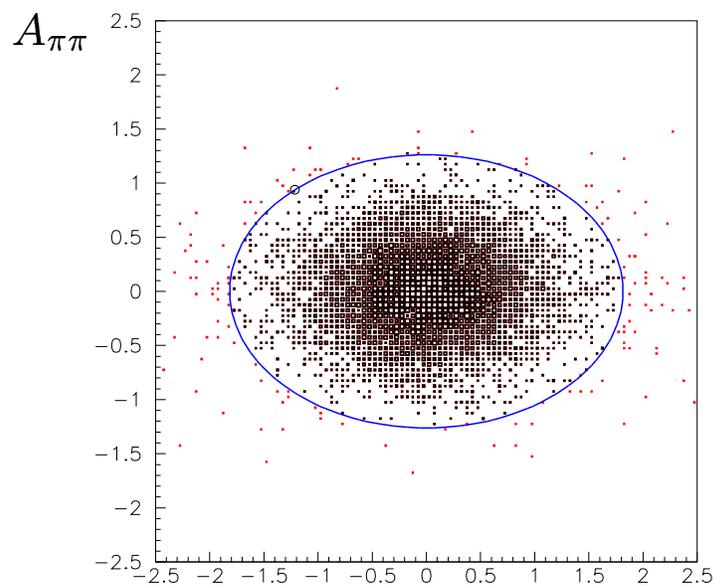


$\delta A_{\pi\pi}$



$\delta S_{\pi\pi}$

- * 5% chance to get $\delta S_{\pi\pi}$ smaller than our fit
- $S_{\pi\pi}$ and $A_{\pi\pi}$ are 2.9 standard deviations from 0
- * An ensemble test shows

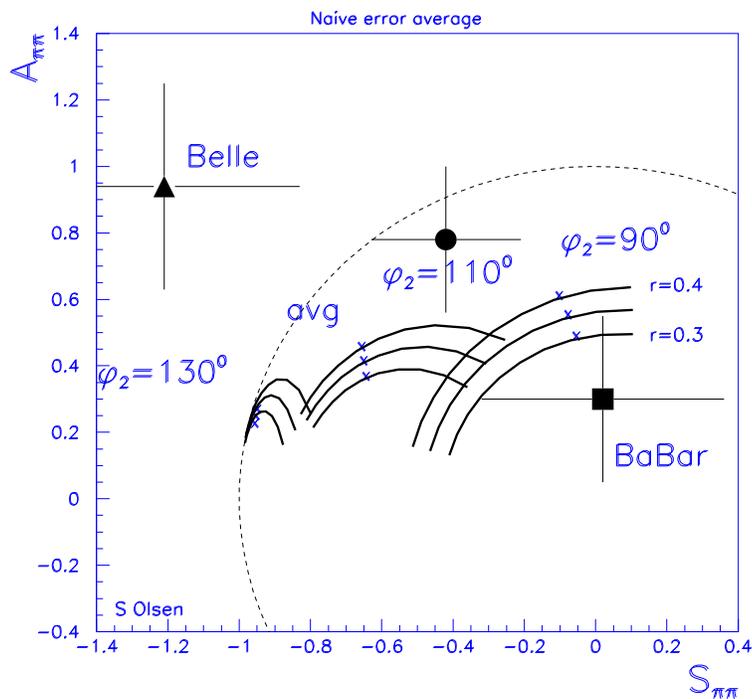


$S_{\pi\pi}$

- 1.6% lie further away from (0,0) than our result

What might this be telling us?

