



**Neutrino Experiments:**  
 **$\nu$  Questions for a New Decade...**  
Janet Conrad, SLAC Summer Institute, 2011

My theme:

If I were a graduating student or recent postdoc,  
and considering working in neutrino physics,  
what would I consider working on?

if you are an experimentalist ... what experiments?  
if you are a theorist ... what questions?

## Part I: Neutrino Basics...

The neutrino we once knew and loved

Neutrino Oscillations

A “nu” Standard Model

## Part II: Oscillation experiments: 2011-2020

Pursuit of the missing pieces

An unconventional approach: DAE $\delta$ ALUS

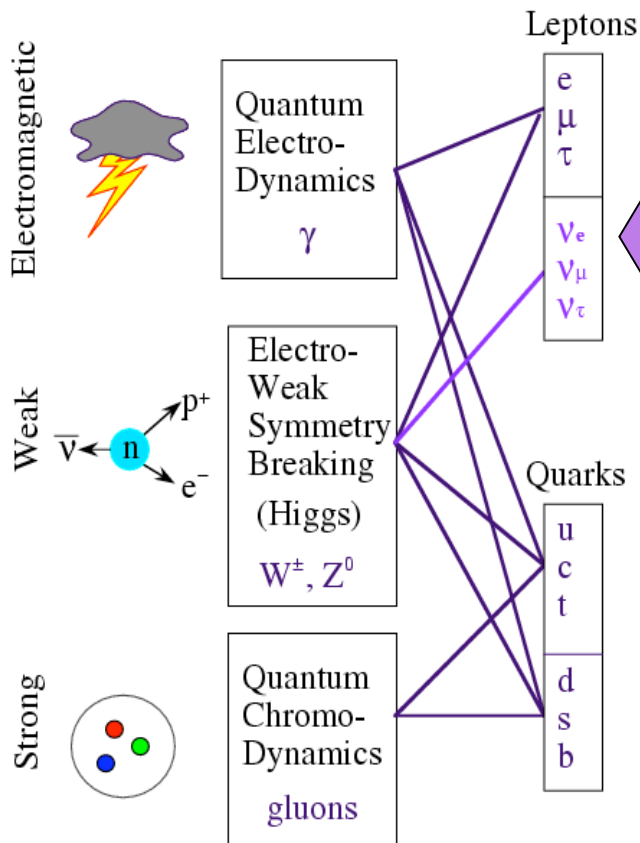
Oscillations at short Baseline



The Neutrino We Used  
to Know and Love

