

# Precision Measurement of $\sin^2 q_w$ from NuTeV

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- Introduction
- Past measurements
- Current Improvements
- What's so new about the results?
- Conclusions

# NuTeV Collaboration

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# Electroweak Theory

- Standard Model unifies Weak and EM to SU(2)xU(1) gauge theory
  - Weak neutral current interaction
  - Measured physical parameters related to mixing parameters for the couplings

$$g' = g \tan \theta_w, e = g \sin \theta_w, G_F = \frac{g^2 \sqrt{2}}{8M_W^2}, \frac{M_W}{M_Z} = \cos \theta_w$$

- Neutrinos in this picture are unique because they only interact through left-handed weak interactions → Probe weak sector only
  - Less complication in some measurements, such as proton structure

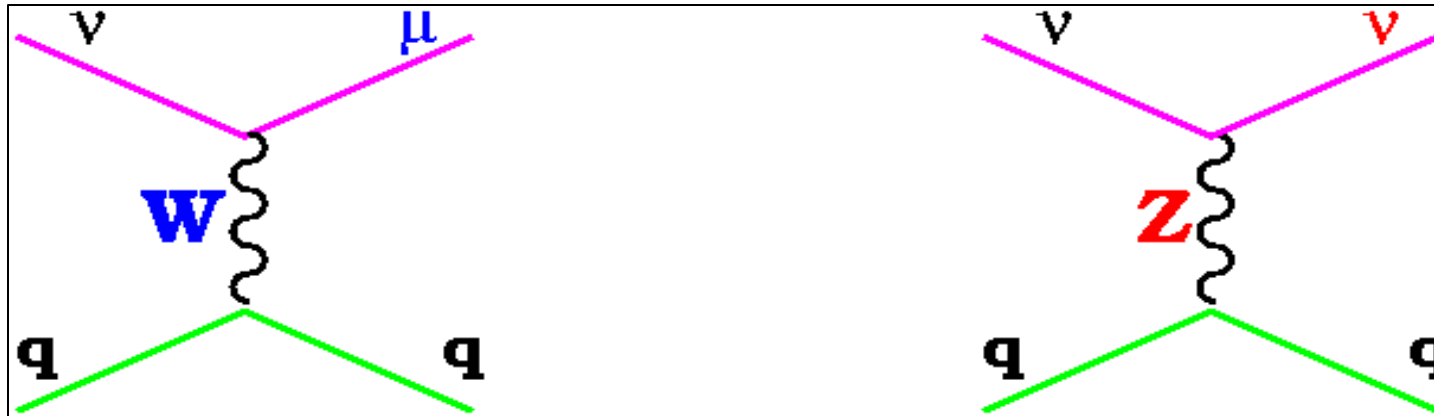
# $\sin^2 q_W$ and n-N scattering

- In the electroweak sector of the Standard Model, it is not known *a priori* what the mixture of electrically neutral electromagnetic and weak mediator is → This fractional mixture is given by the mixing angle
- Within the on-shell renormalization scheme,  $\sin^2 \theta_W$  is:

$$\sin^2 q_w^{\text{On-Shell}} = 1 - \frac{M_W^2}{M_Z^2}$$

- Provides independent measurement of  $M_W$  & information to pin down  $M_{\text{Higgs}}$
- Comparable size of uncertainty to direct measurements
- Measures light quark couplings → Sensitive to other types (anomalous) of couplings
- In other words, sensitive to physics beyond SM → New vector bosons, compositeness,  $\nu$ -oscillations, etc

# How do we measure?



$$\text{coupling} \propto I_{\text{weak}}^{(3)}$$

$$\text{coupling} \propto I_{\text{weak}}^{(3)} - Q_{EM} \sin^2 \theta_W$$

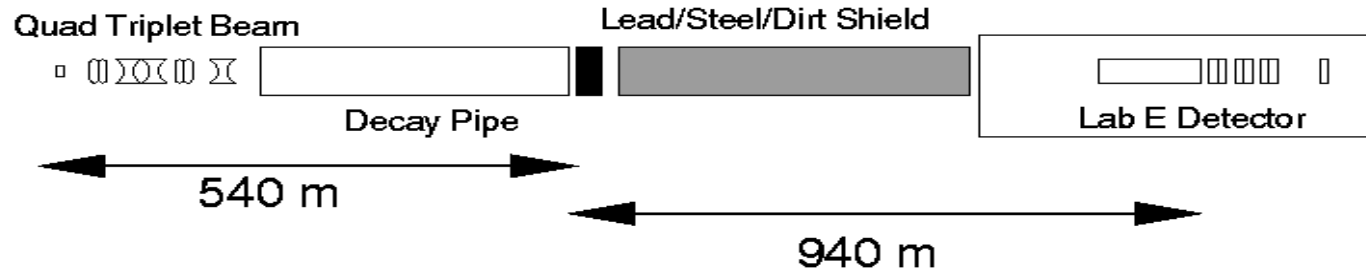
- Cross section ratios between NC and CC proportional to  $\sin^2 \theta_W$
- Llewellyn Smith Formula:

$$R^{n(\bar{n})} = \frac{S_{\text{NC}}^{n(\bar{n})}}{S_{\text{CC}}^{n(\bar{n})}} = \frac{1}{2} \left( 1 - \sin^2 \theta_W + \frac{5}{9} \sin^4 \theta_W \left( 1 + \frac{S_{\text{CC}}^{\bar{n}(n)}}{S_{\text{CC}}^{n(\bar{n})}} \right) \right)$$

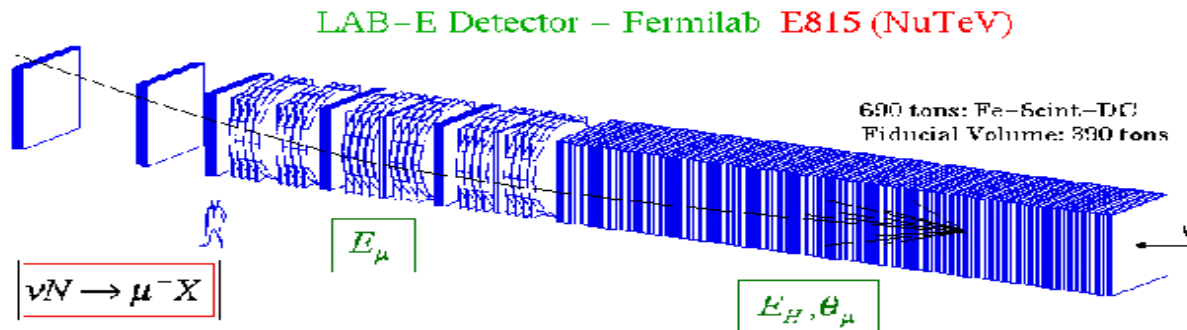
Some corrections are needed to extract  $\sin^2 \theta_W$  from measured ratios (radiative corrections, heavy quark effects, isovector target corrections, HT,  $R_L$ )

# Previous Experiment

## E770: Quad Triplet Beam and Lab E Detector



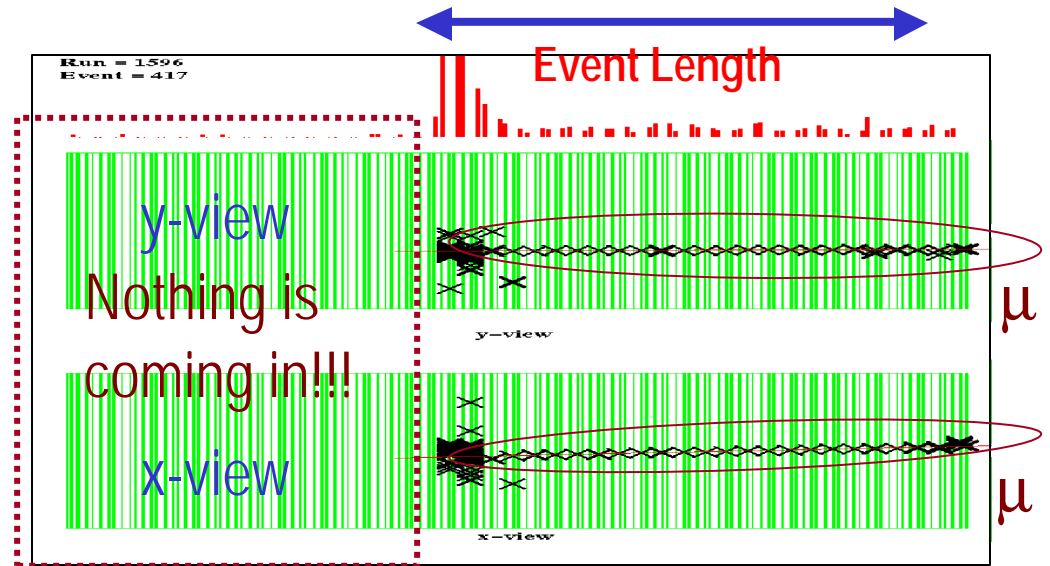
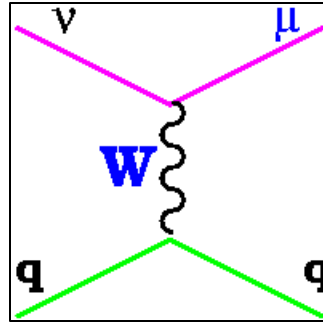
- Conventional neutrino beam from  $\pi/k$  decays
- Focus all signs of  $\pi/k$  for neutrinos and antineutrinos
- Only  $\nu_\mu$  in the beam (NC events are mixed)



