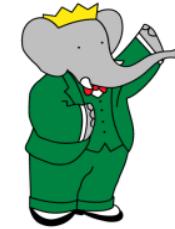
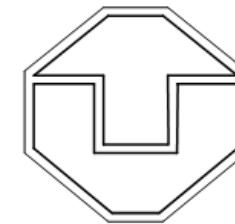


Klaus R. Schubert, TU Dresden



27 October 2008, B-Factory Symposium  
in recognition of the achievements of PEP-II and BABAR

# Quark Mixing at BABAR



Quark Mixing in the St. Model: Origin of observed CP Violation

Manifestations:  $K^0$ ,  $D^0$ ,  $B^0$  Oscillations and

CKM Hierarchy of Weak Decays

BABAR Contributions to  $B^0$  and  $D^0$  Oscillations and to

Determinations of  $V_{us}$ ,  $V_{cb}$ ,  $V_{ub}$ ,  $(V_{ts})$ ,  $V_{td}$

Deviations from the CKM Description of Quark Mixing?



# Without Quark Mixing No CP Violation<sup>\*)</sup>

Example: Discovery of „Direct CPV“

in  $B \rightarrow K^+ \pi^-$ ,  $K^- \pi^+$  PRL 93(2004)131801

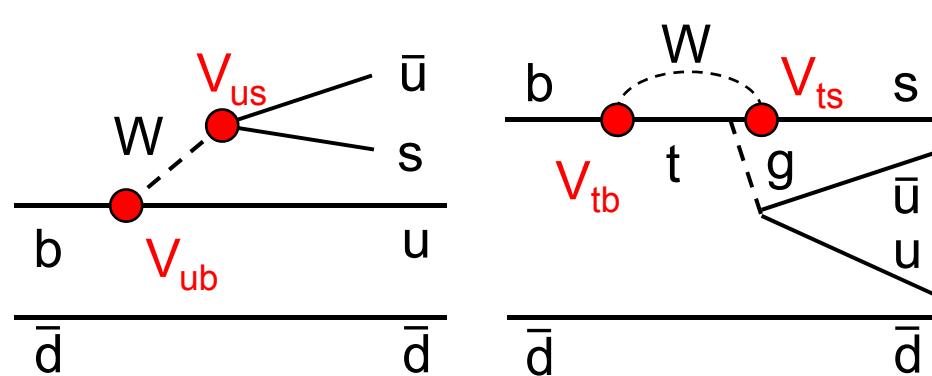


230 M  $B\bar{B}$ , 1600  $K\pi$  Decays.  $N(K^+) > N(K^-)$

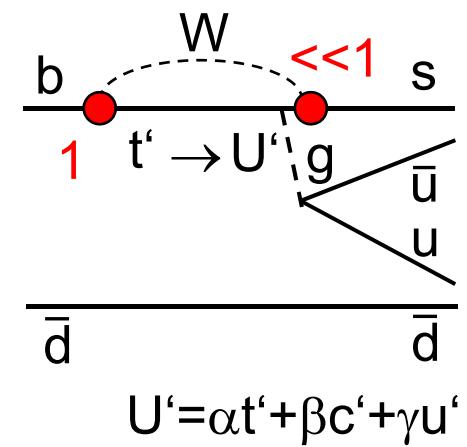
$$(N^+ - N^-)/(N^+ + N^-) = 0.13 \text{ with } 4.2 \sigma \text{ from 0}$$

First CPV Observation without any Time Info.

Explanation: CPV is an interference<sup>\*)</sup> of two decay contributions; here



A slightly different view on the 2nd graph:



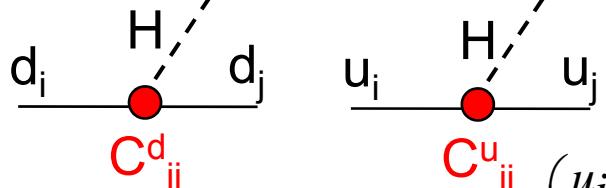
**\*) in the Standard Model**



# Quark Mixing in the St. Model

Quarks (d, s, b) (u, c, t) couple to both W and H fields.

Without H, perfect symmetry between  $d_1 d_2 d_3$  and also between  $u_1 u_2 u_3$ .

Most general  
qHq couplings:  „Rotation“ in d- (u-) space  
diagonalizes  $C^d$  ( $C^u$ )

Gauge couplings  $uWd$  require doublets  $\begin{pmatrix} u_L \\ d_L \end{pmatrix}$ . Rotations rotate the doublets  
and either diagonalize  $C^d$  or  $C^u$ . The difference between the two is V:

$$\begin{pmatrix} u_L \\ d'_L \\ c_L \\ s'_L \\ t_L \\ b'_L \end{pmatrix} = V \begin{pmatrix} u'_L \\ d_L \\ c'_L \\ s_L \\ t'_L \\ b_L \end{pmatrix}$$

The 3x3 unitary matrix V has 4 parameters, e.g.  $|V_{us}|, |V_{cb}|, |V_{ub}|, \text{Im}(V_{ub}V_{ud}^*V_{cd}V_{cb}^*)$

CPT requires:  $\begin{pmatrix} \bar{u}_R \\ \bar{d}'_R \\ \bar{c}_R \\ \bar{s}'_R \\ \bar{t}_R \\ \bar{b}'_R \end{pmatrix} = V^* \begin{pmatrix} \bar{u}'_R \\ \bar{d}_R \\ \bar{c}'_R \\ \bar{s}_R \\ \bar{t}'_R \\ \bar{b}_R \end{pmatrix}$

If  $V^* \neq V$ , q mixing violates CP.  
Only at  $T \approx m_h$  q get masses.  
 $V = V_{KM} \rightarrow V_{CKM}$   
(1973, 1987)

One of the first manifestations of quark mixing was  $K^0\bar{K}^0$  mixing. But ...



# BABAR Publications on Quark Mixing

From 19 Mar 2001 to 20 Oct 2008

BABAR has published

349 Journal papers on physics results

165 in Phys. Rev. Letters

184 in Phys. Rev. D

53 of them on Quark Mixing topics (15%)

7 on  $D^0 \bar{D}^0$  Mixing

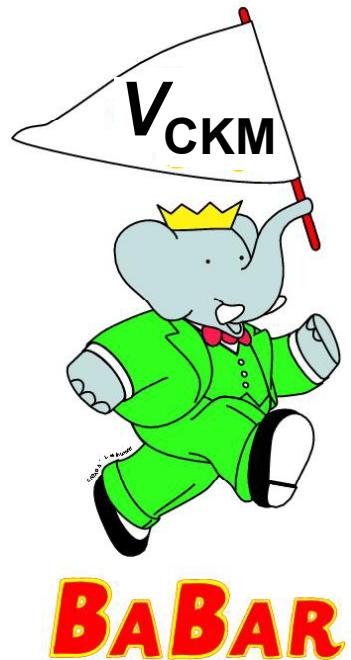
8 on  $B^0 \bar{B}^0$  Mixing

13 on  $V_{cb}$  topics

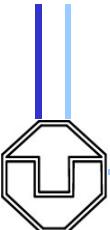
18 on  $V_{ub}$  topics

4 on  $V_{ts}$  topics

3 on  $V_{td}$  topics



Main obligations: Check „if  $V_{CKM}$  is unitary“ and determine its 4 parameters



# D<sup>0</sup>̄D<sup>0</sup> Mixing

All meson systems which are allowed to mix are now observed to mix:

K<sup>0</sup>̄K<sup>0</sup>    K<sub>S</sub><sup>0</sup> K<sub>L</sub><sup>0</sup>    1956,     $\chi = 0.498$ ,  $\Delta\Gamma$ ,  $\Delta m$

B<sup>0</sup>̄B<sup>0</sup>    B<sub>h</sub><sup>0</sup> B<sub>ℓ</sub><sup>0</sup>    1987,     $\chi = 0.19$ ,  $\Delta m$

B<sub>s</sub>̄B<sub>s</sub>    B<sub>sh</sub> B<sub>sl</sub>    2006,     $\chi = 0.499$ ,  $\Delta m$ ,  $\Delta\Gamma$  ( $\neq 0$  with  $1.5\sigma$ ),

D<sup>0</sup>̄D<sup>0</sup>    D<sub>+</sub><sup>0</sup> D<sub>-</sub><sup>0</sup>    2007,     $\chi \approx 0.7 \cdot 10^{-4}$  ( $\neq 0$  with  $9\sigma$ ),  $\Delta m$ ,  $\Delta\Gamma$  ( $\neq 0$  with  $2\sigma$ )

Common Mixing     $M_h(t) = (p M + q \bar{M}) \cdot e^{-i(m+\Delta m/2)t - (\Gamma/2 + \Delta\Gamma/4)t}$

Phenomenology:     $M_l(t) = (p M - q \bar{M}) \cdot e^{-i(m-\Delta m/2)t - (\Gamma/2 - \Delta\Gamma/4)t}$

$$x = \Delta m/\Gamma, \quad y = \Delta\Gamma/2\Gamma$$

$$\chi = (x^2 + y^2)/(2 + 2x^2)$$

$|q/p| \approx 1$  in all four systems



All four  $M_h$  and  $M_l$  are  $\approx$  CP eigenstates

Three independent pairs of properties:

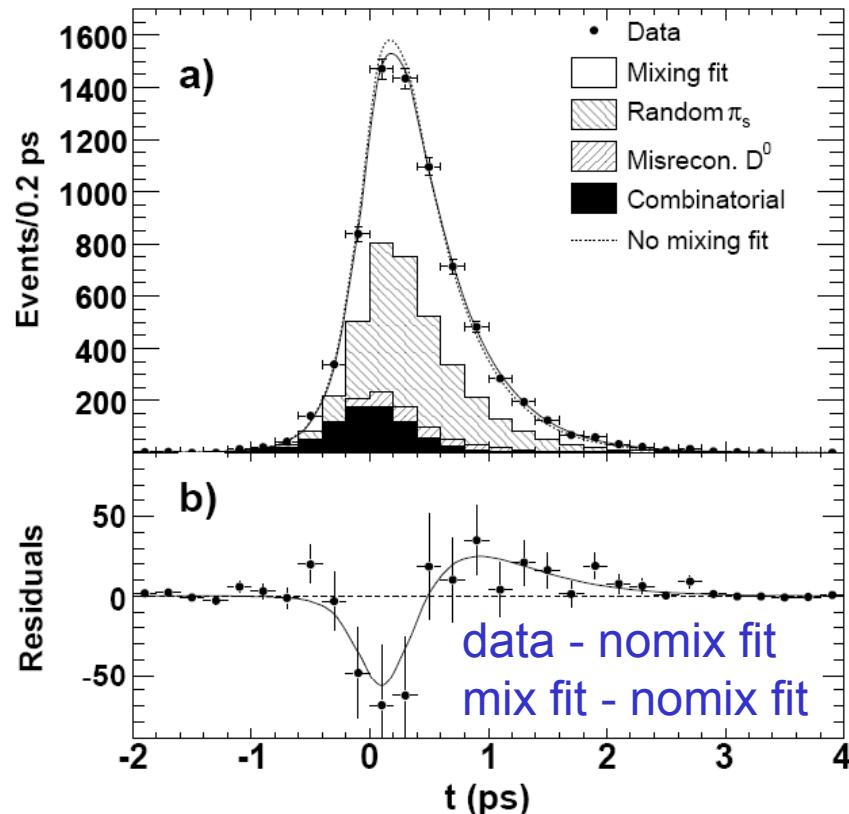
heavy & light  
Long- & Shortliving  
CP = +1 & CP = -1

K<sup>0</sup>    L = - = h  
B<sub>s</sub>    L = - ( $1.5\sigma$ ) = ?  
D<sup>0</sup>    L = - ( $4\sigma$ ) = ℓ ( $2\sigma$ )  
B<sup>0</sup>    L = ? = ?



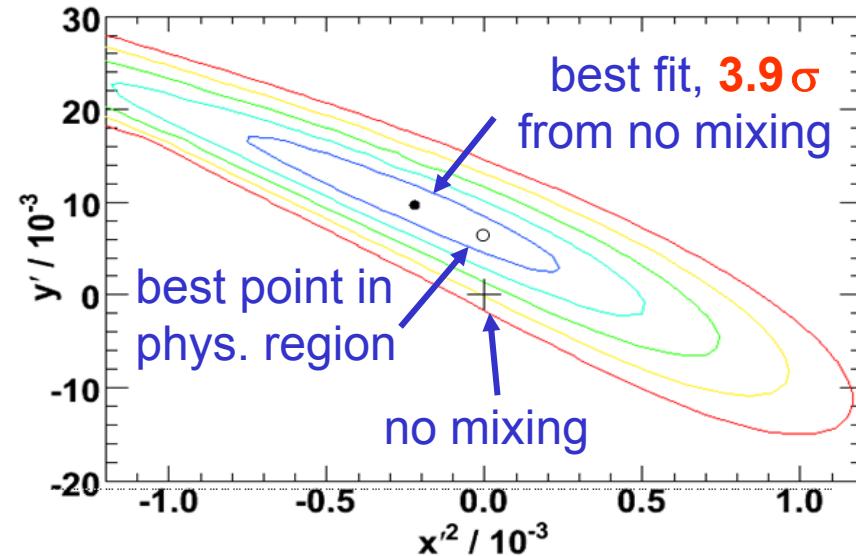
# $D^0 \bar{D}^0$ Mixing: $y'$ and $x^2 + y^2$ in $D^0 \rightarrow \bar{D}^0 \rightarrow K^+ \pi^-$

$$N_{K^+\pi^-}(t) = N_{K^-\pi^+}(0) e^{-\Gamma t} \left[ R_D + \sqrt{R_D} y' \Gamma t + \frac{x'^2 + y'^2}{4} (\Gamma t)^2 \right] \begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos \delta & \sin \delta \\ -\sin \delta & \cos \delta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

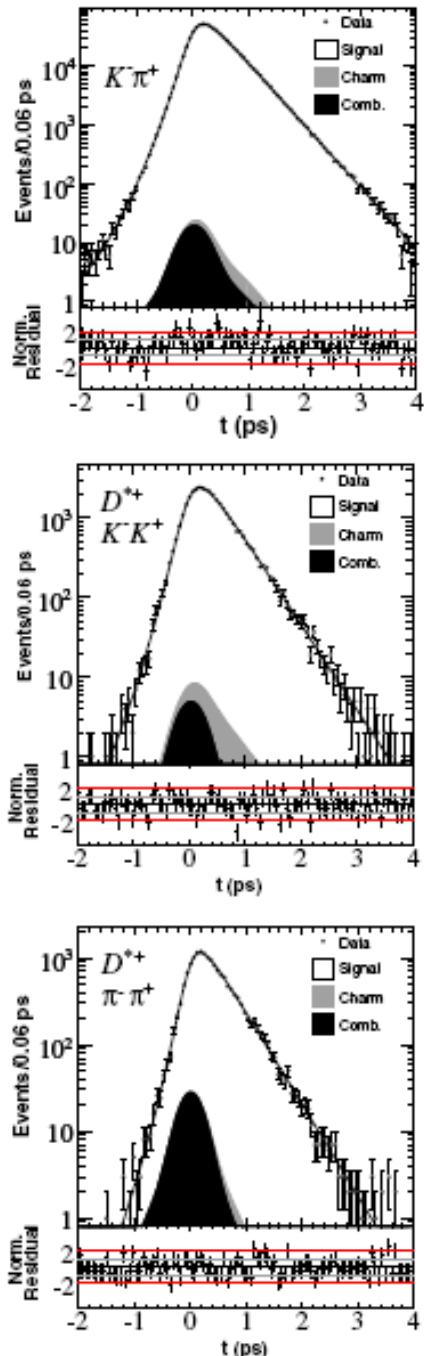
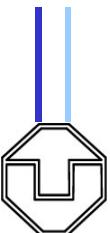


PRL 98(2007)211802 384/fb

$$\begin{aligned} R_D &: (3.03 \pm 0.16 \pm 0.10) \times 10^{-3} \\ x'^2 &: (-0.22 \pm 0.30 \pm 0.21) \times 10^{-3} \\ y' &: (9.7 \pm 4.4 \pm 3.1) \times 10^{-3} \end{aligned}$$



CDF PRL 100(2008)121802 1.5/fb  $x'^2 = (-0.12 \pm 0.35)10^{-3}$ ,  $y' = (8.5 \pm 7.6)10^{-3}$ ,  $3.8\sigma$



## $D^0 \bar{D}^0$ Mixing: $y$ in $\tau(KK, \pi\pi, K\pi)$

PRD 78(2008)011105(R) 384/fb



$e^+e^- \rightarrow D^{*+}X, D^{*+} \rightarrow D^0\pi^+, D^0 \rightarrow K^-\bar{K}^+, \pi^-\pi^+, K^-\pi^+$

$$\frac{1}{\tau(KK)} = \frac{1}{\tau(\pi\pi)} = \frac{1+y}{\tau(K\pi)} \quad y = (1.24 \pm 0.39 \pm 0.13) \cdot 10^{-2}$$

$3\sigma$



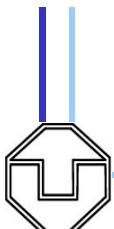
PRL 98(2007)211808

540/fb

$$y = (1.31 \pm 0.32 \pm 0.25) \cdot 10^{-2} \quad 3.2\sigma$$

HFAG Aug/08 average (together with others):

$$(1.07 \pm 0.26) \cdot 10^{-2} \quad 4.2\sigma$$



## $x^2 + y^2$ in $D^0 \rightarrow \bar{D}^0 \rightarrow K^+ \ell^- \bar{\nu}$ , $K^+ \pi^- \pi^0$ , $K^+ \pi^- \pi^+ \pi^-$



$K^+ \ell^- \bar{\nu}$   $\chi = (x^2 + y^2)/2 = (0.4^{+7}_{-6}) 10^{-4}$   $344/\text{fb}$  PRD 76(2007)014018



$K^+ \ell^- \bar{\nu}$   $(1.3 \pm 2.2 \pm 2.0) 10^{-4}$   $492/\text{fb}$  PRD 77(2008)112003



$K^+ \pi^- \pi^0$   $3.2 \times 10^{-4}$  with  $3.2\sigma$   $384/\text{fb}$  arXiv:0807.4544 → PRL



$K^+ \pi^- \pi^+ \pi^-$   $(1.9 \pm 1.6) 10^{-4}$   $230/\text{fb}$  hep-ex/0607090(2006)