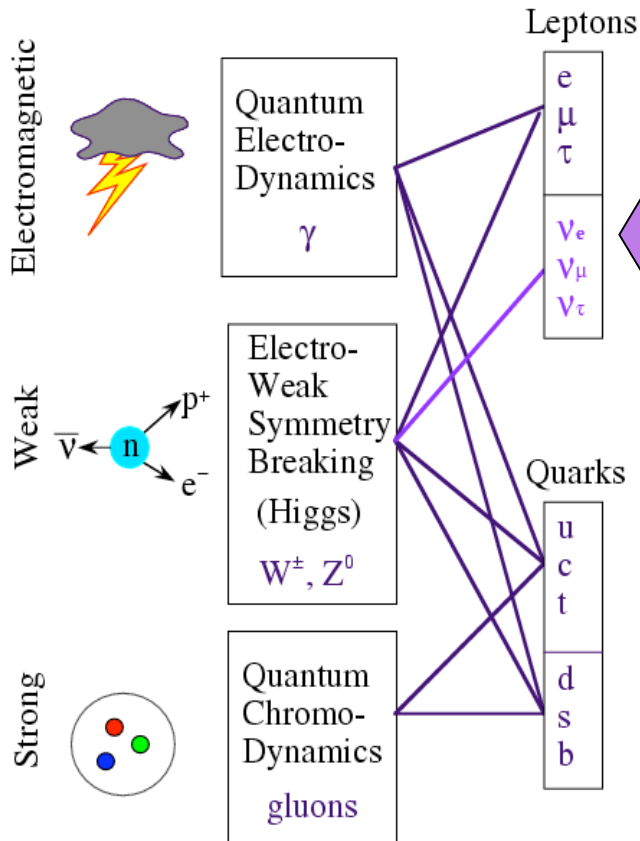


# The Standard Model



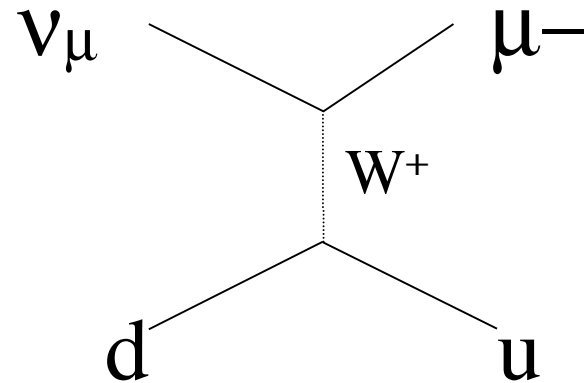
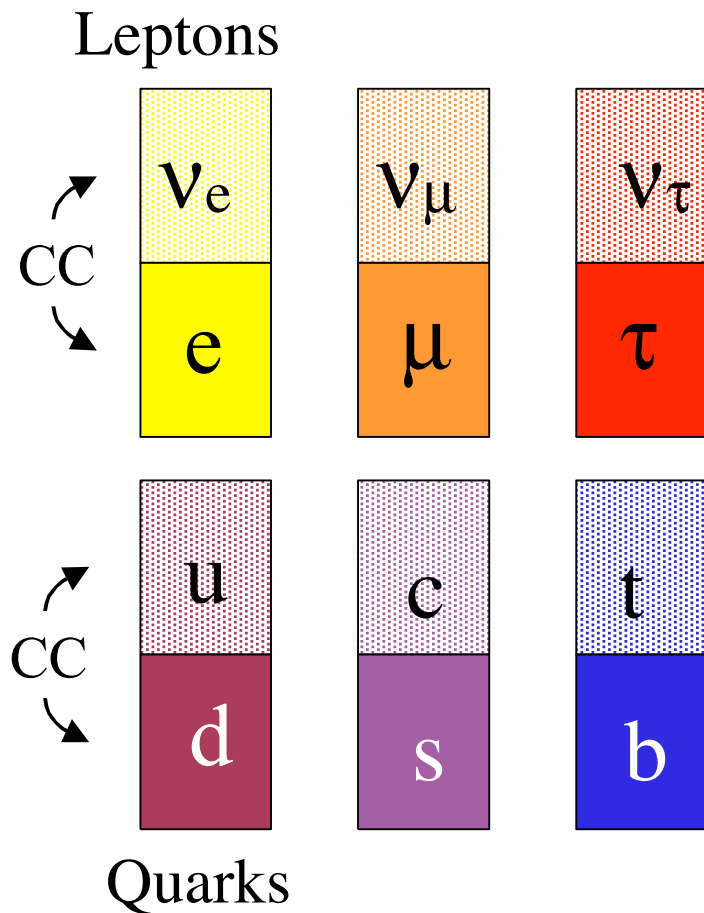
- Only interact via the “weak force”
- Interact thru W and Z bosons
- Neutrinos have three flavors
  - Electron  $\nu_e \rightarrow e$
  - Muon  $\nu_\mu \rightarrow \mu$
  - Tau  $\nu_\tau \rightarrow \tau$
- Neutrinos are left-handed (Antineutrinos are right-handed)
- Neutrinos are massless

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In the Standard Model,  
Neutrinos are part of the lepton “weak doublets”

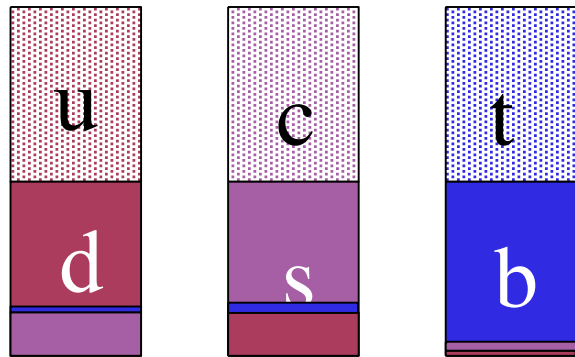


For a CC interaction to occur  
you need enough energy  
to produce the massive  
final state particles