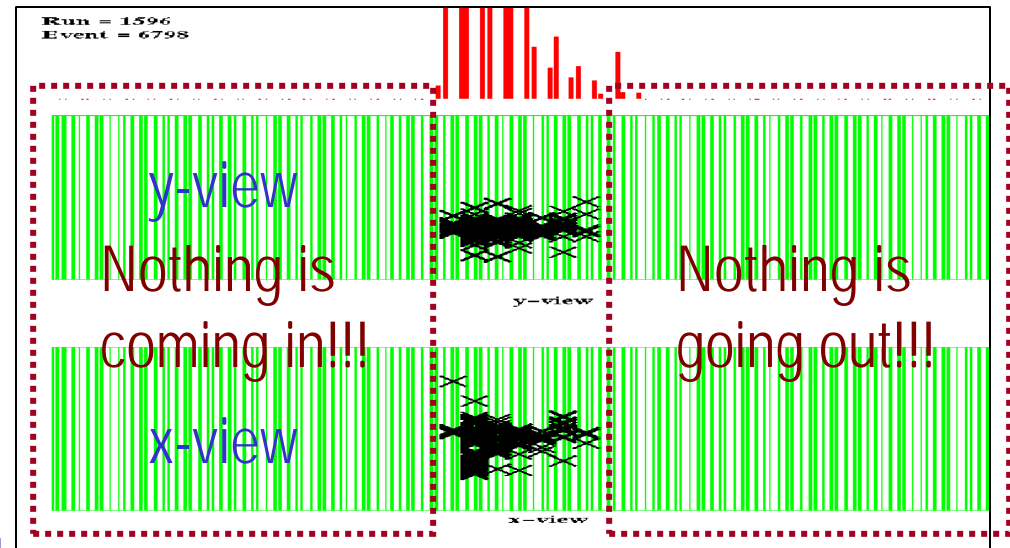
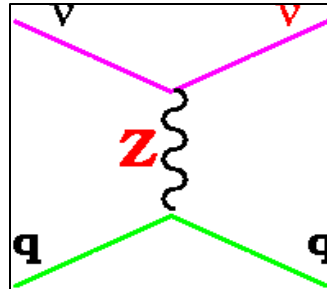
- Very small cross section  $\rightarrow$  Heavy neutrino target
- $\nu_e$  are the killers (CC events look the same as NC events)

# How Do We Separate Events?

Charged Current Events



Neutral Current Events

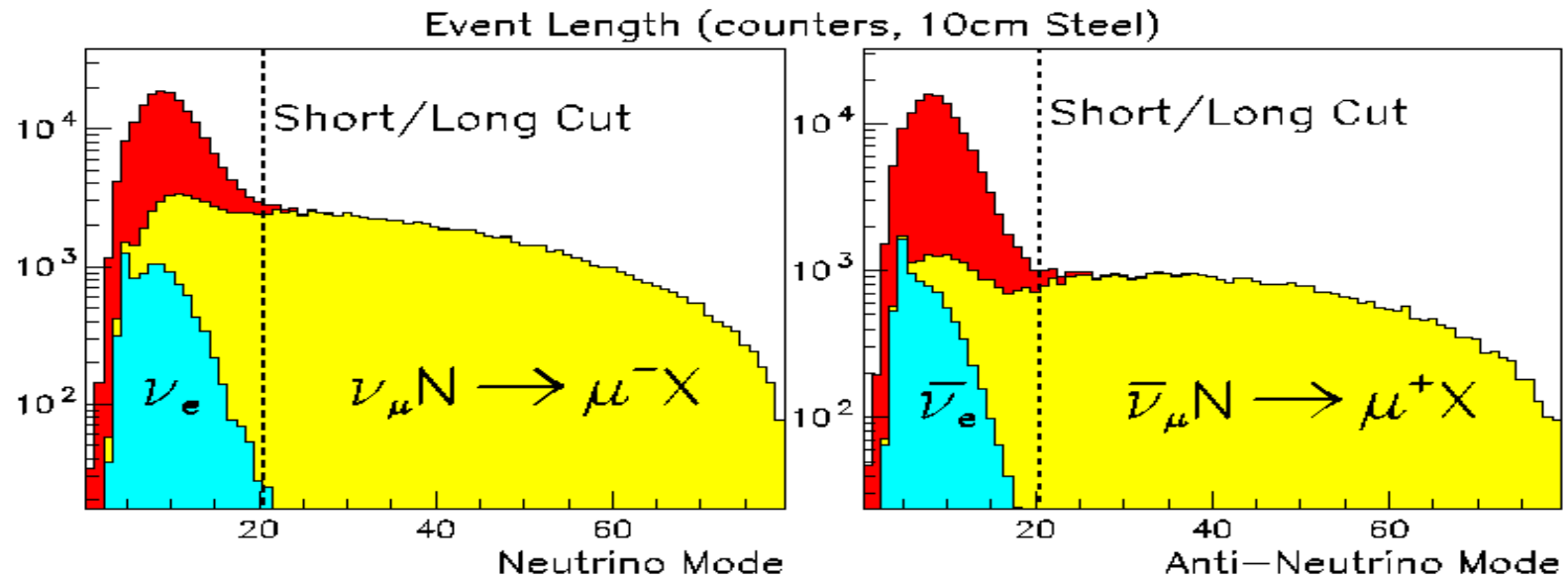


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# Event Length

Define an Experimental Length variable

→ Distinguishes CC from NC experimentally in statistical manner



Compare experimentally measured ratio

$$R_{\text{Exp}} = \frac{N_{\text{Short}}}{N_{\text{Long}}} = \frac{L < L_{\text{Cut}}}{L > L_{\text{Cut}}} = \frac{N_{\text{NC Candidates}}}{N_{\text{CC Candidates}}}$$

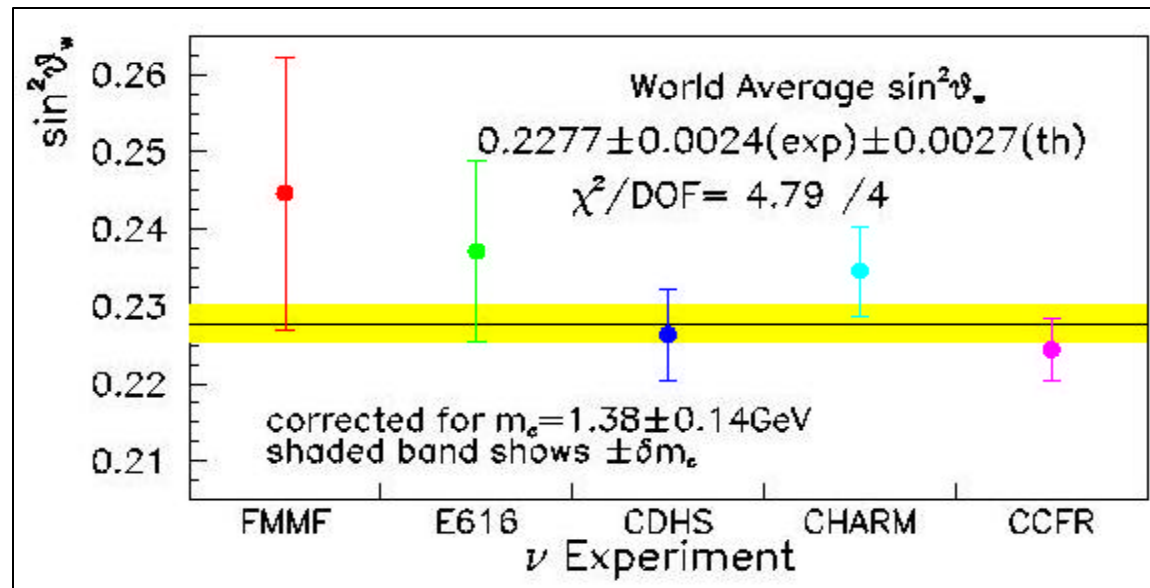
to theoretical prediction of  $R^\nu$



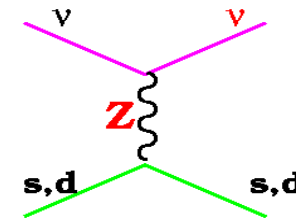
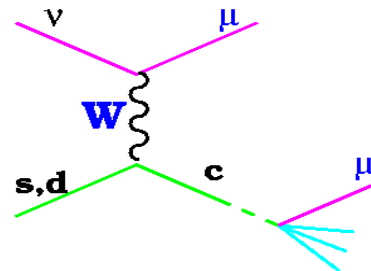
# Past Experimental Results

$$\sin^2 \theta_W^{\text{On-Shell}} = 1 - \frac{M_W}{M_Z} = 0.2277 \pm 0.0036$$

$$\Rightarrow M_W^{\text{On-Shell}} = 80.14 \pm 0.19 \text{ GeV}/c^2$$



- Significant correlated error from CC production of charm quark ( $m_c$ ) modeled by slow rescaling, in addition to  $\nu_e$  error



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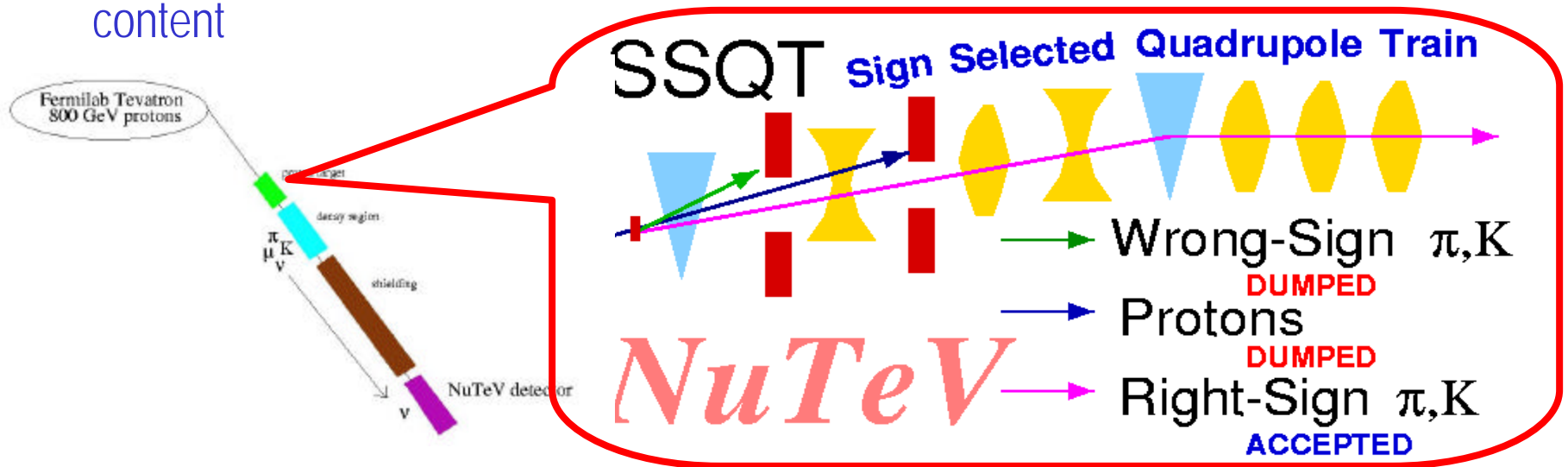
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# The NuTeV Experiment