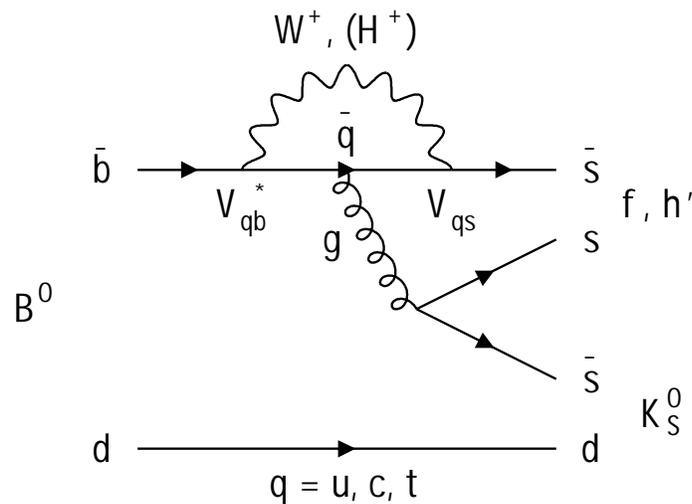
- We have found no problems with our analysis
- BaBar's result is inconsistent with ours by 2σ
- At face value it hints at two large asymmetries
- Gronau and Rosner (hep-ph/0202170) relate:
 - $S_{\pi\pi} \propto \sin(2\phi_2) + 2r \sin(\phi_1 - \phi_2) \cos \delta - r^2 \sin(2\phi_1)$
 - $A_{\pi\pi} \propto 2r \sin(\phi_1 + \phi_2) \sin \delta$
 - r is ratio of penguin to tree amplitudes (0.3 preferred?),
 - δ is the difference of strong phases



- Extraction of ϕ_2 simplified if asymmetry large

CP Asymmetries in Other Modes

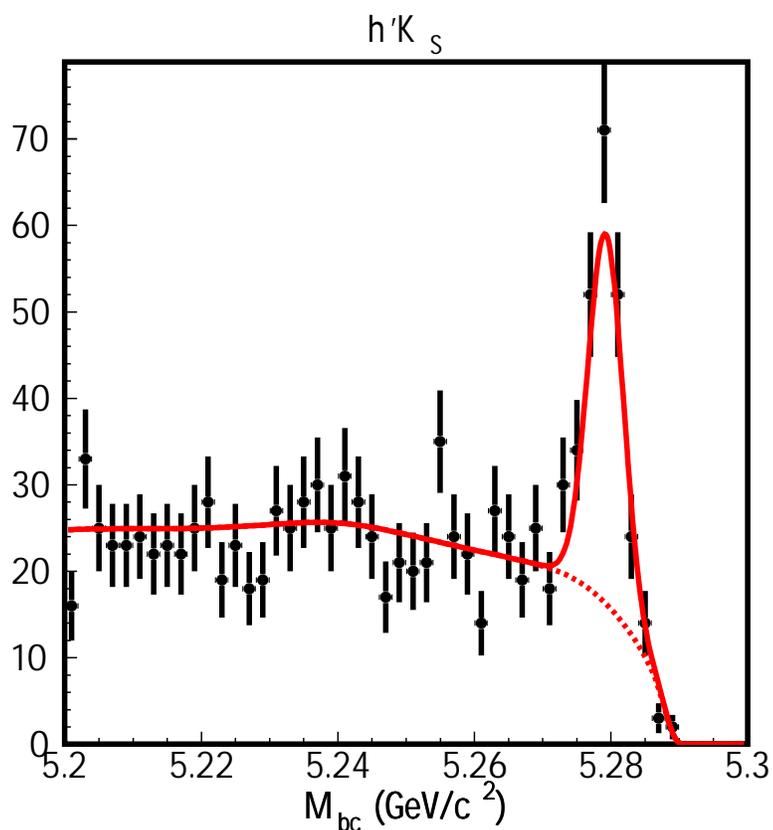
- In the Standard Model $B^0 \rightarrow \phi K_S^0$ very similar to $J/\psi K_S^0$



- However $\mathcal{B}(B^0 \rightarrow \eta' K_S^0)$ at 5×10^{-5} is
 - o bigger than the un-seen ηK mode
 - o not easy to explain theoretically
 - o may hint at new physics in penguin loop
- New physics \Rightarrow possible new phases
 - o $S_{SSS} = \sin(2\phi_1 + \Theta_{\text{New Physics}})$?