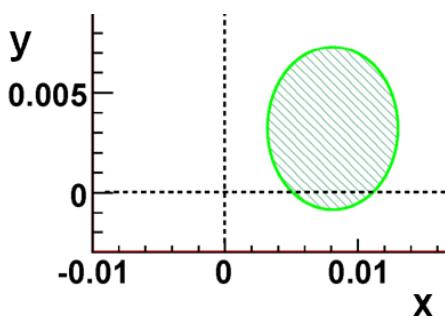
## $x$ and $y$ from $D^0 \rightarrow K_s^0 \pi^+ \pi^-$ Dalitz Plot Analysis



$$x = (0.80 \pm 0.29 \pm {}^{0.13}_{0.16}) 10^{-2}$$

$$y = (0.33 \pm 0.24 \pm {}^{0.10}_{0.14}) 10^{-2}$$

$2\sigma$  from no mixing



$540/\text{fb}$

PRL 99(2007)131803

# $D^0 \bar{D}^0$ Mixing: Summary



$D^0(t) \rightarrow K^+ \pi^-$

$\Rightarrow (y', x'^2) \neq (0,0)$  with  $4\sigma$



$\tau(K^+K^-, \pi^+\pi^-)/\tau(K^-\pi^+)$

$\Rightarrow y \neq 0$  with  $3.2$  and  $3\sigma$



$D^0(t) \rightarrow K^0_S \pi^+ \pi^-$  Dalitz Plot

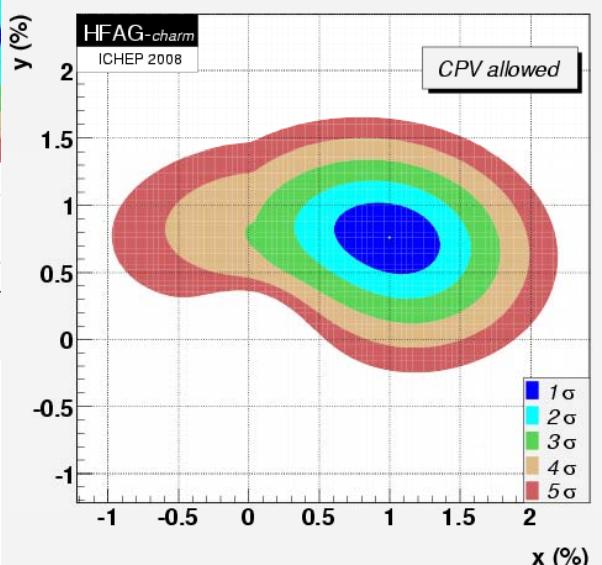
$\Rightarrow (x,y) \neq (0,0)$  with  $2\sigma$

HFAG average August 2008:

$$x = (10.1 \pm 2.4) 10^{-3}, y = (7.3 \pm 1.8) 10^{-3}$$

$$\Rightarrow \chi = (x^2 + y^2)/2 = (0.77 \pm 0.25) 10^{-4}$$

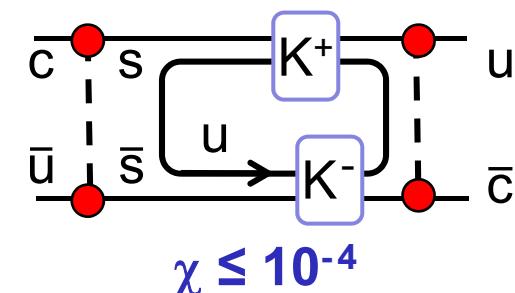
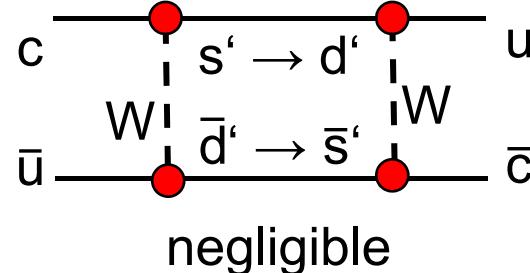
of all produced  $D^0$  decay as  $\bar{D}^0$ ,  $\chi \neq 0$  with  $9.8\sigma$ .



No CPV( $D^0$ ) observed.

St. Model

Expectation:





# $B^0 \bar{B}^0$ Mixing

PDG 2008 uses 3 BABAR results on  $\Delta m$ :

2002 21/fb  $\ell^\pm - \ell^\pm$ ,  $A = (N^{+-} - N^{\pm\pm}) / (N^{+-} + N^{\pm\pm})$

2002 30/fb  $B^0$ (full.rec) - CPtag,

2006 81/fb  $B^0 \rightarrow D^* \ell \nu$ (part.rec) -  $\ell^\pm$

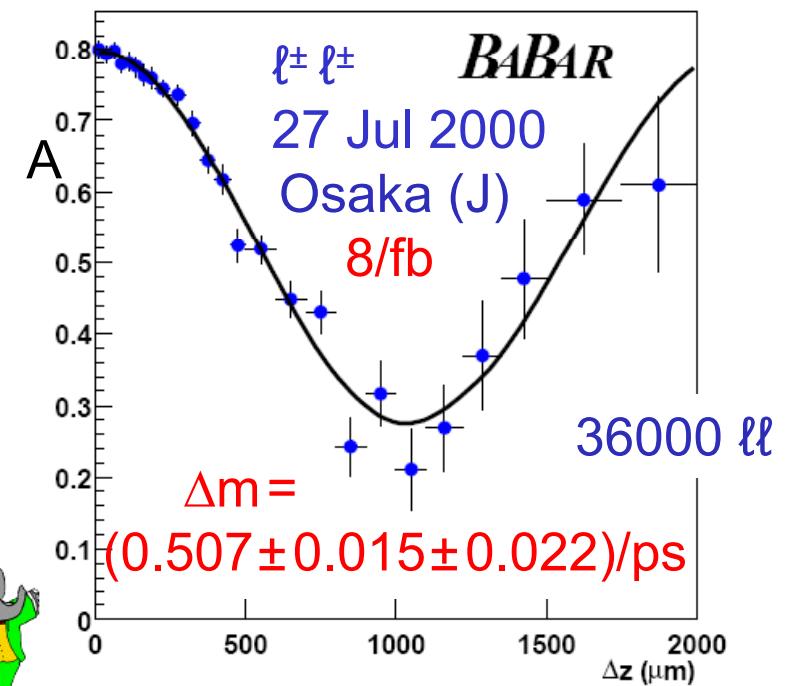
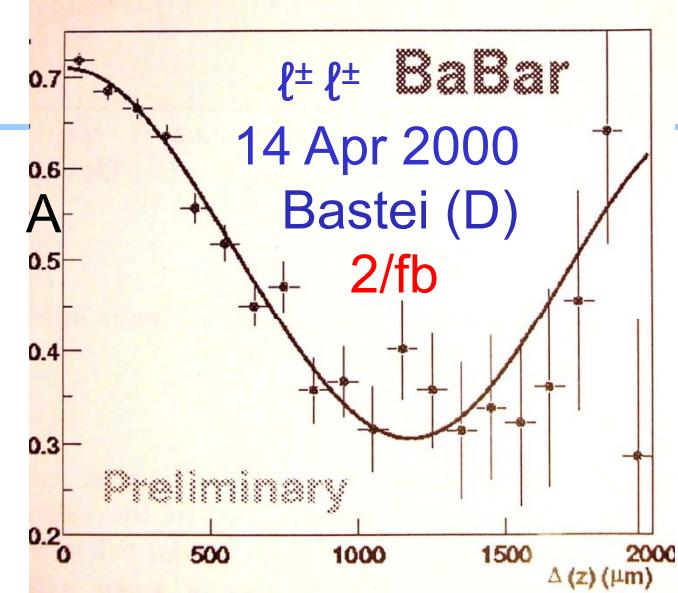
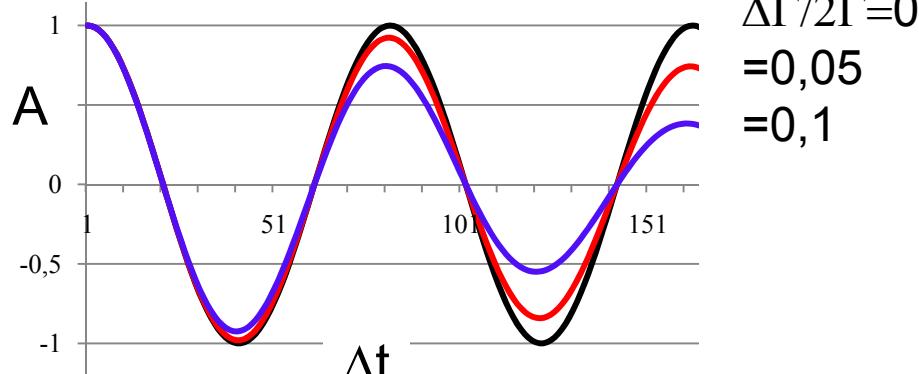
PRD 73(2006)012004



Present PDG Mean  $\Delta m = (0.507 \pm 0.005)/\text{ps}$

dominated by BABAR 06 + BELLE 05

$B^0$ (full.rec) - CPtag:

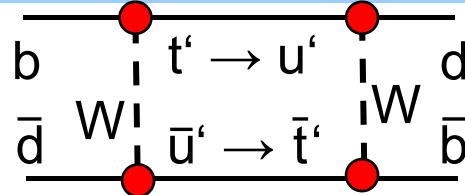




# $B^0 \bar{B}^0$ Mixing; CP, T and CPT

St. Model

Expectation:



$$\Delta m = \frac{G_F^2 m_B f_B^2 B_B \eta_B}{6\pi^2} |V_{td}|^2 |V_{tb}|^2 f(m_t^2, m_W^2)$$

$$\text{LQCD 2007: } f_B^2 B_B = (223 \pm 8 \pm 16)^2 \text{ MeV}^2$$

$$|V_{tb} V_{td}| = (8.1 \pm 0.6) 10^{-3}$$

$$\Delta\Gamma/2\Gamma \approx 2 \cdot 10^{-3}, \quad \left| \frac{q}{p} \right| - 1 = o(10^{-3})$$

## Search for CP and T Violation in Mixing:

[PRL 96(2006)251802]

$\frac{N^{++} - N^{--}}{N^{++} + N^{--}}$  in dilepton events measures the CP- and  
 $\frac{N^{++} - N^{--}}{N^{++} + N^{--}}$  T-violating asymmetry  $\bar{B}^0 \rightarrow B^0 / B^0 \rightarrow \bar{B}^0$

211/fb



$|q/p| - 1 = (-0.8 \pm 2.7 \pm 1.9) 10^{-3}$ , PDG 08:  $(1.8 \pm 1.8) 10^{-3}$  with D0 & Belle 2006

## CPT Test in $B^0 \bar{B}^0$ Mixing:

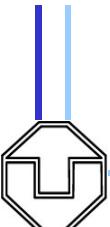
same paper

$$\frac{N^{+-}(\Delta t > 0) - N^{+-}(\Delta t < 0)}{N^{+-}(\Delta t > 0) + N^{+-}(\Delta t < 0)}$$

measures the CPT-violating asymmetry  $B^0 \rightarrow B^0 / \bar{B}^0 \rightarrow \bar{B}^0$ . Results:

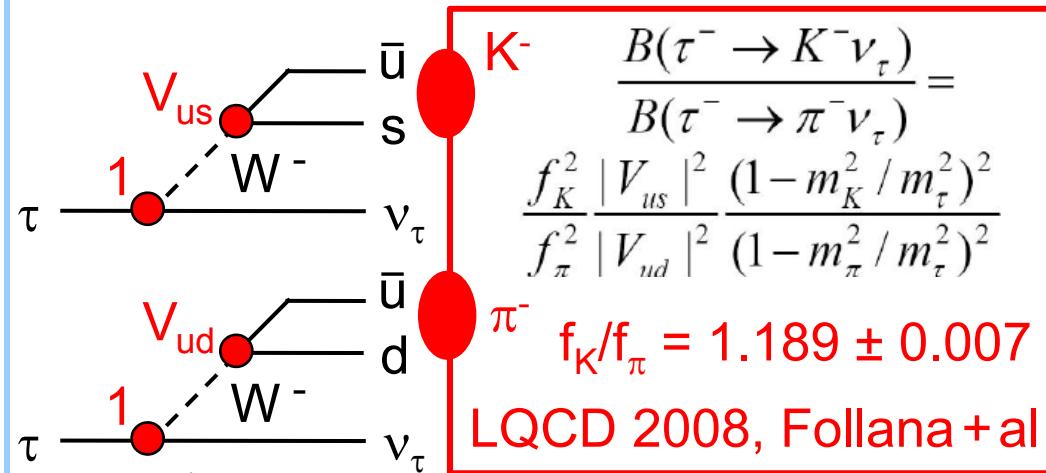
$$\delta = -\frac{z}{2} = -\frac{\delta m}{\Delta m} + i \frac{\delta \Gamma}{2\Delta m} = \frac{(3.5 \pm 1.9 \pm 1.0) \cdot 10^{-3}}{\text{ps} \cdot \Delta \Gamma} + i(7.0 \pm 3.6 \pm 1.6) \cdot 10^{-3}$$

{ $\delta$  from Charpak & Gourdin 1967}



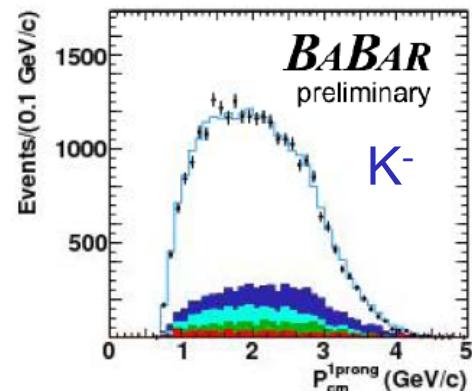
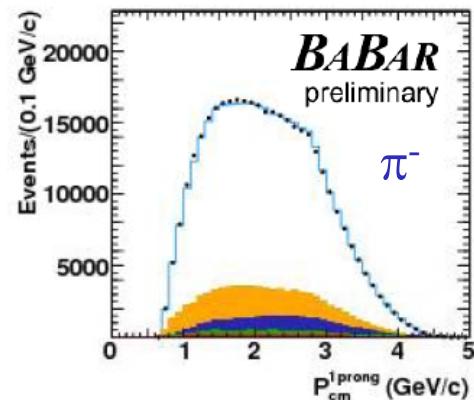
**V<sub>us</sub>**

Contributions from our 580 M  $\tau$ -lepton pairs; exclusively and inclusively



I. Nugent @ TAU 08

467/fb



$$\Gamma(\tau \rightarrow K\nu)/\Gamma(\tau \rightarrow \pi\nu) = (6.53 \pm 0.06 \pm 0.09) 10^{-2}$$

27 Oct 2008

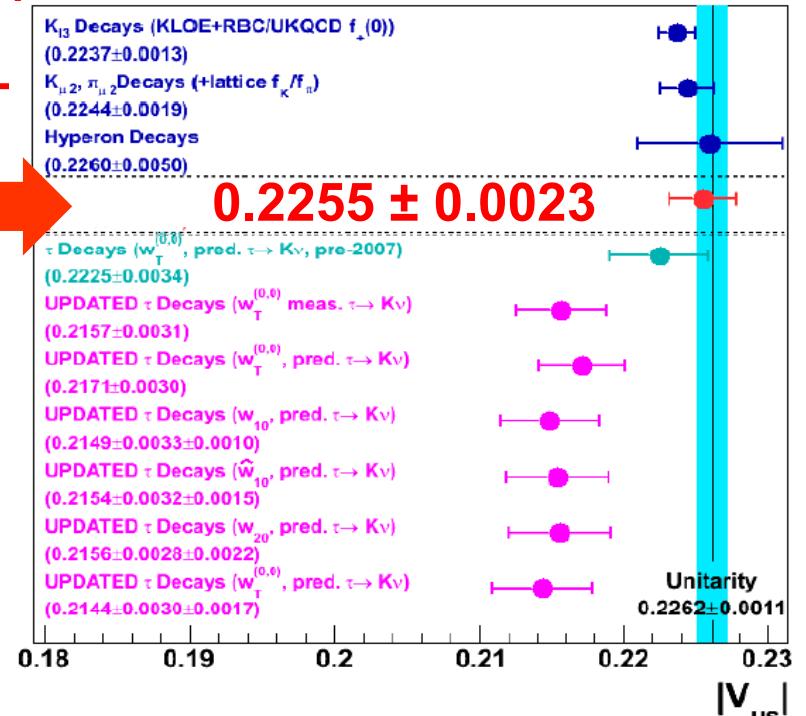
K. R. Schubert (TU Dresden), B-Factory Symposium at SLAC

1or 3 K+X

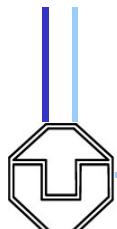
$$\frac{\Gamma_{S\bar{u}}}{\Gamma_{d\bar{u}}} + \delta(m_s) = \frac{|V_{us}|^2}{|V_{ud}|^2}$$

0or2 K+X

$\delta$  from Gamiz + al 2005 + ...



12



$V_{cb}$

$W$

$b \quad t'$

$t' = V_{tb} t + V_{cb} c + V_{ub} u$ , coherent at time of  $W$  emission,  
decoherent at time of meson formation:

$$\Gamma(B \rightarrow c+X) \sim |V_{cb}|^2, \Gamma(B \rightarrow t+X) = 0, \Gamma(B \rightarrow u+X) \sim |V_{ub}|^2$$

Rate measurements allow determination of  $|V_{cb}|$ ,

Smallest influence of the strong interaction:

Best-studied reconstructed mode:  $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}$

$BF \sim 5\%$ , str.int.contr.  $\sim 10\%$  if  $d\Gamma/dq^2$  at  $q^2_{\max}$ :



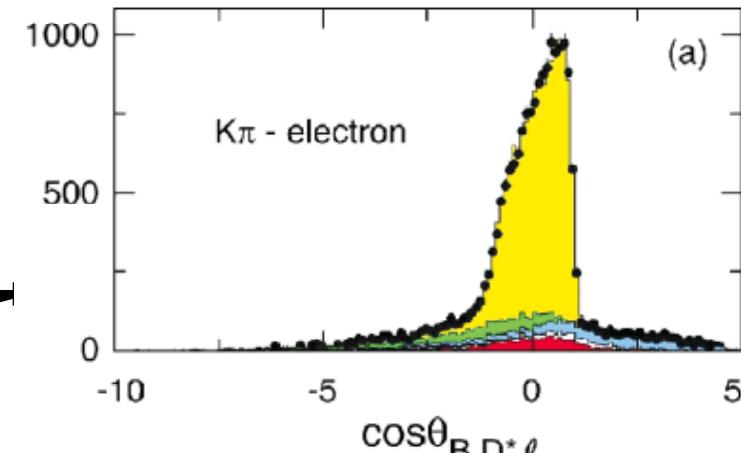
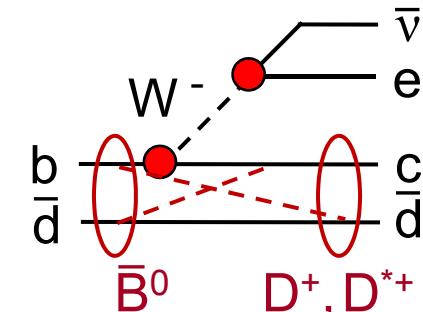
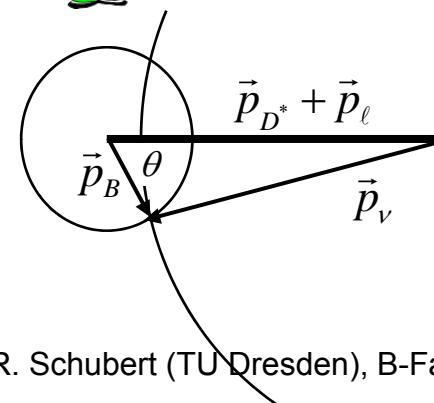
Latest result:

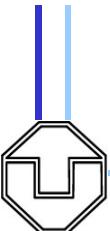
PRD 77(2008)032002



79/fb

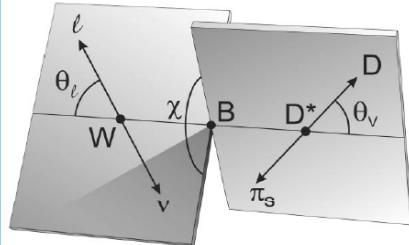
„Full“ reconstruction  
of the decay with  
 $D^{*+} \rightarrow (K^-\pi^+)_D \pi^+$  slow  
and  $\cos\Theta_{B,D^*\ell}$