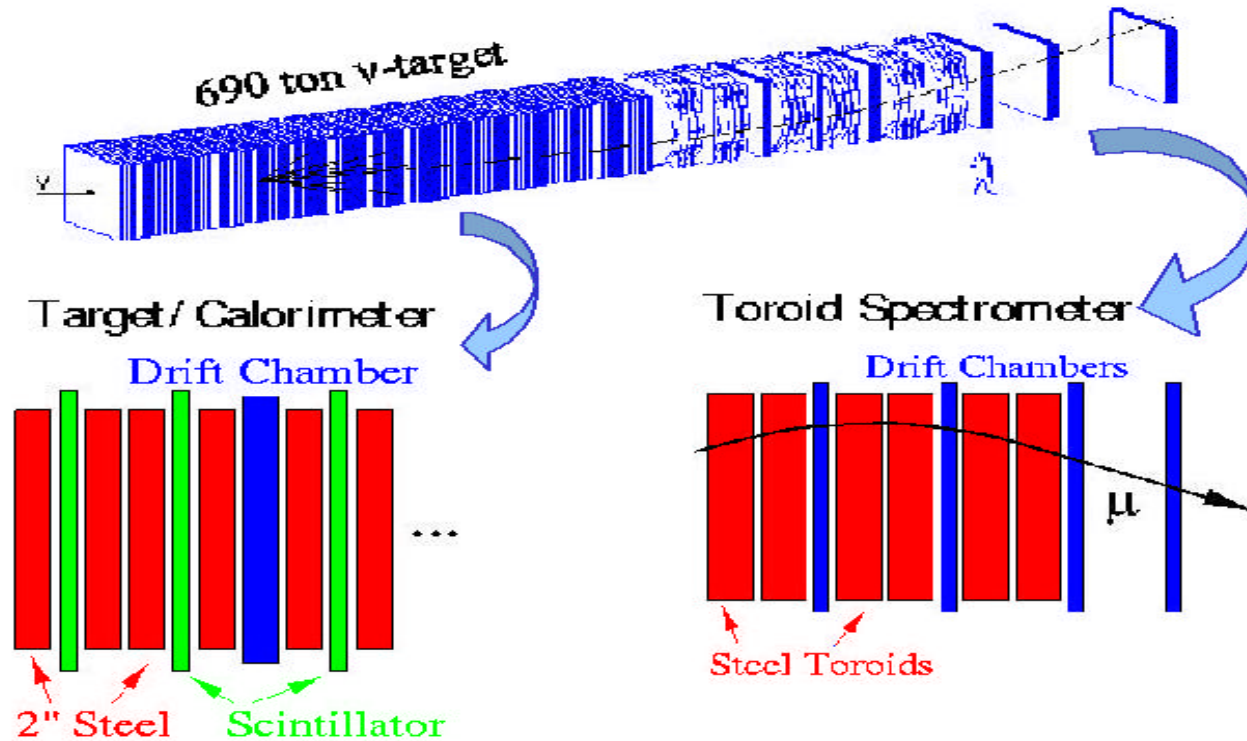
- Suggestion by Paschos-Wolfenstein formula by separating  $\nu$  and  $\bar{\nu}$  beams:

$$R^- = \frac{S_{NC}^n - S_{NC}^{\bar{n}}}{S_{CC}^n - S_{CC}^{\bar{n}}} = ?^2 \left( \frac{1}{2} - \sin^2 \theta_w \right) = \frac{R^n - R^{\bar{n}}}{1-r}$$

- Reduce charm CC production error by subtracting sea quark contributions
  - Only valence u, d, and s contributes while sea quark contributions cancel out
  - Massive quark production through Cabibbo suppressed  $d_s$  quarks only
- Smarter beamline → Removes all neutral secondaries to eliminate  $\nu_e$  content



# The NuTeV Detector



- Calorimeter
  - 168 FE plates & 690tons
  - 84 Liquid Scintillator
  - 42 Drift chambers interspersed

- Solid Iron Toroid
  - Measures Muon momentum
  - $\Delta p/p \sim 10\%$

Continuous test beam for in-situ calibration

# The NuTeV Detector



*A picture from 1998. The detector has been dismantled to make room for other experiments, such as DØ*

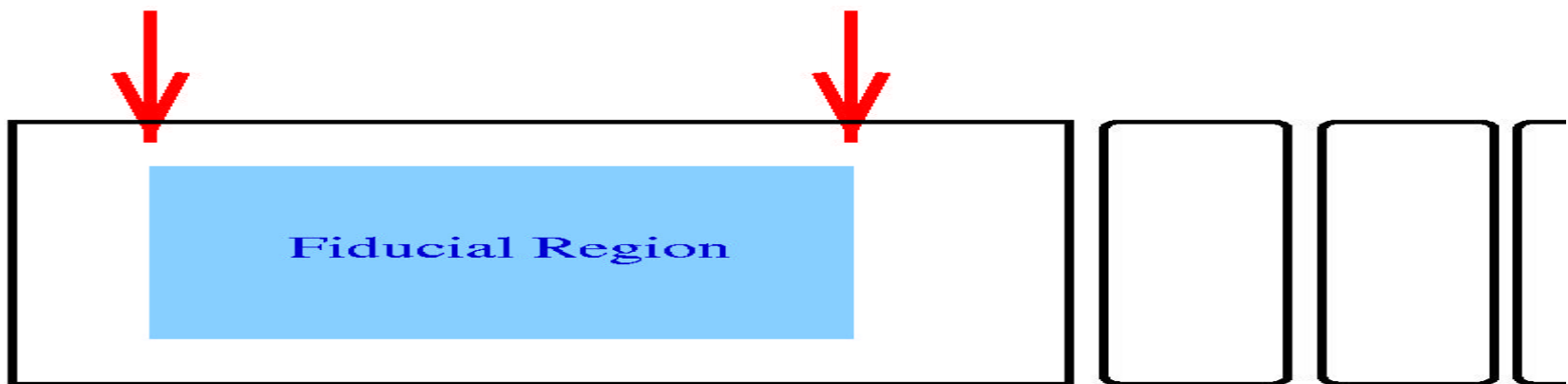
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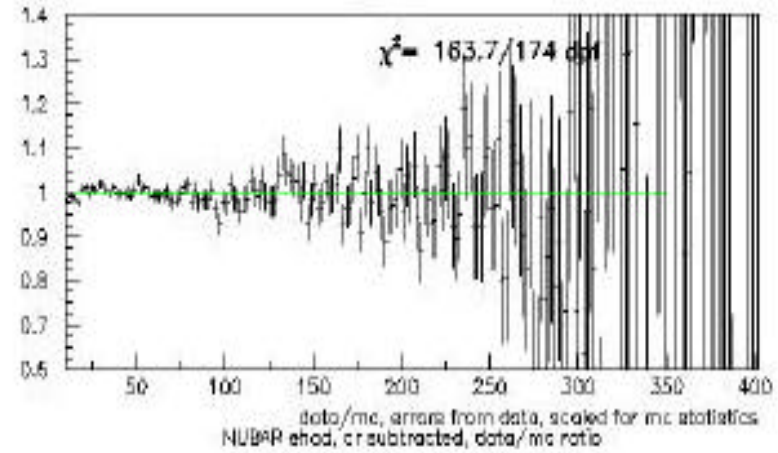
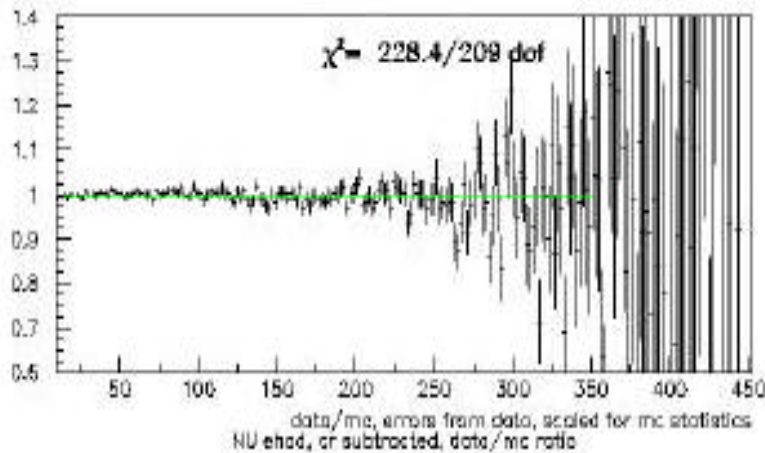
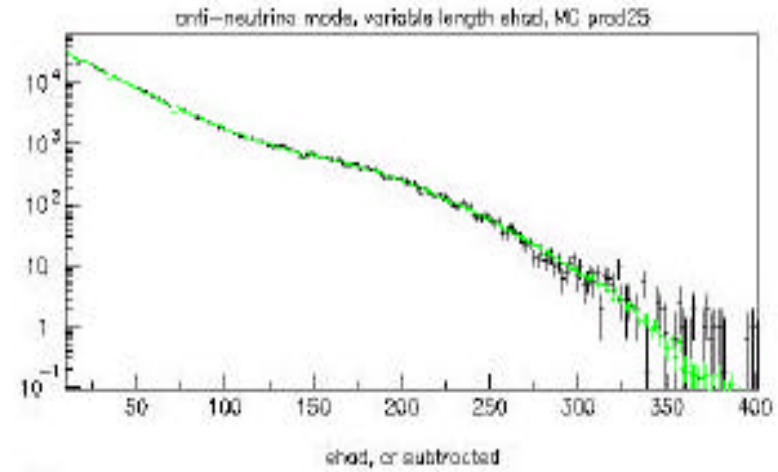
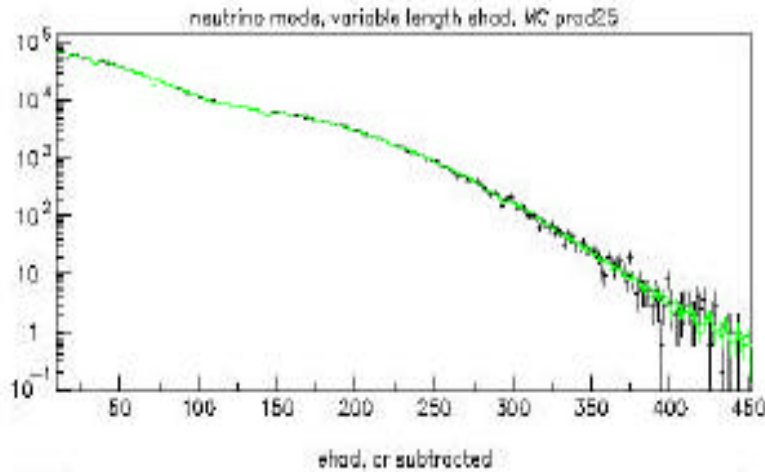
# NuTeV Event Selection