Selection of $B^0 \rightarrow \eta' K_S^0$

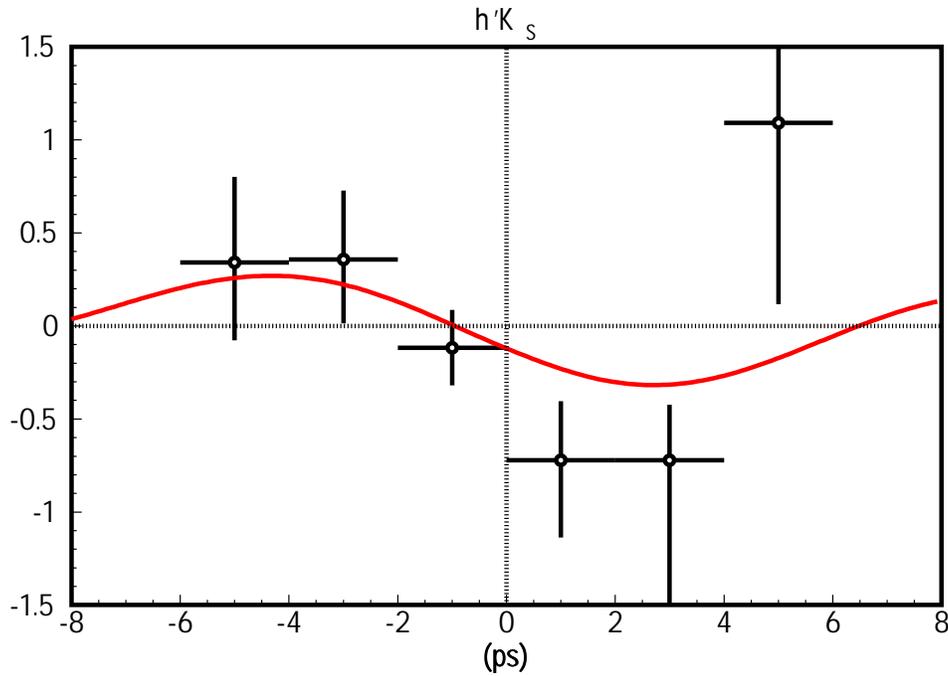
- Result from 42 fb^{-1} accepted by PLB (hep-ex 0207033)
- Select η' in two modes:
 - $\eta' \rightarrow \eta \pi^+ \pi^-$ ($\eta \rightarrow \gamma \gamma$)
 - $\eta' \rightarrow \rho^0 \gamma$
- Add a K_S^0 and look for signal in M_{bc} and ΔE