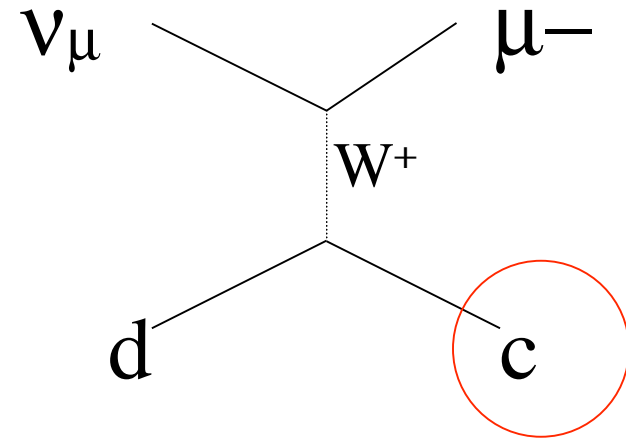
The quarks also form weak doublets...<sup>7</sup>

In the quark sector, we have “mixing”

quark mass eigenstates  $\neq$  quark weak eigenstates



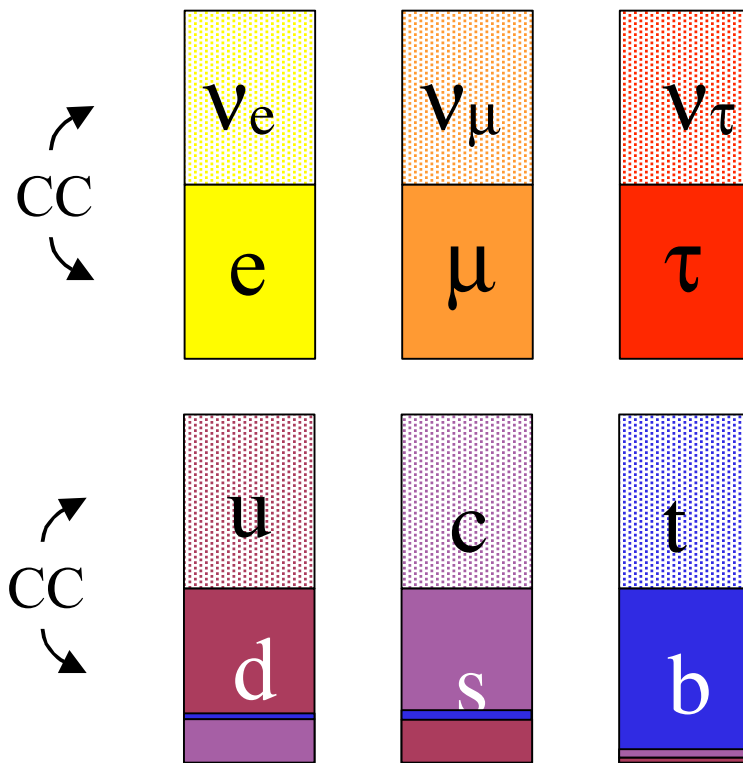
Small effect,  
but clearly  
seen in weak  
interactions...



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}.$$

... and  
kaon decays,  
D meson decays,  
etc.