- $E_{\text{had}} > 20\text{GeV}$ 
  - To ensure vertex finding efficiency
  - To reduce cosmic ray contamination
- $X_{\text{vert}}$  and  $Y_{\text{vert}}$  within the central 2/3
  - Full hadronic shower and muon containment
  - Further reduce  $\nu_e$  contamination
- Longitudinal vertex,  $Z_{\text{vert}}$ , cut
  - To ensure neutrino induced interaction
  - Better discriminate CC and NC



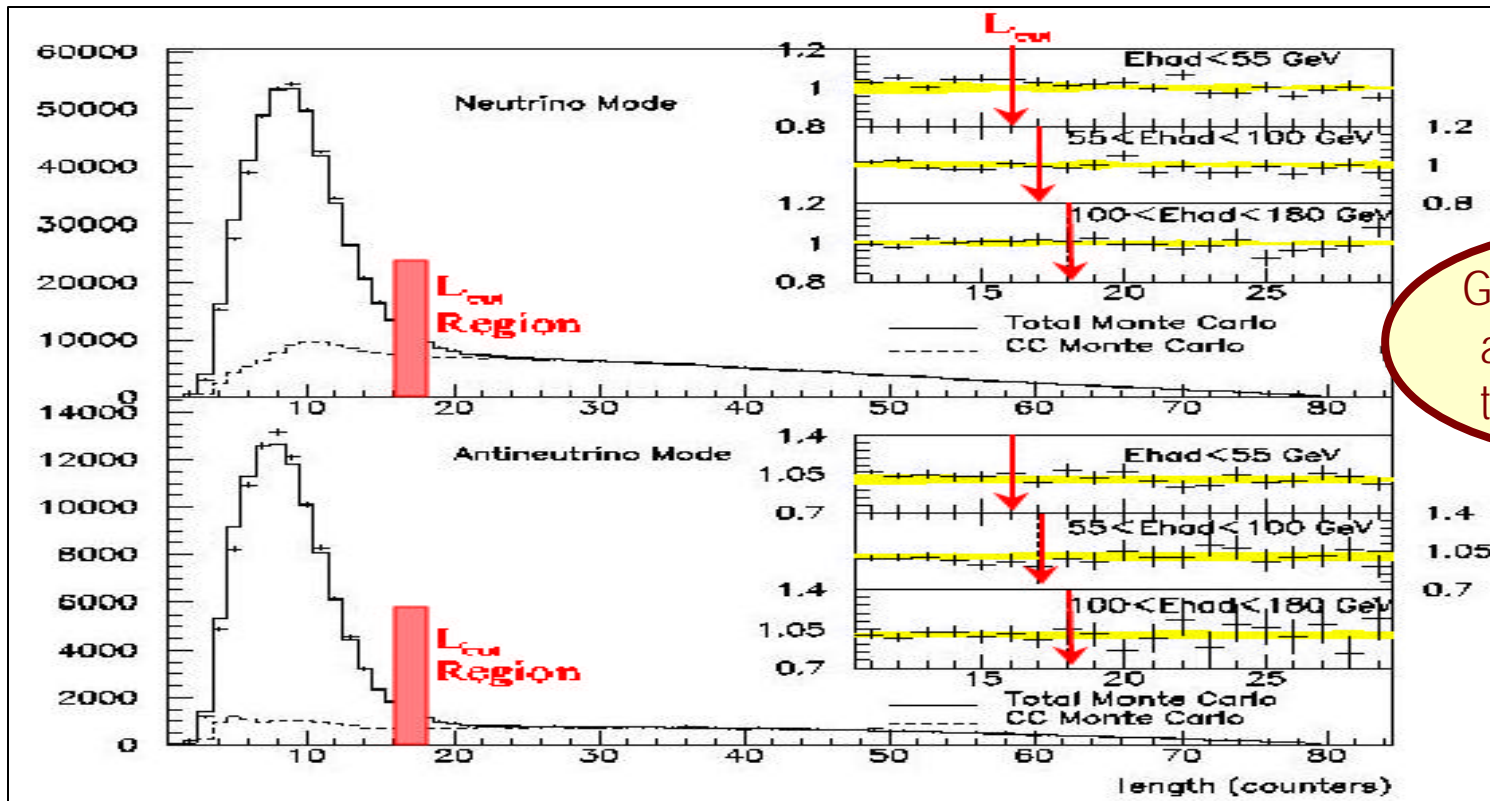
# Events and Flux After Selection

Remaining number of events: 1.62M  $\nu$  & 350k  $\bar{\nu}$



# NuTeV Event Length Distributions

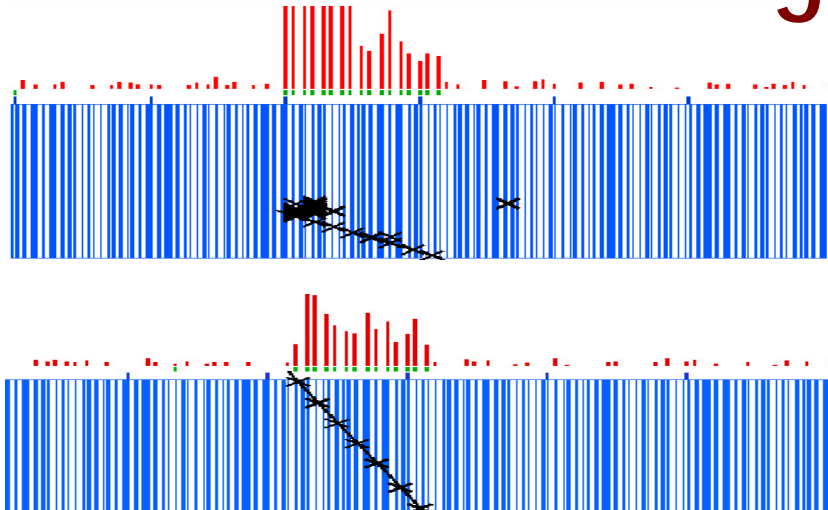
Energy Dependent Length cut implemented to improve statistics and reduce systematic uncertainties.



Good Data-MC agreement in the cut region

Mode	$N_{short}$	$N_{long}$	$R_v = N_{short} / N_{Long}$
$\nu$	457k	1167k	$0.3916 \pm 0.0007(\text{stat})$
$\bar{\nu}$	101k	250k	$0.4050 \pm 0.0016(\text{stat})$

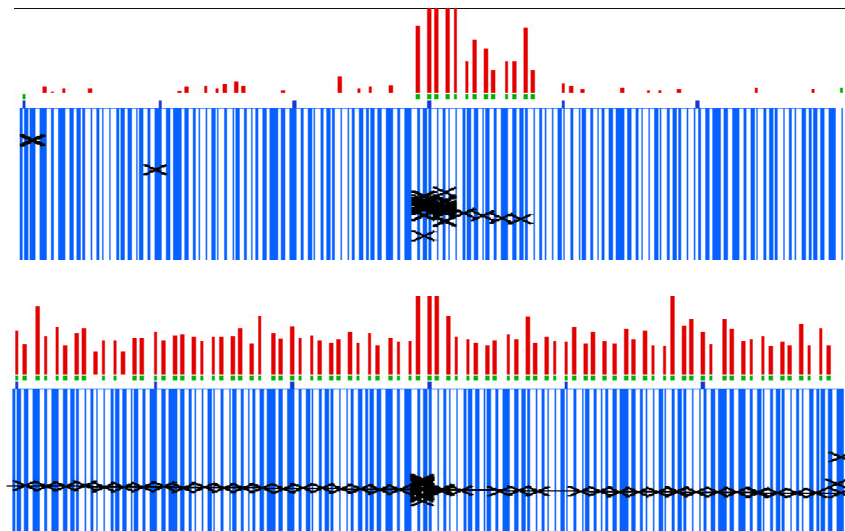
# Event Contamination and Backgrounds



- SHORT  $n_m$  CC's (20%  $n$ , 10%  $\bar{n}$ )  
 $\mu$  exit and rangeout
- SHORT  $n_e$  CC's (5%)  
 $\nu_e N \rightarrow eX$
- Cosmic Rays (0.9%)