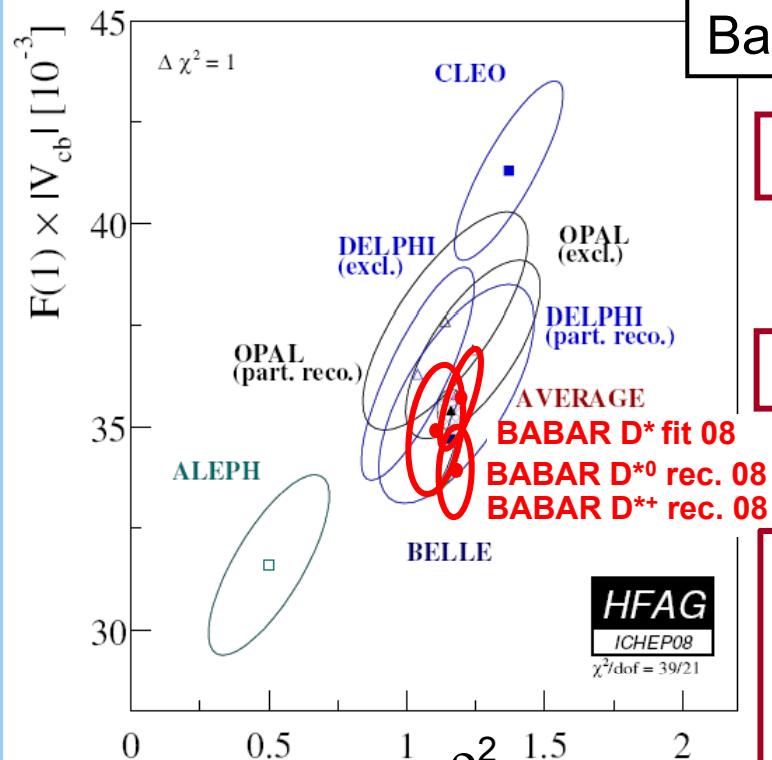
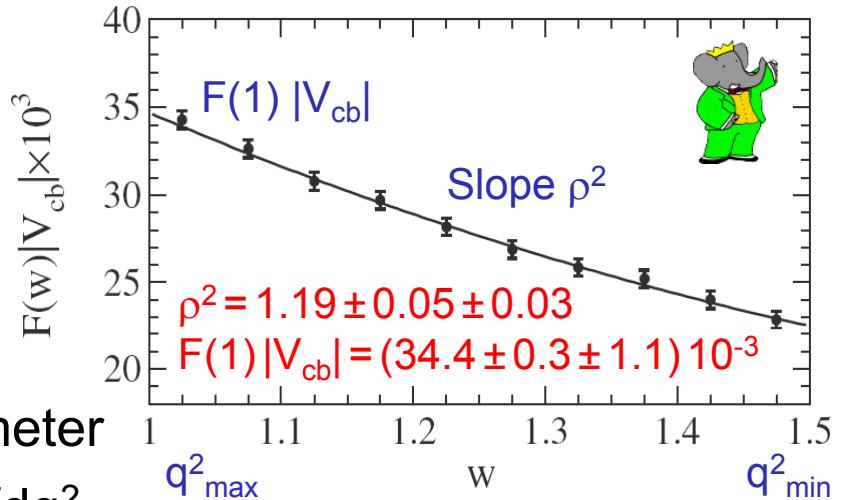


## $V_{cb}$ continued

Full information on  $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}$  is in  
the rate  $d^4\Gamma/dq^2 d\chi d\cos\Theta_\ell d\cos\Theta_V$ .



Integration over the  
angles with fitted parameter  
values  $R_1, R_2$  gives  $d\Gamma/dq^2$



Bad agreement  $\Rightarrow$  Look for new approaches:

PRL 100(2008)231803  $B^- \rightarrow D^{*0} \ell^- \bar{\nu}$  205/fb

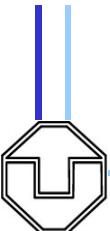
$D^{*0} \rightarrow (K^- \pi^+)_D \pi^0$  slow  $\rho^2 = 1.16 \pm 0.06 \pm 0.08$   
 $F(1)|V_{cb}| = (35.9 \pm 0.6 \pm 1.4) 10^{-3}$

arXiv:0809.0828  $B \rightarrow (D^0, D^\pm) \ell^- \bar{\nu}$  207/fb  
 $\rho^2 = 1.21 \pm 0.02 \pm 0.07$   
 $F(1)|V_{cb}| = (35.7 \pm 0.2 \pm 1.2) 10^{-3}$

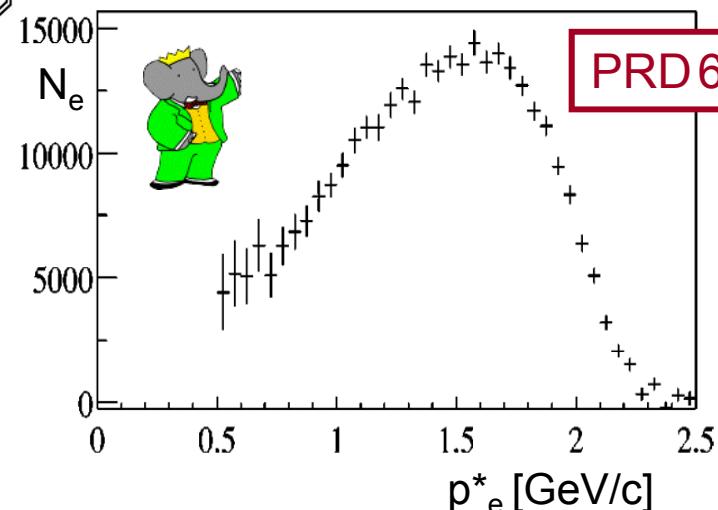
HFAG + LQCD:  $|V_{cb}|_{D^*} = (38.5 \pm 0.7 \pm 1.0) 10^{-3}$

HFAG + LQCD:  $|V_{cb}|_D = (39.2 \pm 1.6 \pm 0.9) 10^{-3}$

My average:  $|V_{cb}|_{\text{excl}} = (38.6 \pm 0.6 \pm 1.0) 10^{-3}$



## $V_{cb}$ (inclusive)



47/fb Momentum spectrum  
of electrons in  $B\bar{B} \rightarrow e^+\nu X e^-\bar{\nu} X$  events  
 $\Rightarrow BF(B \rightarrow e^+\nu X, E_e > 0.6 \text{ GeV}/c)$   
 $= (10.36 \pm 0.06 \pm 0.23)\%, 0.98 X_c + 0.02 X_u$

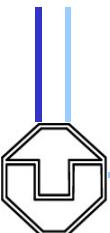
$$\Gamma(B \rightarrow e^+\nu X_c, E_e > E_{\min}) = |V_{cb}|^2 \cdot f_{HQE}(E_{\min}; m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3)$$

HQE = effective QCD with expansion in  $\Lambda_{\text{QCD}}/m_b$

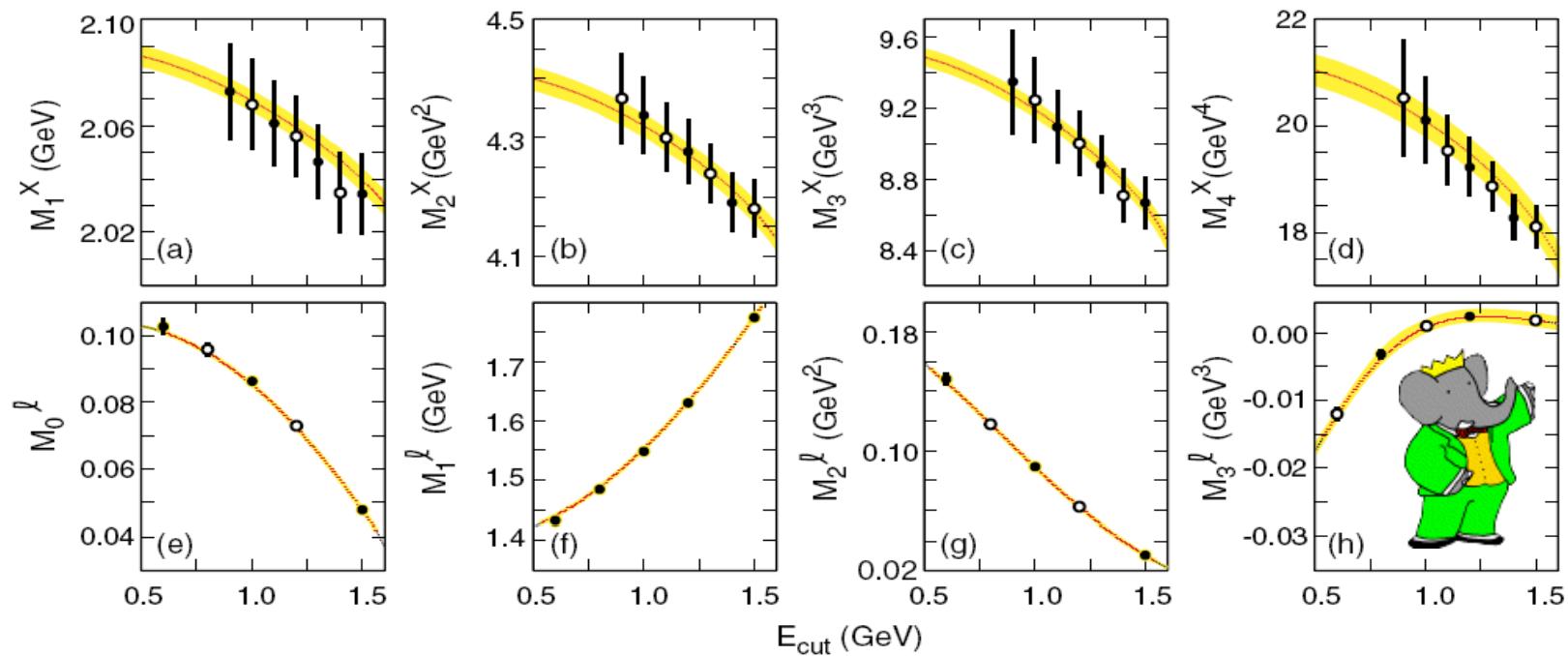
The shape of the spectrum, with more precision its moments  $\langle E_e^k \rangle$ ,  $k=1,2,3$  for 5 different  $E_{\min}$ , determine the parameters  $m_b \dots \rho_{LS}^3$  and therewith  $|V_{cb}|$  and the extrapolated  $BF$  for  $E_{\min}=0$ . The HQE fit in the „kinetic scheme“ in  
 PRL 93(2004)011803 includes moments  $\langle m_X^k \rangle$ ,  $k=1\dots 4$  of the mass spectrum of the  $X_c$  system for 8 different  $E_{\min}$ . The 2004 BABAR+HQE fit finds

$$|V_{cb}|_{\text{incl}} = (41.4 \pm 0.4 \pm 0.7) 10^{-3}.$$

The credibility is demonstrated by the quality of the overconstraining fit:



## more $V_{cb}$ inclusive



$$|V_{cb}|_{\text{incl}} \text{ (BABAR 2004)} = (41.4 \pm 0.4 \pm 0.7) 10^{-3}$$

$$|V_{cb}|_{\text{incl}} \text{ (HFAG 2008)} = (41.7 \pm 0.4 \pm 0.6) 10^{-3} \quad \text{incl. CLEO, BELLE, DELPHI}$$

and moments from  $B \rightarrow X_s \gamma$

$$|V_{cb}|_{\text{excl}} \text{ (HFAG+LQCD)} = (38.6 \pm 0.6 \pm 1.0) 10^{-3}$$

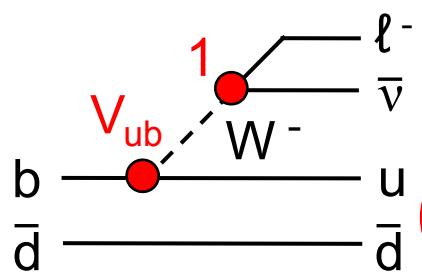
Inclusive  $\pm 1.7\%$ , exclusive  $\pm 3.0\%$ . Tension between the two is  $2.3 \sigma$ .



# $V_{ub}$

Since 1990 (ARGUS, CLEO)  $|V_{ub}/V_{cb}| \approx 0.1$ , i.e.  $N(B \rightarrow u+X)/N(B \rightarrow c+X) \approx 0.02$ ,  
 Rate measurements for determinations of  $|V_{ub}|$  have  $bg/\text{signal} \approx 50$ .

Cleanest ways: **exclusive** and **inclusive** semileptonic decays



3 papers on  $\pi l \nu$ :

$$\frac{d\Gamma}{dq^2} = |V_{ub}|^2 \frac{G_F^2 p_\pi^3}{24\pi^3} |f_+(q^2)|^2$$

$f_+(q^2)$  from LQCD  
for large  $q^2$   
from LCSR for small  $q^2$

Integrate  $\frac{d^3\Gamma(B \rightarrow X_u l \nu)}{dp_\ell dq^2 dm_X^2}$   
over optimized regions of  
the lepton momentum,  
 $q^2(l\bar{\nu})$ , and the mass of  $X_u$

PRL 98(2007)091801



206/fb

$\pi^+ l \nu$  untagged, i.e.  $B\bar{B} \rightarrow X + \pi^+ l \nu$

$BF = 1.46 \cdot 10^{-4} \pm 11\%$ ,  $|V_{ub}| = 3.8 \cdot 10^{-3} \pm 15\%$

PRL 97(2006)211801



211/fb

tagged,  $B\bar{B} \rightarrow (D^{(*)} l \nu \text{ or had.rec}) + (\pi^+, \pi^0) l \nu$

$BF = 1.33 \cdot 10^{-4} \pm 15\%$ ,  $|V_{ub}| = 3.6 \cdot 10^{-3} \pm 15\%$

newest  
paper:

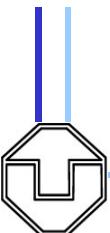
PRL 101(2008)081801



348/fb

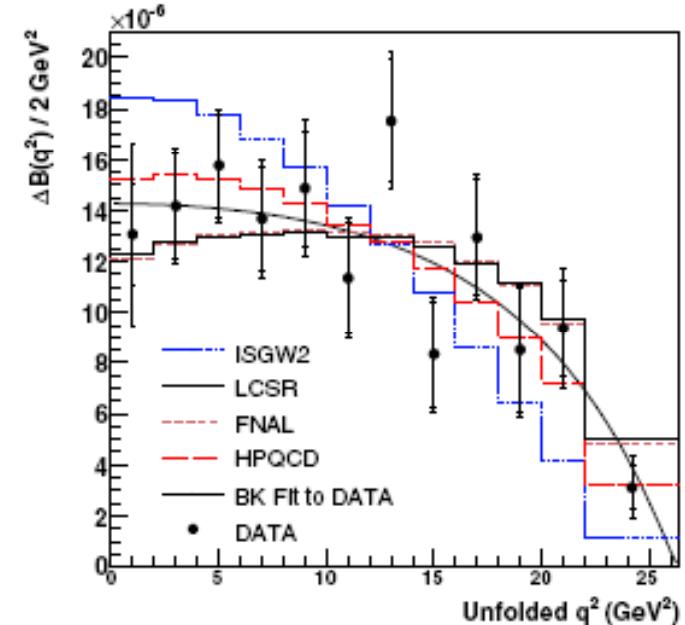
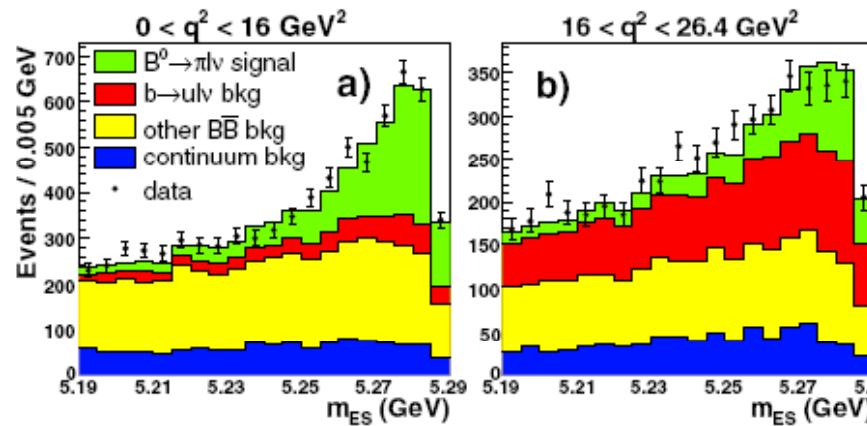
$(\pi^+, \pi^0) l \nu$  tagged with  $D^{(*)} l \nu$

$BF \pm 12\%$ ,  $|V_{ub}| = 3.6 \cdot 10^{-3} \pm 15\%$



## $V_{ub}$ (2)

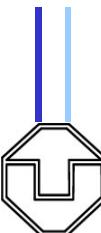
from the  
un-tagged  
 $\pi^+ \ell^- \nu$   
analysis:



## Inclusive $|V_{ub}|$ Measurements

I choose 3 BABAR analyses.  $|V_{ub}|$  extraction is done with very refined HQE methods. Expansion converges poorly in the limited  $p_\ell q^2 m_X$  bg-minimizing regions. Non-perturbative „shape functions“ needed; leading parameters now taken from HQE( $B \rightarrow X_c \ell \bar{\nu}$ ) results.

- Cut on  $p_\ell$  only
- Cut on  $p_\ell$  and  $q^2$
- Cuts on  $m_X$ ;  $m_X$  and  $q^2$ ;  $P^+ = E_X - p_X$



# $V_{ub}$ inclusive



First:  $p_\ell$  only,  $p_e > 2.0 \text{ GeV}/c$ ,  $f_u = 0.25$

PRD 73(2006)012006 (80+10)/fb

$D\ell\bar{\nu}$  and  $D^*\ell\bar{\nu}$  modeled, continuum from data,  $p_{\text{miss}} > 0.5 \text{ GeV}/c \Rightarrow \Delta BF(p_e > 2.0)$ ,

$|V_{ub}|(\text{BLNP, HFAG-08}) = 4.3 \cdot 10^{-3} \pm 9\%$ , stable with  $p_e$  cut variations.

2nd:  $p_\ell$  and  $q^2$  PRL 95(2005)111801 (81+10)/fb  $p_e > 2.1 \text{ GeV}/c$  and

$s_h^{\max}(p_e, q^2) < m_D^2$  with  $p_\nu = 0.8 p_{\text{miss}}$   $-0.08$  if  $0 < E_{\text{miss}} - p_{\text{miss}} < 0.8 \text{ GeV}/c \Rightarrow$