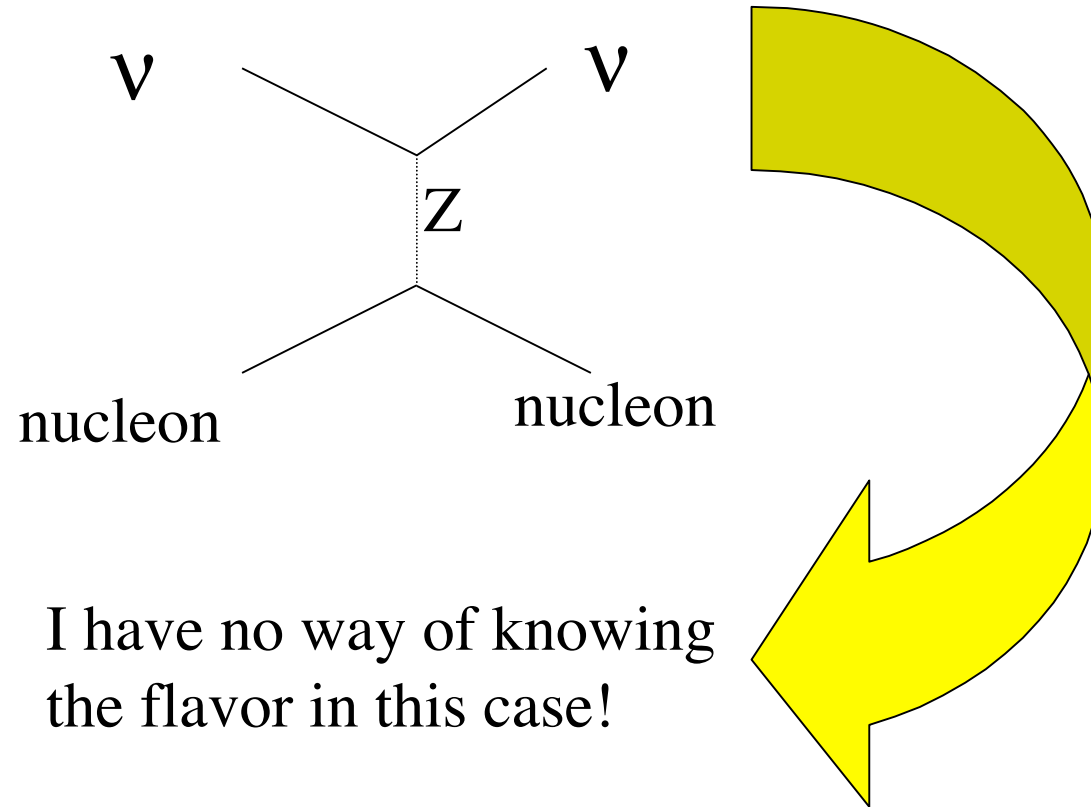
But within the model,  
there is no mixing in the lepton sector



Which looks  
a little strange,  
doesn't it?

## Neutrinos can also have Neutral Current (NC) Interactions

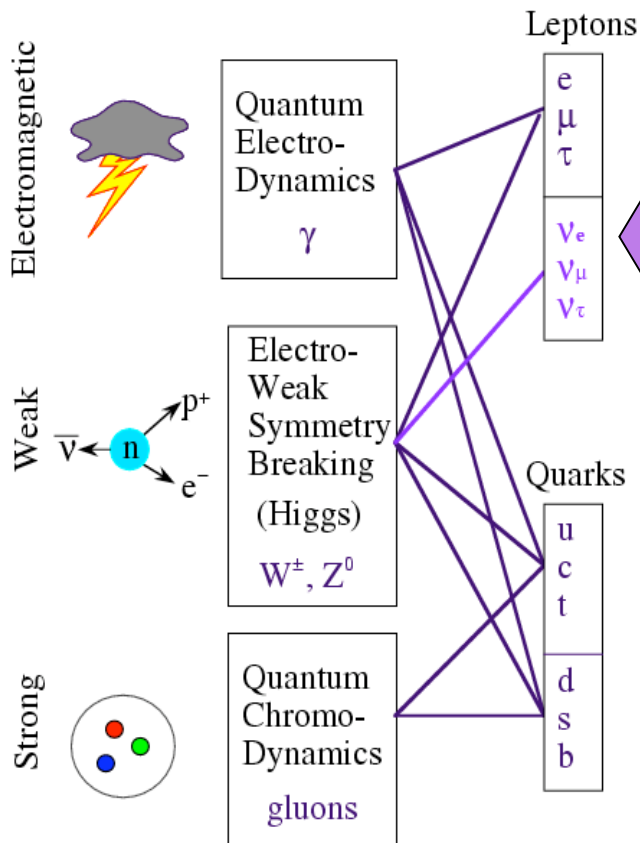
e.g.



I have no way of knowing  
the flavor in this case!

If I am interested in neutrino flavor,  
I have to rely upon the CC interaction!

# The Standard Model



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A quick reminder about parity violation...