- 128 ± 14 candidates (background of 105) for CP fit

CP Asymmetry in $B^0 \rightarrow \eta' K_S^0$

- Flavour tag and measure Δt as for other modes



- Fit gives

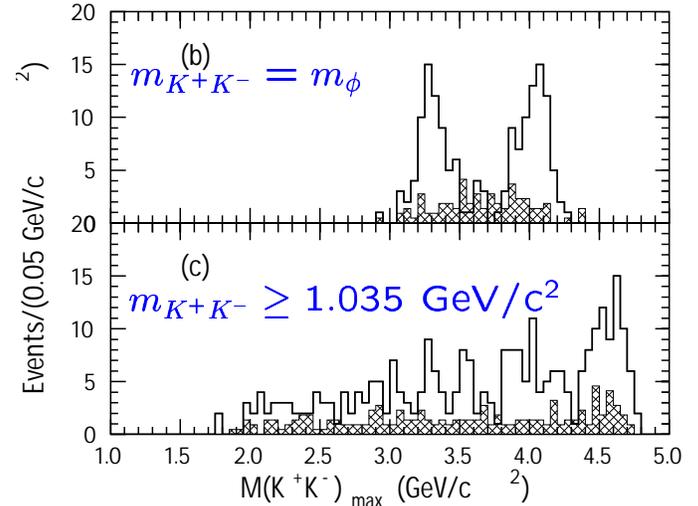
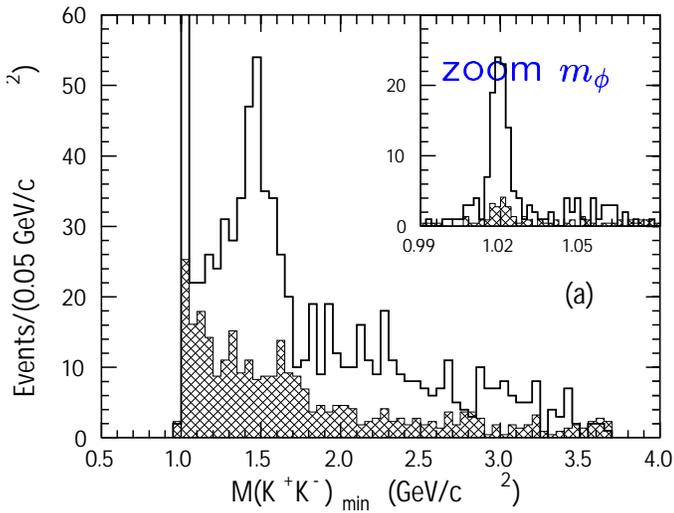
- $S_{\eta'K_S^0} = 0.76 \pm 0.36(\text{stat}) \pm 0.06(\text{sys})$

- $A_{\eta'K_S^0} = 0.26 \pm 0.22(\text{stat}) \pm 0.03(\text{sys})$

- Check $\eta'K^+$ asymmetries – find none.
- Errors about as expected for a sample this size
- Will soon reach interesting precision

Selection of $B^0 \rightarrow K^+K^-K_S^0$

- Belle systematically studying three body final states
- In particular $B^+ \rightarrow K^+K^-K^+$ very interesting



- Suppose $K^+K^-K_S^0$ is a mixture of CP-even and CP-odd
- $B \rightarrow KK\pi$ shows $b \rightarrow u\bar{u}s$ isospin violating trees small ($\leq 3\%$)
- $b \rightarrow q\bar{q}s$ penguin transitions conserve isospin

$$\begin{aligned}
 |K^+K^-K_S^0\rangle &= \alpha |>_{\text{CP}=+1} + \beta |>_{\text{CP}=-1} \\
 |K^0\bar{K}^0K^+\rangle &= \alpha \frac{(|K^+K_S^0K_S^0\rangle + |K^+K_L^0K_L^0\rangle)}{\sqrt{2}} + \beta |K^+K_S^0K_L^0\rangle
 \end{aligned}$$