- LONG  $n_m$  NC's (0.7%)  
hadron shower  
punch-through effects

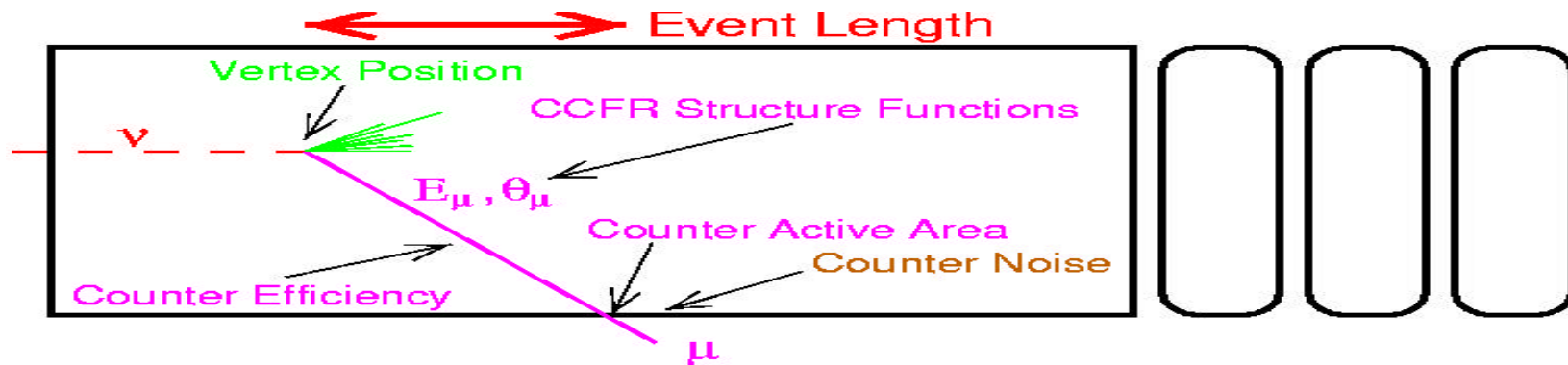
- Hard  $m$  Brem(0.2%)  
Deep  $\mu$  events



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# Other Detector Effects

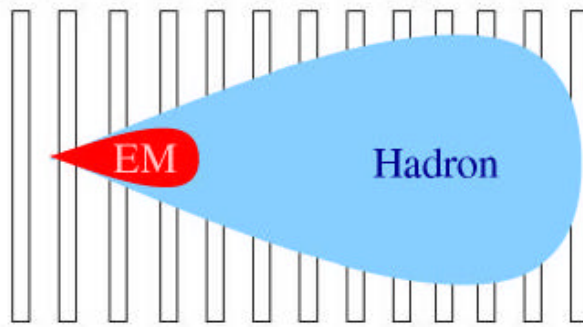


Sources of experimental uncertainties kept small, through modeling using  $n$  and TB data

Effect	Size( $d\sin^2q_w$ )	Tools
$Z_{\text{vert}}$	0.001/inch	$\mu^+\mu^-$ events
$X_{\text{vert}}$ & $Y_{\text{vert}}$	0.001	MC
Counter Noise	0.00035	TB $\mu$ 's
Counter Efficiency	0.0002	$\nu$ events
Counter active area	0.0025/inch	$\nu$ CC, TB
Hadron shower length	0.0015/cntr	TB $\pi$ 's and $k$ 's
Energy scale	0.001/1%	TB
Muon Energy Deposit	0.004	$\nu$ CC

# Measurements of $n_e$ Flux

- Neutrino events in anti-neutrino running constraint charm and  $K_L$  induced production ( $K_{e3}$ ) in the medium energy range ( $80 < E_\nu < 180 \text{ GeV}$ )
- Shower Shape Analysis can provide direct measurement  $\nu_e$  events, though less precise



$$\frac{N_{\text{meas}}}{N_{\text{MC}}}$$

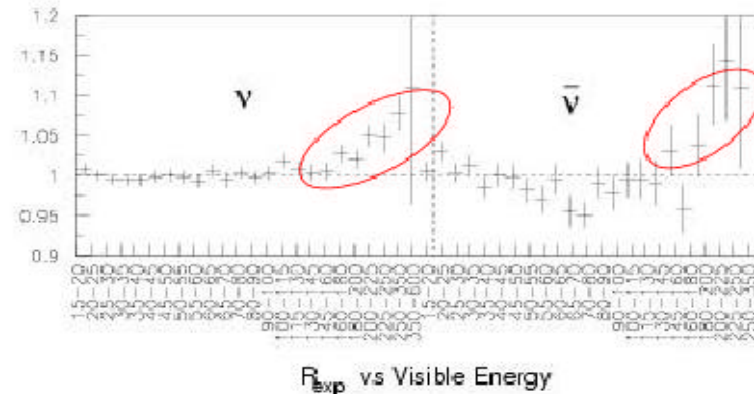
$$1.05 \pm 0.03 (n_e)$$

$$1.01 \pm 0.04 (\bar{n}_e)$$

Weighted average  
used for  $\nu_e$   
 $\rightarrow \delta R_{\nu}^{\text{exp}} \sim 0.0005$

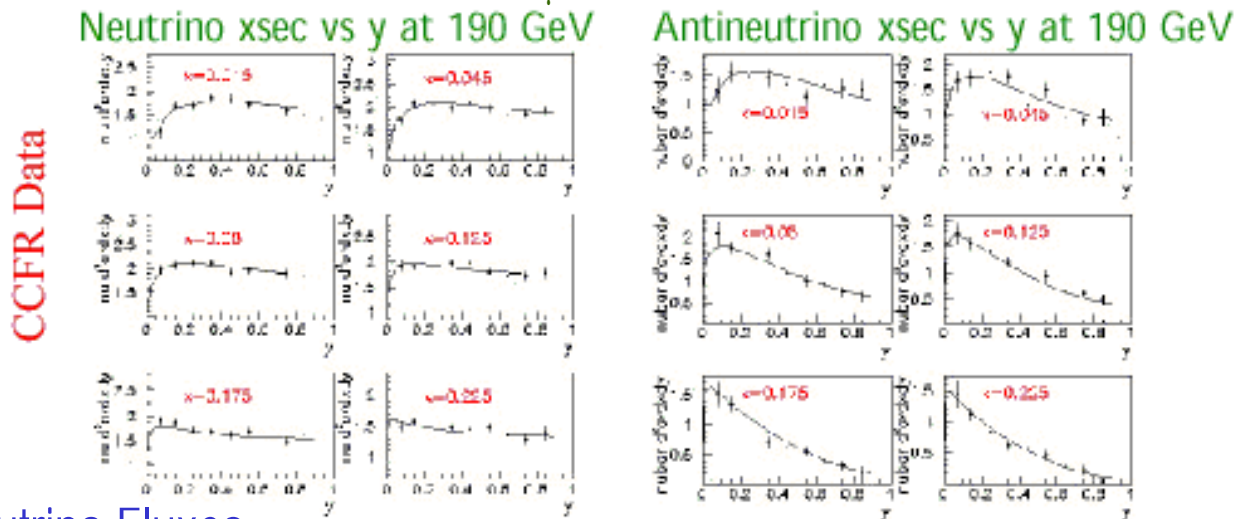
- $\nu_e$  from very short events ( $E_\nu > 180 \text{ GeV}$ )
  - Precise measurement of  $\nu_e$  flux in the tail region of flux  $\rightarrow$  ~35% more  $\bar{\nu}_e$  in  $\bar{\nu}$  than predicted
  - Had to require ( $E_{\text{had}} < 180 \text{ GeV}$ ) due to ADC saturation

Results in  $\sin^2\theta_w$  shifts by +0.002

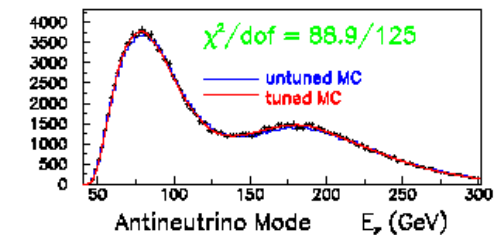
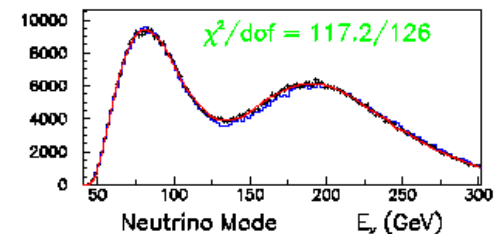


# MC to Relate $R_n^{\text{exp}}$ to $R^n$ and $\sin^2 q_W$

- Parton Distribution Model
  - Correct for details of PDF model → Used CCFR data for PDF
  - Model cross over from short  $\nu_\mu$  CC events



- Neutrino Fluxes
  - $\nu_\mu, \nu_e, \bar{\nu}_\mu, \bar{\nu}_e$  in the two running modes
  - $\nu_e$  CC events always look short
- Shower length modeling
  - Correct for short events that look long
- Detector response vs energy, position, and time
  - Continuous testbeam running minimizes systematics



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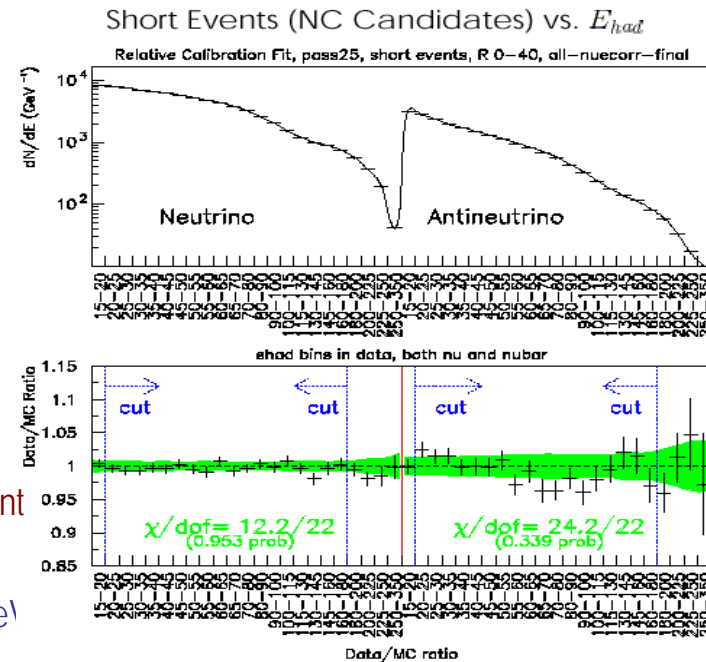
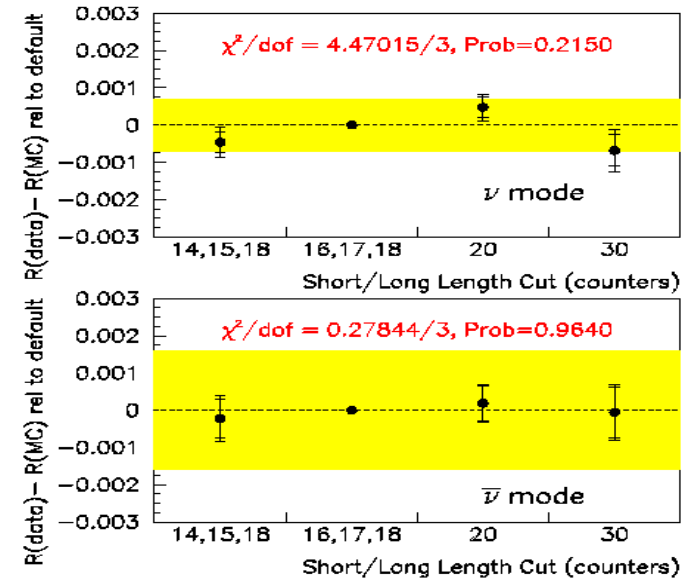
# $R_n^{\text{exp}}$ Stability Check

- Crucial to verify the  $R_v^{\text{exp}}$  comparison to MC is consistent under changes in cuts and event variables
  - Longitudinal vertex  $\rightarrow$  Detector uniformity
  - Length cut  $\rightarrow$  Check CC to NC cross over
  - Transverse vertex  $\rightarrow$  NC background at the detector edge
  - Visible energy ( $E_{\text{Had}}$ )  $\rightarrow$  Checks detector energy scale and other factors

Green bands represent  $1\sigma$  uncertainty.