All spin 1/2 particles have “helicity”

The projection of spin along the particle's direction

The operator:  $\sigma \cdot \mathbf{p}$

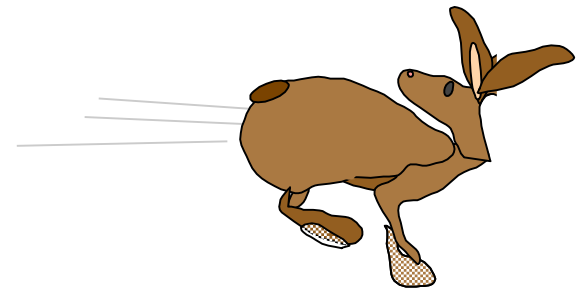
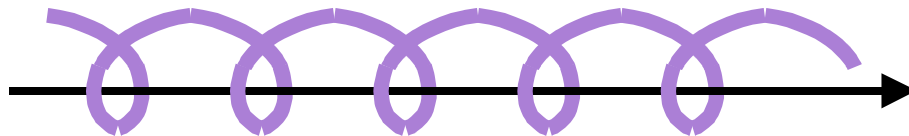
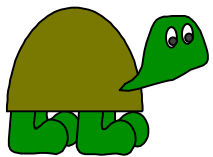
right-helicity



left-helicity

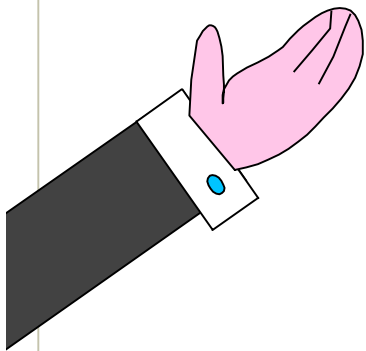


Frame dependent (if particle is massive)



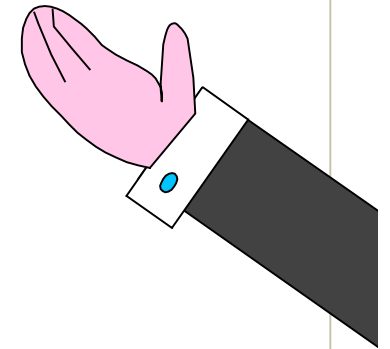


Handedness (or chirality) is the Lorentz-invariant counterpart  
Identical to helicity for massless particles (standard model  $\nu$ 's)



*Hello!*

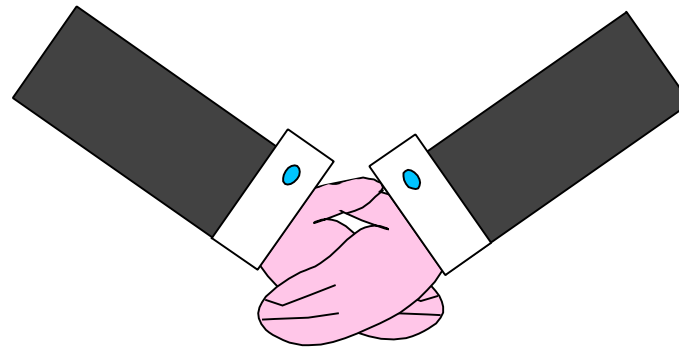
*Hello!*



Naively  
you would think nature would make  
an equal left-handed/right-handed mix.

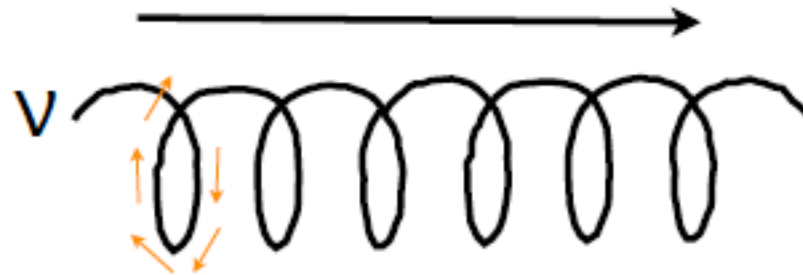
But NO!  
The weak interaction produces  
right-handed antiparticles  
and left-handed particles  
**100% of the time!**

"The W only shakes  
with the left hand"

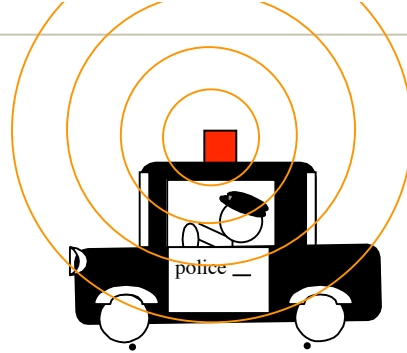


Since neutrinos **ONLY** interact via the weak interaction

Neutrinos are always left-handed



And antineutrinos are right-handed



How do you enforce the law of left-handedness?