$|V_{ub}|(\text{BLNP, HFAG}) = 4.4 \cdot 10^{-3} \pm 11\%$

3rd:  $m_X$ ,  $q^2$  and  $E_X - p_X$  347/fb

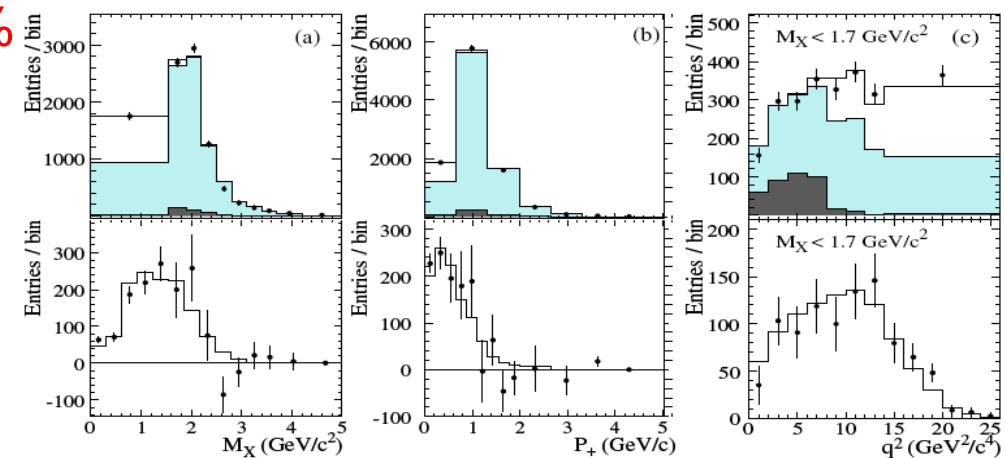
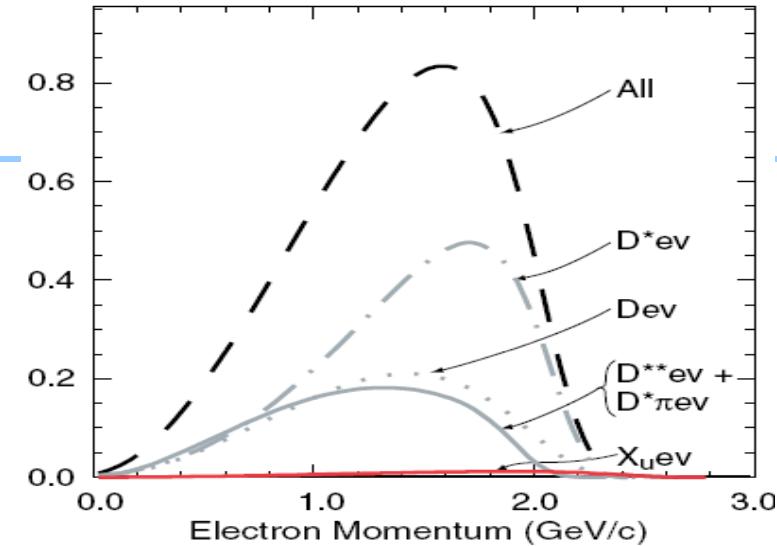
PRL 100(2008)171802

$B\bar{B} \rightarrow B_{\text{reco}} (\eta = 0.4\%) + X_u \ell\bar{\nu}$

$p_\ell > 1 \text{ GeV}/c$ ,  $D^*\ell\bar{\nu}$  veto, K veto

3 regions:  $m_X < 1.55$ ;  $E_X - p_X < 0.66$ ;

$M_X < 1.7 \text{ GeV}$  and  $q^2 > 8 \text{ GeV}^2$ .  $10^3 V_{ub}(\text{BLNP}) = 4.1 \pm 9\%$ ,  $4.4 \pm 10\%$ ,  $3.8 \pm 10\%$





## $V_{ub}$ and $V_{cb}$ Summary

HFAG averages all incl.  $V_{ub}$  results separately for BNLP, DGE, GGOU, ADFR.

Errors  $\pm 7\%$ , spread  $\pm 5\%$

$$\Rightarrow |V_{ub}|_{\text{incl}} = 4.1 \cdot 10^{-3} \pm 9\%$$

From  $B \rightarrow \pi \ell \nu$

$$|V_{ub}|_{\text{excl}} = 3.6 \cdot 10^{-3} \pm 15\% \quad \Delta < 1\sigma$$

BABAR & BELLE 2000 → 2008:

$$\sigma(|V_{ub}|) \pm 30\% \rightarrow \pm 9\%$$

Recalling  $|V_{cb}|$ :

$$|V_{cb}|_{\text{excl}} = 38.6 \cdot 10^{-3} \pm 3.0\%$$

With  $|V_{ub}|$ ,  $|V_{cd}|$ ,

$$|V_{cb}|_{\text{incl}} = 41.7 \cdot 10^{-3} \pm 1.7\% \quad \Delta = 2.3\sigma$$

$|V_{us}|$  (mainly  $K\ell 3$ , but  $\tau$  is coming),

$$\sigma(|V_{cb}|) \pm 5\% \rightarrow \pm 2\%$$

and  $|V_{td}|$  ( $\Delta m$  of  $B^0, B_s$ ),

the unitarity of the CKM matrix

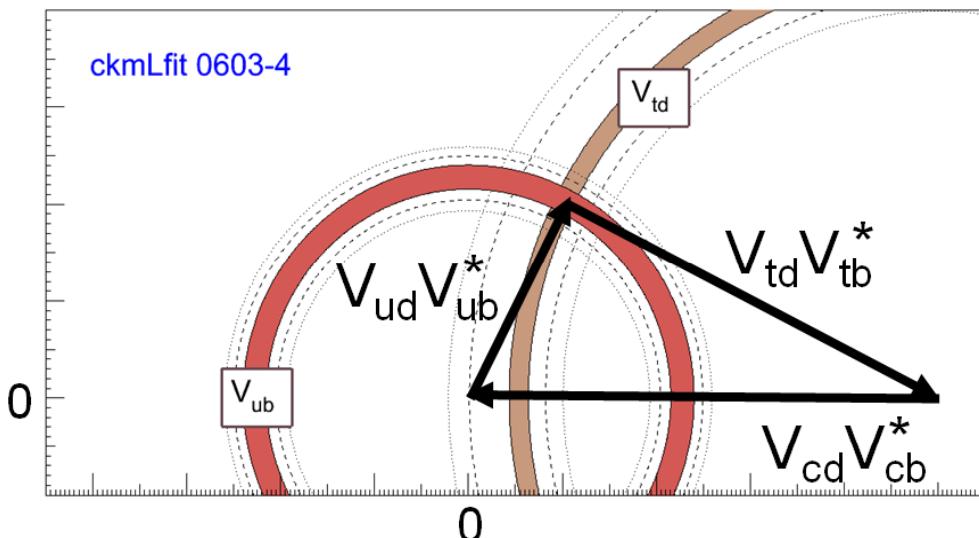
shows that CP is violated:

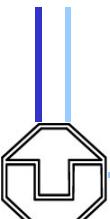
Conclusion from only

CP-symmetric observations.

[two solutions; CPV ( $\varepsilon_K, \beta, \gamma$ )

shows  $\text{Im}(V_{ud}V_{ub}^*V_{cb}V_{cd}^*) > 0.$ ]





# $V_{ts}$ in Decays

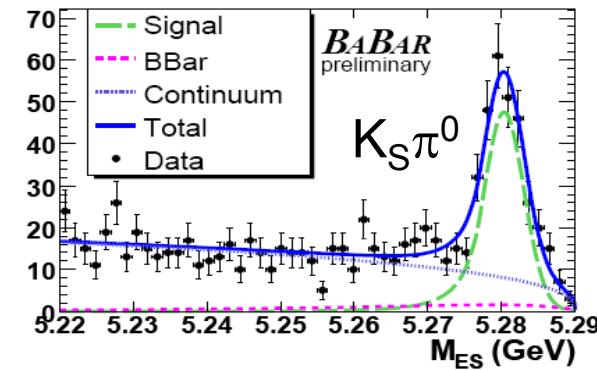
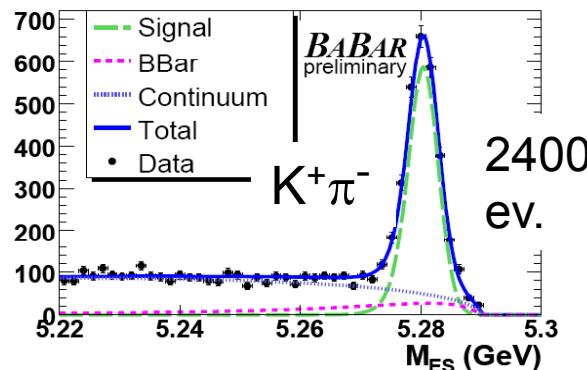
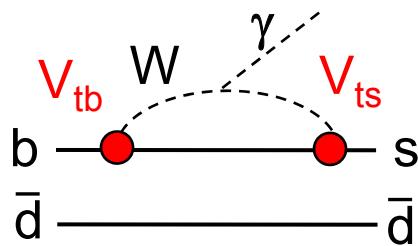
$$B^0 \rightarrow K^{*0} \gamma$$

arXiv:0808.1915



347/fb

Modes  $K^+\pi^-$ ,  $K_S\pi^0$ ,  $K^+\pi^0$ ,  $K_S\pi^+$



$$\mathcal{B}(B^0 \rightarrow K^{*0}\gamma) = (4.58 \pm 0.10 \pm 0.16) \times 10^{-5} \quad \mathcal{B}(B^+ \rightarrow K^{*+}\gamma) = (4.73 \pm 0.15 \pm 0.17) \times 10^{-5}$$

Precision of formfactor calculation not sufficient for  $|V_{tb}| |V_{ts}|$ , this may change!