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# $\sin^2\theta_W$ Fit to $R_n^{\text{exp}}$ and $R_{\bar{n}}^{\text{exp}}$

- Thanks to the separate beam → Measure  $R^{\nu}$ 's separately
- Use MC to simultaneously fit  $R_n^{\text{exp}}$  and  $R_{\bar{n}}^{\text{exp}}$  to  $\sin^2\theta_W$  and  $m_c$ , and  $\sin^2\theta_W$  and  $\rho$

$$R^{n(\bar{n})} = \frac{S_{\text{NC}}^{n(\bar{n})}}{S_{\text{CC}}^{n(\bar{n})}} = \sin^2\theta_W \left( \frac{1}{2} - \sin^2\theta_W + \frac{5}{9} \sin^4\theta_W \left( 1 + \frac{S_{\text{CC}}^{\bar{n}(n)}}{S_{\text{CC}}^{n(\bar{n})}} \right) \right)$$

- $R^{\nu}$  Sensitive to  $\sin^2\theta_W$  while  $R^{\bar{\nu}}$  isn't, so  $R^{\nu}$  is used to extract  $\sin^2\theta_W$  and  $R^{\bar{\nu}}$  to control systematics
- Single parameter fit, using SM values for EW parameters ( $\rho_0=1$ )

$$\sin^2\theta_W = 0.2277 \pm 0.0013 \text{ (stat)} \pm 0.0009 \text{ (syst)}$$

$$m_c = 1.32 \pm 0.09 \text{ (stat)} \pm 0.06 \text{ (syst)} \text{ w/ } m_c = 1.38 \pm 0.14 \text{ GeV}/c^2 \text{ as input}$$

- Two parameter fit for  $\sin^2\theta_W$  and  $\rho_0$  yields

$$\sin^2\theta_W = 0.2265 \pm 0.0031$$

$$\rho_0 = 0.9983 \pm 0.040$$

Syst. Error dominated since we cannot take advantage of sea quark cancellation

# NuTeV $\sin^2\theta_W$ Uncertainties

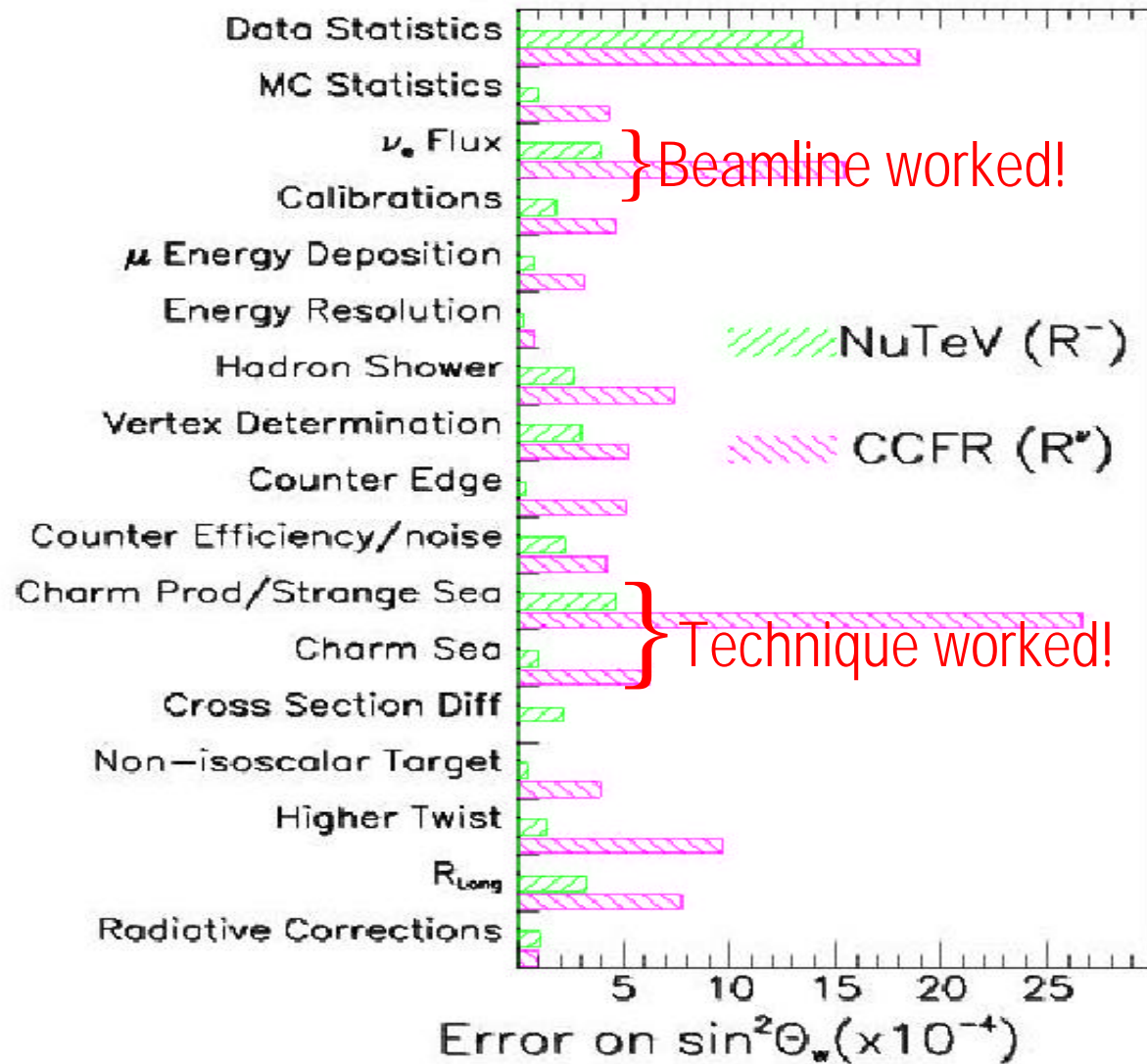
Source of Uncertainty	$d \sin^2\theta_W$
<b>Statistical</b>	<b>0.00135</b>
$\nu_e$ flux	0.00039
Event Length	0.00046
Energy Measurements	0.00018
<b>Total Experimental Systematics</b>	<b>0.00063</b>
CC Charm production, sea quarks	0.00047
Higher Twist	0.00014
Non-isoscalar target	0.00005
$s^{\bar{n}} / s^n$	0.00022
Radiative Correction	0.00011
$R_L$	0.00032
<b>Total Physics Model Systematics</b>	<b>0.00064</b>
<b>Total Systematic Uncertainty</b>	<b>0.00162</b>
<b><math>DM_W</math> (GeV/c<sup>2</sup>)</b>	<b>0.08</b>

Dominant uncertainty

1-Loop Electroweak Radiative Corrections based on Bardin, Dokuchaeva **JINR-E2-86-2 60 (1986)**

$$d\sin^2\theta_W^{(On-shell)} = -0.00022 \times \left( \frac{M_t^2 - (175\text{GeV})^2}{(50\text{GeV})^2} \right) + 0.00032 \times \ln\left( \frac{M_H}{150\text{GeV}} \right)$$

# NuTeV vs CCFR Uncertainty Comparisons



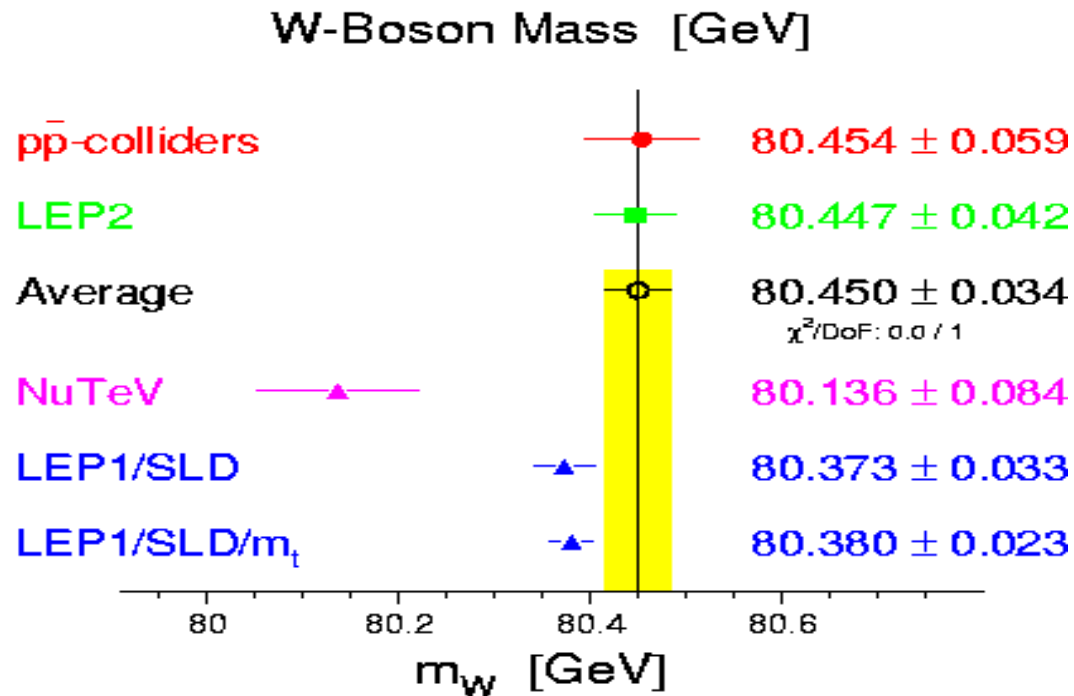
# The NuTeV $\sin^2\theta_W$

$$\sin^2\theta_W^{\text{On-Shell}} = 0.2277 \pm 0.0013 \text{ (stat)} \pm 0.0009 \text{ (syst)}$$