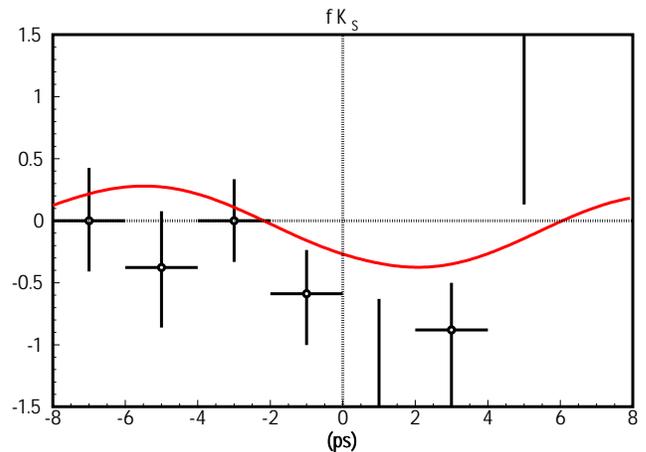
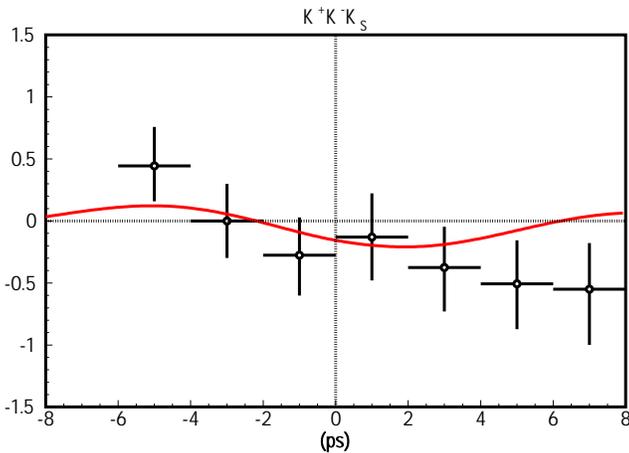
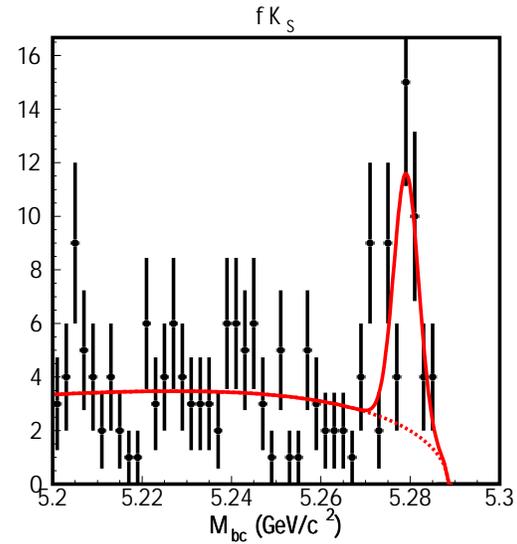
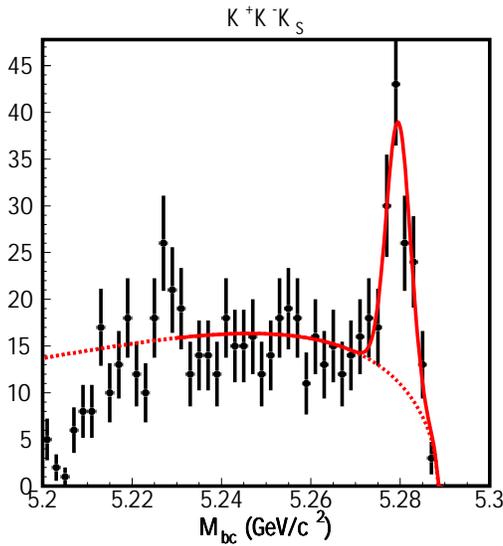
- From $\mathcal{B}(B^+ \rightarrow K^+K_S^0K_S^0)$ and $\mathcal{B}(B^0 \rightarrow K^+K^-K^0)$ conclude

- $|K^+K^-K_S^0\rangle_{\text{non-}\phi}$ is $97^{+3}_{-16}\%$ even

- While $B^0 \rightarrow \phi K_S^0$ is CP-odd

CP Asymmetry in $B^0 \rightarrow K^+K^-K_S^0$

- CP-signal consists of
 - 95 ± 7 $K^+K^-K_S^0$ candidates with $m_{K^+K^-} \neq m_\phi$
 - 35 ± 3 ϕK_S^0 candidates