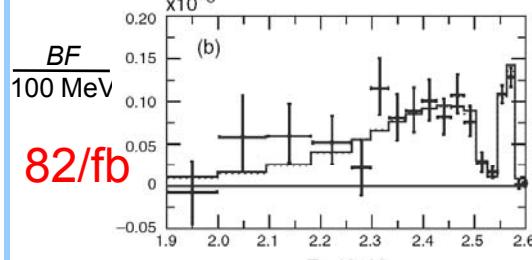
$$b \rightarrow s \gamma$$

$|V_{ts}|$  not goal of the 3



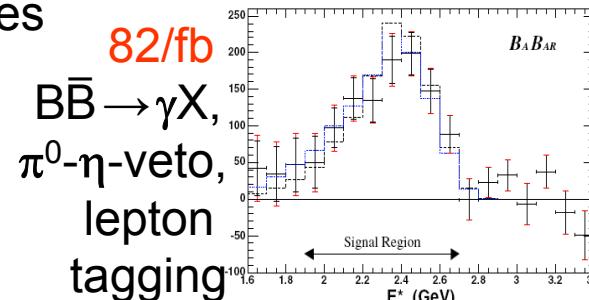
PRD 72(2005)052004

$\Sigma$  of 4  $K^*$  + 34 other modes



27 Oct 2008

PRL 97(2006)171803



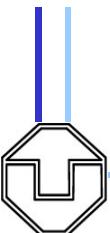
PRL 77(2008)051103

210/fb  $B_{reco}$  tags  $\Rightarrow$  smaller but cleaner event sample.  
BF compatible, but  $\sigma(BF)$  3 times larger. WA(PDG 08):

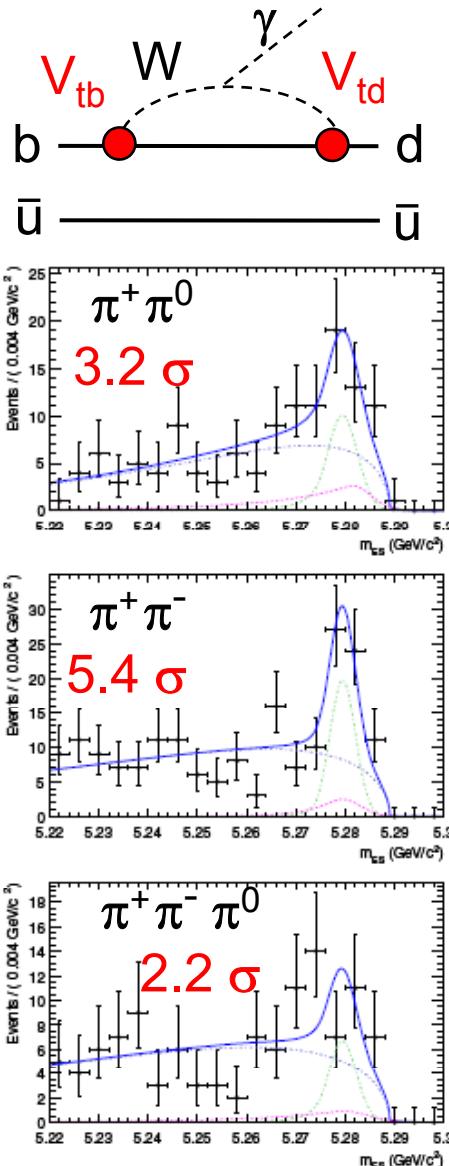
$$BF(b \rightarrow s \gamma) = (35.6 \pm 2.5) 10^{-5}$$

K. R. Schubert (TU Dresden), B-Factory Symposium at SLAC

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# $V_{td}$ in Decays



$$B^+ \rightarrow \rho^+ \gamma$$

$$B^0 \rightarrow \rho^0 \gamma$$

$$B^0 \rightarrow \omega \gamma$$

[arXiv:0808.1379](https://arxiv.org/abs/0808.1379)



$423/fb$

$$\rho^+ \rightarrow \pi^+ \pi^0$$

$$\rho^0 \rightarrow \pi^+ \pi^-$$

$$\omega \rightarrow \pi^+ \pi^- \pi^0$$

Combined significance  $6.5 \sigma$

$$BF(\text{combined}) = (1.63 \pm 0.30 \pm 0.28) 10^{-6}$$

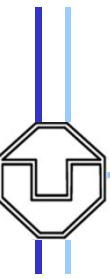
$$|V_{td}/V_{ts}| = 0.233 \pm 0.025 \pm 0.022$$

in agreement but not competitive with

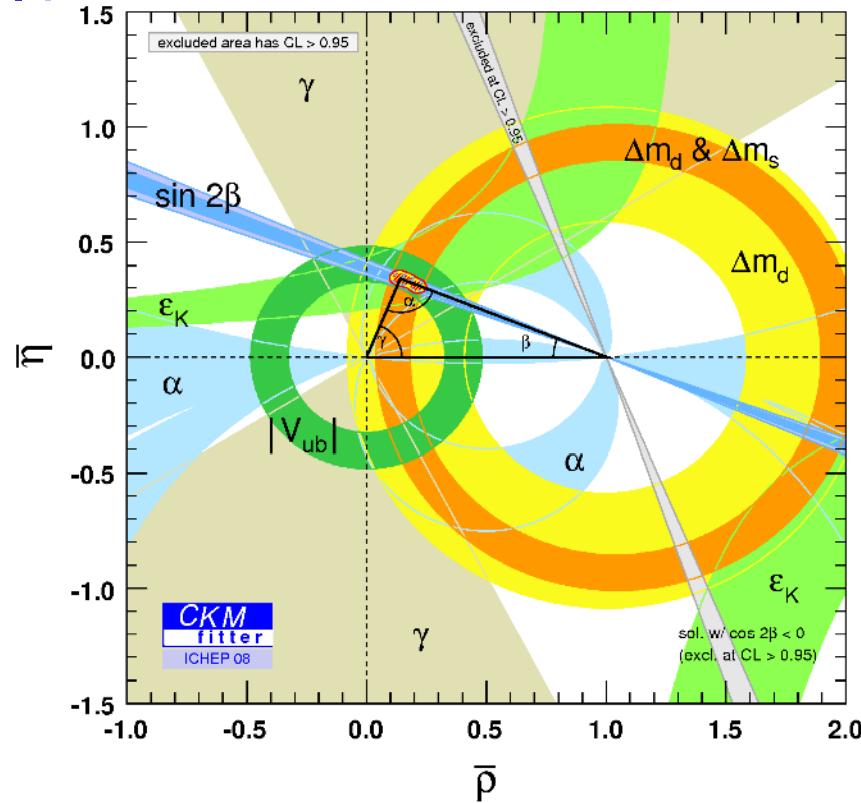
$$|V_{td}/V_{ts}| = 0.208 \pm 0.002 \pm 0.008$$

from  $\Delta m(B^0)/\Delta m(B_s)$  and LQCD.

(this topic really belongs into S. Playfer's talk)



# Summary



No deviation from the CKM description of quark mixing has been observed.

Precision of the agreement between  $|V_{us}|$ ,  $|V_{cb}|$ ,  $|V_{ub}|$ ,  $|V_{tb}V_{td}|$ ,  $|V_{td}/V_{ts}|$ , the phases of the invariant quartets  $V_{ud}V_{ub}^*V_{tb}V_{td}^*$ ,  $V_{td}V_{tb}^*V_{cb}V_{cd}^*$ ,  $V_{ud}V_{ub}^*V_{cb}V_{cd}^*$ , and  $|V_{ud}|$ ,  $|V_{cd}|$ ,  $|V_{cs}|$ ,  $|V_{ts}V_{tb}|$  is impressive.

CKMfitter 2008:  $|V_{us}| = 0.2252 \pm 0.0008$ ,  
 $|V_{cb}| = 0.0405 \pm 0.0011$   
 $|V_{ub}| = 0.0034 \pm 0.0002$ ,  
 $\text{Im}(V_{ub}V_{ud}^*V_{cd}V_{cb}^*) = + (2.8 \pm 0.2) 10^{-5}$ .

Why is precision important? Future Theory may reduce #of St.M. parameters  
(when preparing this talk, I encountered only one  $4\sigma$  discrepancy, the rate of  $\tau \rightarrow K\nu$  disagrees with that of  $K \rightarrow \mu\nu$  and lepton universality.)



Progress of Theoretical Physics, Vol. 49, No. 2, February 1973

## **CP-Violation in the Renormalizable Theory of Weak Interaction**

Makoto KOBAYASHI and Toshihide MASKAWA

*Department of Physics, Kyoto University, Kyoto*

(Received September 1, 1972)

One spin-½ quartet ( $p, n, \lambda, \zeta$ ) +  $H, W$

2 L-doublets, 4 R-singlets  $\Rightarrow$  no CPV

2 L-doublets, 1 R-d., 2 R-s.  $\Rightarrow$  CPV

one new scalar field  $\Rightarrow$  CPV

Next we consider a 6-plet model, another interesting model of *CP*-violation.

Suppose that 6-plet with charges  $(Q, Q, Q, Q-1, Q-1, Q-1)$  is decomposed into  $SU_{\text{weak}}(2)$  multiplets as  $2+2+2$  and  $1+1+1+1+1+1$  for left and right components, respectively.

...

$$\begin{pmatrix} \cos \theta_1 & -\sin \theta_1 \cos \theta_3 & -\sin \theta_1 \sin \theta_3 \\ \sin \theta_1 \cos \theta_2 & \cos \theta_1 \cos \theta_2 \cos \theta_3 - \sin \theta_2 \sin \theta_3 e^{i\delta} & \cos \theta_1 \cos \theta_2 \sin \theta_3 + \sin \theta_2 \cos \theta_3 e^{i\delta} \\ \sin \theta_1 \sin \theta_2 & \cos \theta_1 \sin \theta_2 \cos \theta_3 + \cos \theta_2 \sin \theta_3 e^{i\delta} & \cos \theta_1 \sin \theta_2 \sin \theta_3 - \cos \theta_2 \sin \theta_3 e^{i\delta} \end{pmatrix}$$

Then, we have *CP*-violating effects through the interference among these different current components.

## **Honours**

### **UNITARY SYMMETRY AND LEPTONIC DECAYS**

**PRL 10  
(1963)  
531**

Nicola Cabibbo  
CERN, Geneva, Switzerland  
(Received 29 April 1963)

$$J_\mu = \cos \theta \cdot (V + A) \frac{\Delta S=0}{\mu} + \sin \theta \cdot (V + A) \frac{\Delta S=1}{\mu}$$

$$\theta = 0.257 \text{ from } \Gamma(K \rightarrow \mu\nu)/\Gamma(\pi \rightarrow \mu\nu)$$

<sup>4</sup>Similar considerations are forwarded in M. Gell-Mann and M. Lévy, Nuovo Cimento 16, 70 (1960)

$$G V_\alpha + G V_\alpha^{(\Delta S=1)} = G_\mu \bar{p} \gamma_\nu (n + \varepsilon A) (1 + \varepsilon^2)^{-\frac{1}{2}}$$

$$\varepsilon^2 = .06$$

$V_{CKM} \not\propto$

$V_{GLCHGWSBIMKM}$

We are very  
proud of the  
prize awarded  
to KM.