$$\sin^2\theta_W^{\text{On-shell}} = 1 - \frac{M_W^2}{M_Z^2}$$

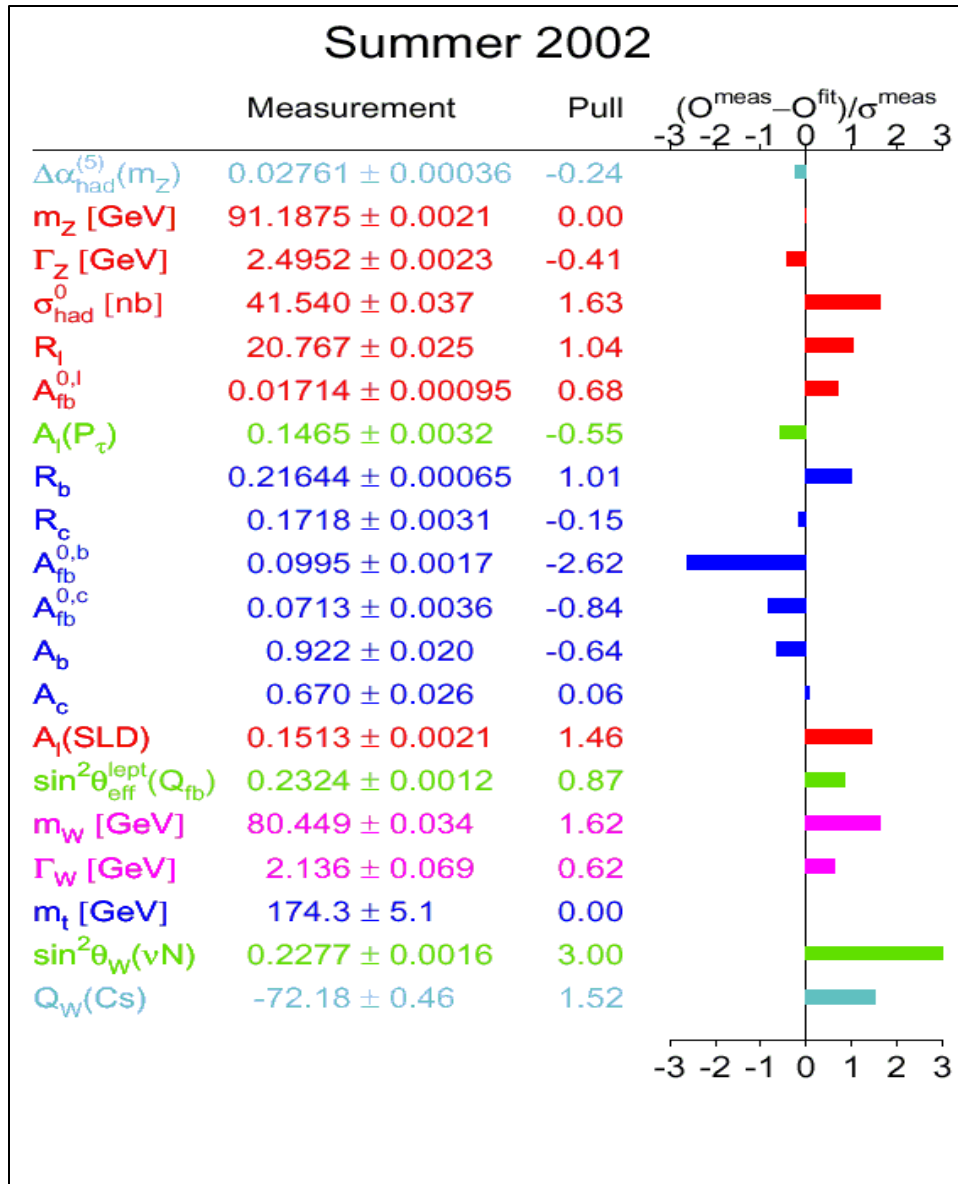
$$\Rightarrow M_W^{\text{On-Shell}} = 80.14 \pm 0.08 \text{ GeV}/c^2$$

Comparable precision but value smaller than other measurements





# SM Global Fits with NuTeV Result



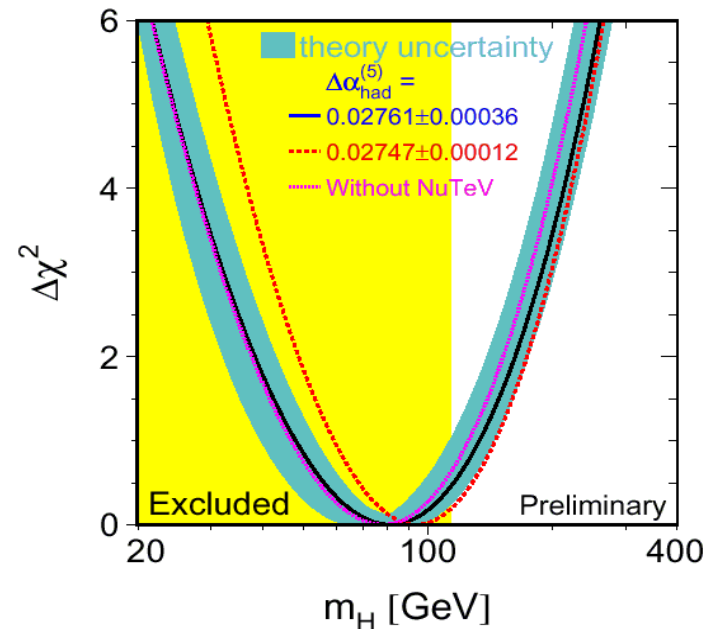
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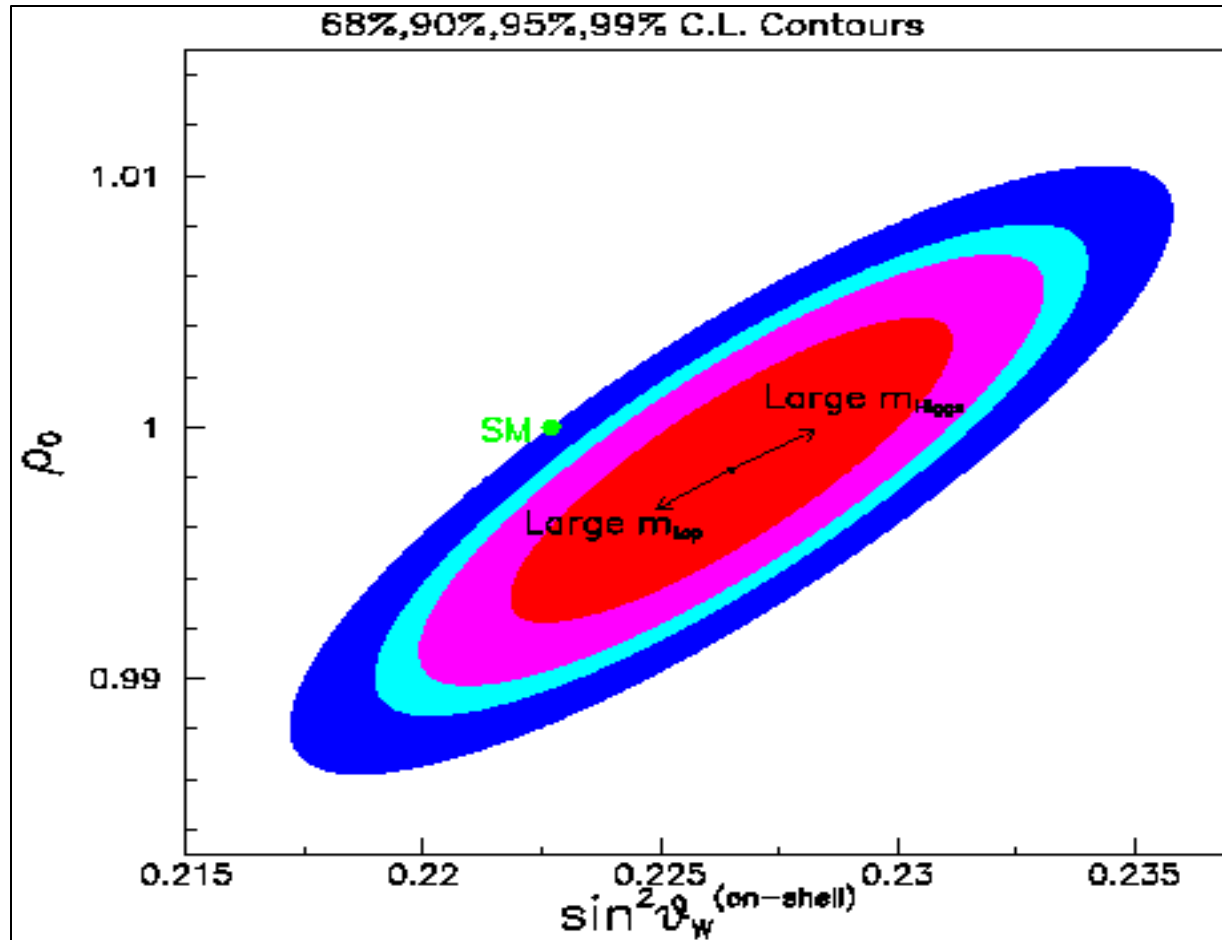
Without NuTeV  
 $\chi^2/\text{dof} = 20.5/14$ :  $P = 11.4\%$

With NuTeV  
 $\chi^2/\text{dof} = 29.7/15$ :  $P = 1.3\%$

Confidence level in upper  
 $M_{\text{higgs}}$  limit weakens slightly.