- Fit gives

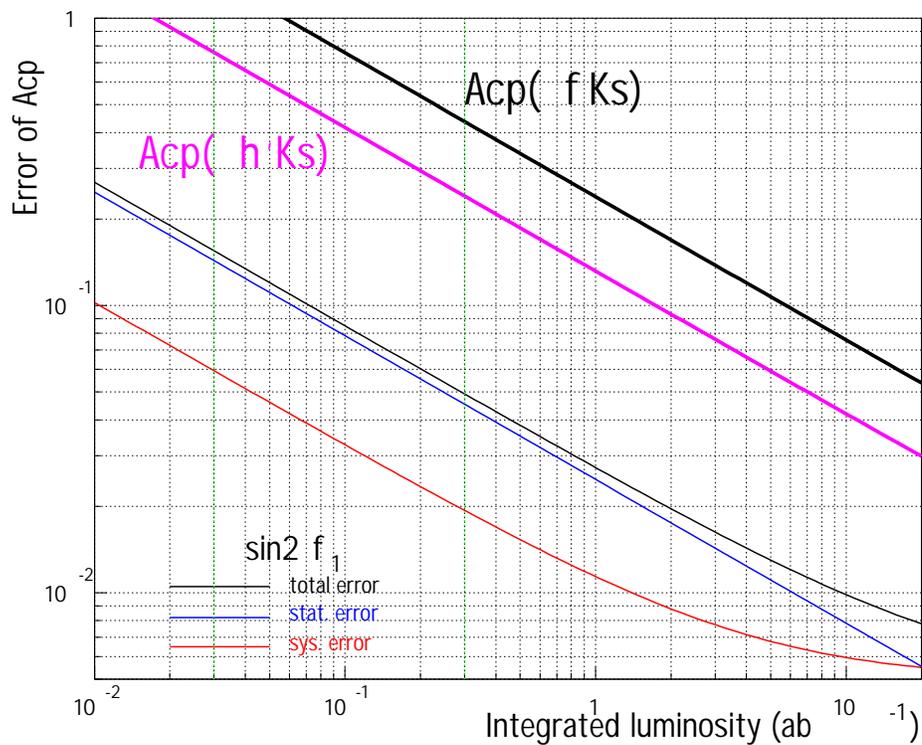
$$-\xi_{CP} S_{K^+K^-K_S^0} = 0.52 \pm 0.46(\text{stat}) \pm 0.11(\text{sys}) \begin{matrix} +0.27 \\ -0.03 \end{matrix} (\text{CP})$$

$$-\xi_{CP} S_{\phi K_S^0} = -0.73 \pm 0.64(\text{stat}) \pm 0.18(\text{sys})$$

- Higher mass K^+K^- modes make channel accessible sooner

Outlook for $\sin(2\phi_1)$

- Projections based on \sqrt{N} scaling
 - Most systematics still limited by size of control samples



- Precision of 0.2 on $S_{\eta' K_S^0}$ potentially interesting
- ϕK_S^0 asymmetry precision better with non- $\phi K^+ K^-$

Summary

- $\sin 2\phi_1 = 0.719 \pm 0.074(\text{stat}) \pm 0.035(\text{sys})$
- Indications of a non-zero asymmetry in $\pi^+\pi^-$

$$S_{\pi\pi} = -1.21_{-0.27}^{+0.38}(\text{stat})_{-0.13}^{+0.16}(\text{sys})$$
$$A_{\pi\pi} = 0.94_{-0.31}^{+0.25}(\text{stat}) \pm 0.09(\text{sys})$$

- New modes starting to have finite uncertainties

$$-\xi_{CP} S_{\eta K_S^0} = 0.76 \pm 0.36(\text{stat}) \pm 0.06(\text{sys})$$
$$-\xi_{CP} S_{\phi K_S^0} = -0.73 \pm 0.64(\text{stat}) \pm 0.18(\text{sys})$$
$$-\xi_{CP} S_{K^+K^-K_S^0} = 0.52 \pm 0.46(\text{stat}) \pm 0.11(\text{sys})_{-0.03}^{+0.27}(\text{CP})$$

- Looking forward to 0.25 ab^{-1} sample
 - Should further clarify matters