# Tree-level Parameters: $\rho_0$ and $\sin^2\theta_W^{(\text{on-shell})}$



- Either  $\sin^2\theta_W^{(\text{on-shell})}$  or  $\rho_0$  could agree with SM but both agreeing simultaneously is unlikely

# Model Independent Analysis

- Performed the fit to quark couplings (and  $g_L$  and  $g_R$ )
  - For isoscalar target, the  $\nu N$  couplings are

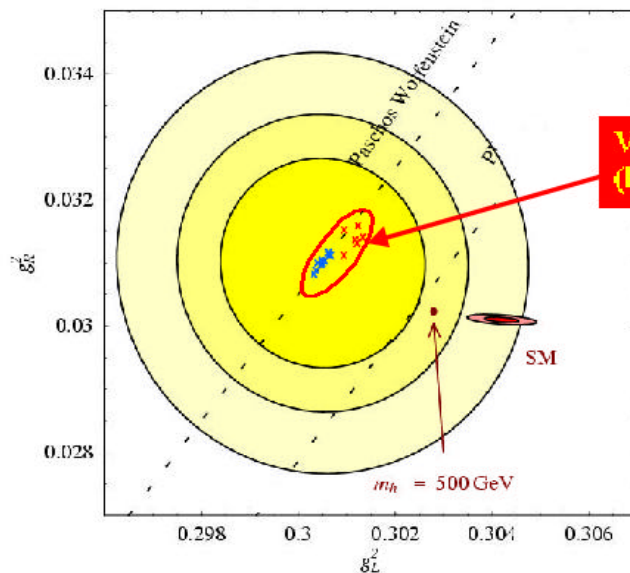
$$g_L^2 = u_L^2 + d_L^2 = ?_0^2 \left( \frac{1}{2} + \sin^2 ?_w + \frac{5}{9} \sin^4 ?_w \right)$$

$$g_R^2 = u_R^2 + d_R^2 = ?_0^2 \frac{5}{9} \sin^4 ?_w$$

- From two parameter fit to  $R_n^{\text{exp}}$  and  $R_{\bar{n}}^{\text{exp}}$

$$g_L^2 = 0.3005 \pm 0.0014 \quad (\text{SM: } 0.3042 \leftarrow -2.6\sigma \text{ deviation})$$

$$g_R^2 = 0.0310 \pm 0.0011 \quad (\text{SM: } 0.0301 \leftarrow \text{Agreement})$$



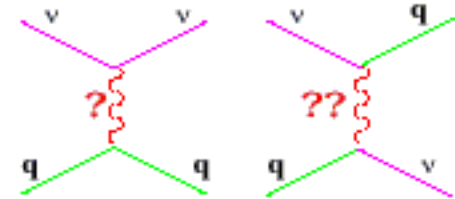
Difficult to explain the disagreement with SM by:  
 Parton Distribution Function or LO vs NLO or  
 Electroweak Radiative Correction: large  $M_{\text{Higgs}}$

# What is the discrepancy due to (Old Physics)?

- R- technique is sensitive to  $q$  vs  $\bar{q}$  differences and NLO effect
  - Difference in valence quark and anti-quark momentum fraction
- Isospin spin symmetry assumption might not be entirely correct
  - Expect violation about 1% → NuTeV reduces this effect by using the ratio of  $\nu$  and  $\bar{\nu}$  cross sections → Reducing dependence by a factor of 3
- $s$  vs  $\bar{s}$  quark asymmetry
  - $s$  and  $\bar{s}$  needs to be the same but the momentum could differ
    - A value of  $\Delta s = s - \bar{s} \sim +0.002$  could shift  $\sin^2\theta_W$  by  $-0.0026$ , explaining  $\frac{1}{2}$  the discrepancy (S. Davison, et. al., hep-ph/0112302)
    - NuTeV di- $\mu$  measurement shows that  $\Delta s \ll 0.002$
- NLO and PDF effects
  - PDF,  $m_c$ , Higher Twist effect, etc, are small changes
- Heavy vs light target PDF effect (Kovalenko et al., hep-ph/0207158)
  - Using PDF from light target on Iron target could make up the difference  
→ NuTeV result uses PDF extracted from CCFR (the same target)

# What other explanations (New Physics)?

- Heavy non-SM vector boson exchange:  $Z'$ ,  $LQ$ , etc
  - LL coupling enhanced than LR needed for NuTeV
- Propagator and coupling corrections
  - Small compared to the effect
- MSSM : Loop corrections wrong sign and small for the effect
- Gauge boson interactions
  - Allow generic couplings → Extra  $Z'$  bosons???
  - LEP and SLAC results says  $< 10^{-3}$
- Many other attempts in progress but so far nothing seems to explain the NuTeV results
  - Lepto-quarks
  - Contact interactions with LL coupling (NuTeV wants  $m_{Z'} \sim 1.2\text{TeV}$ , CDF/D0:  $m_{Z'} > 700\text{GeV}$ )
  - Almost sequential  $Z'$  with opposite coupling to  $\nu$



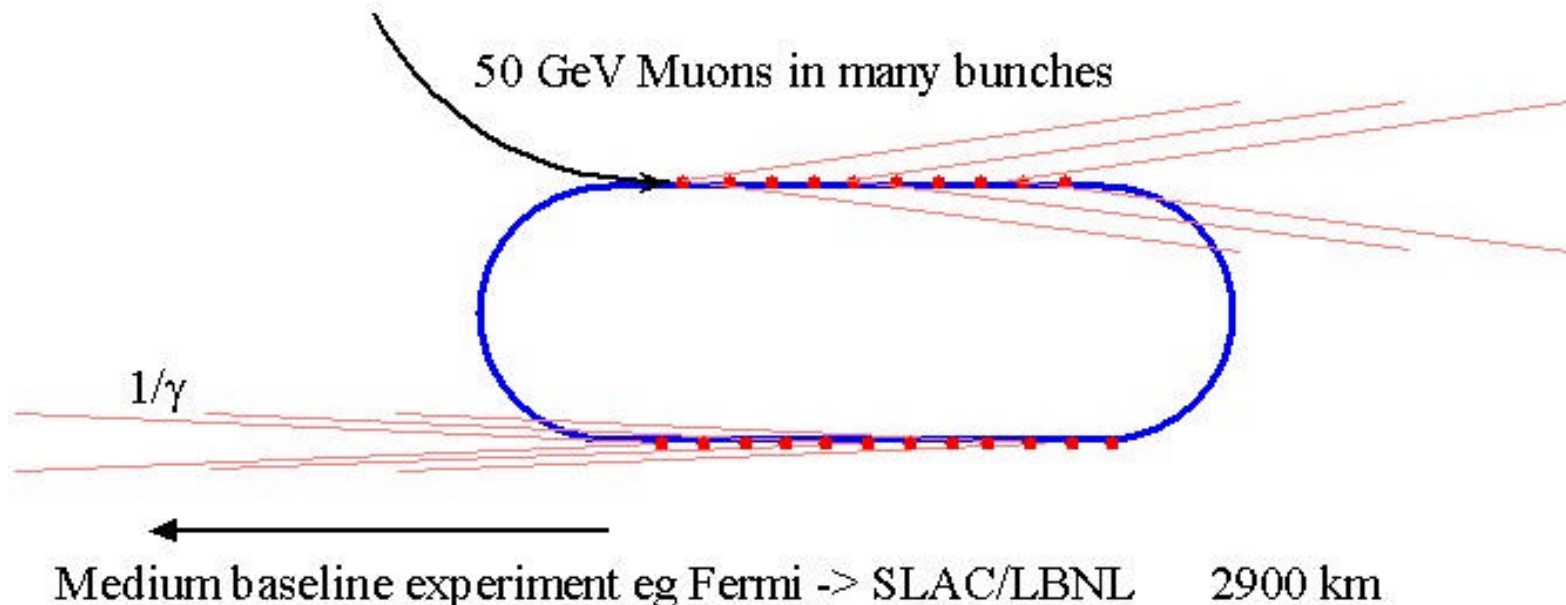
Langacker *et al*, Rev. Mod. Phys. **64** 87; Cho *et al.*, Nucl. Phys. **B531**, 65;  
Zupfeld and Cheung, hep-ph/9810277; Davidson *et al.*, hep-ph/0112302

# Future???

Muon storage ring can generate  $10^6$  times higher flux and well understood, high purity neutrino beam  $\rightarrow$  significant reduction in statistical uncertainty

But  $\nu_e$  and  $\nu_\mu$  from muon decays are in the beam at all times  $\rightarrow$  Deadly for traditional heavy target detectors

Muon Storage Ring as a Neutrino Source



# Conclusions

- NuTeV has measured  $\sin^2\theta_W$ :

$$\sin^2\theta_W^{\text{On-shell}} = 0.2277 \pm 0.0013 \text{ (stat)} \pm 0.0009 \text{ (syst)}$$

$$\Rightarrow M_W^{\text{On-Shell}} = 80.14 \pm 0.08 \text{ GeV}/c^2$$

- NuTeV result deviates from SM prediction by about  $+3\sigma$  (PRL 88, 091802, 2002)
- Interpretations of this result implicates lower left-hand coupling ( $-2.6\sigma$ ) but good agreement in right-hand coupling with SM
- NuTeV discrepancy has generated a lot of interest in the community
  - Still could be a large statistical fluctuation ( $5\sigma$  has happened before)
  - Yet, many interpretations are being generated:
    - Some could explain partially but not all
    - Asymmetric s-quark sea
    - Additional mediator, extra U(1) vector bosons, etc
  - No single one can explain the discrepancy  $\rightarrow$  it still is a puzzle...
- Could this be a signature of new physics?
  - No other current experiment is equipped to redo this measurement
  - Muon storage ring seems to provide a promising future...