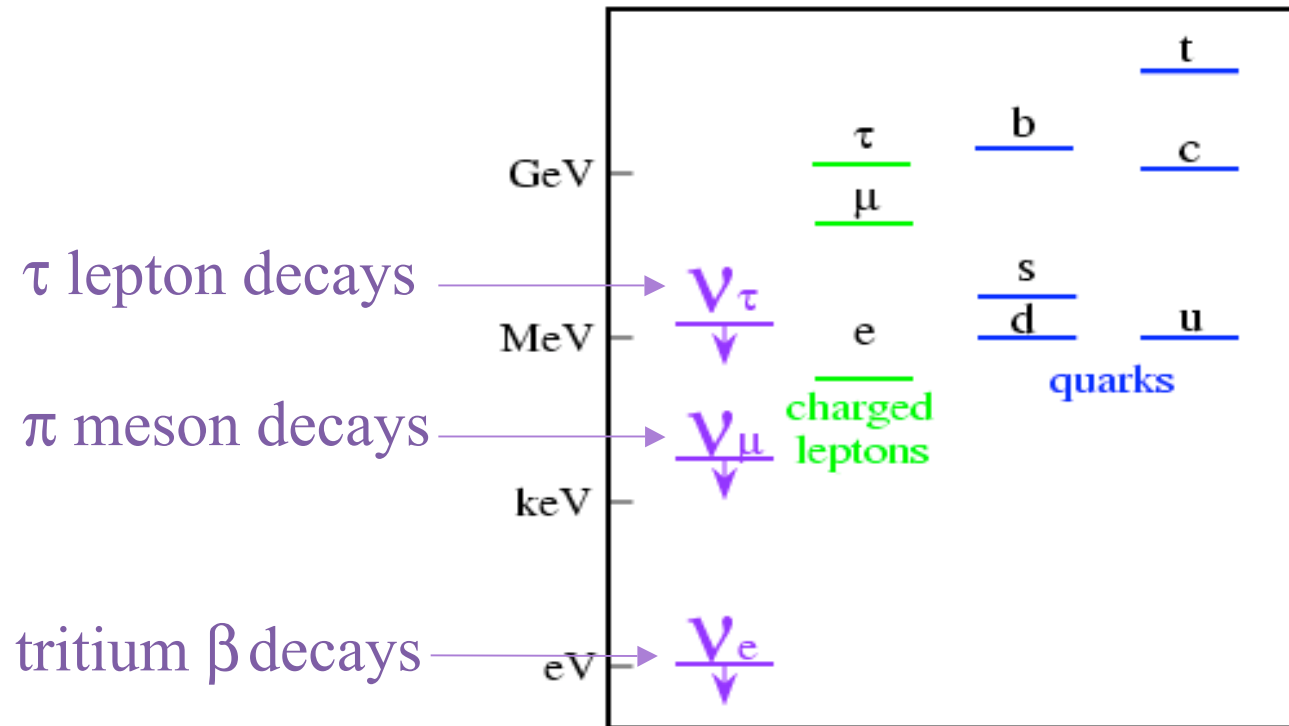
Well... what couples left-handed particles to right?

A Dirac mass term  
in the SM Lagrangian:

$$m(\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L)$$

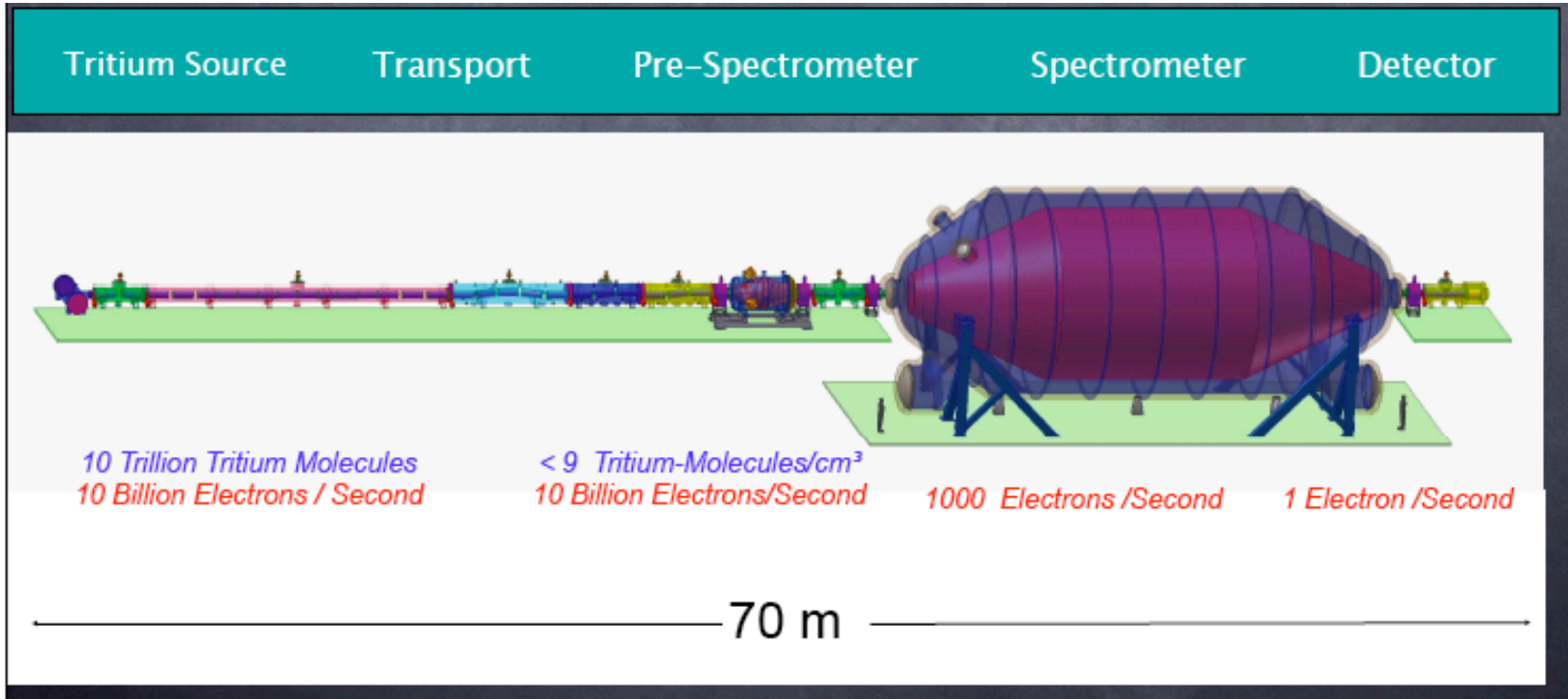
If you want to build parity violation into “the law”  
you have to keep this term out of the Lagrangian...  
a simple solution is:  $m=0$

Direct (kinematic) searches are consistent with massless  $\nu$ 's:



We only have limits!

The future of direct mass measurement is the KATRIN Experiment:



Probes to  $m_\nu < 0.2$  eV @90% CL

- improved statistics (stronger source, longer running)
- improved resolution (electrostatic spectrometer with  $\Delta E = 1$  eV)
- background reduction (materials choices, veto)

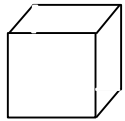


Just to set the scale of the size of KATRIN...

# Neutrino production

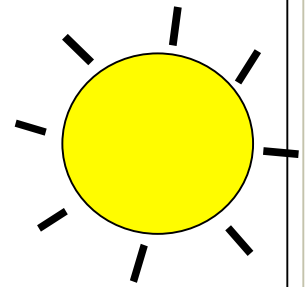
vs from  
Supernovae

Relic vs from  
Big Bang

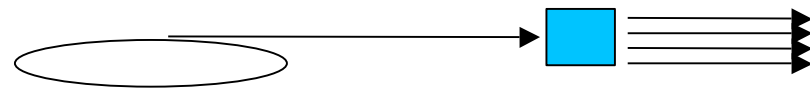
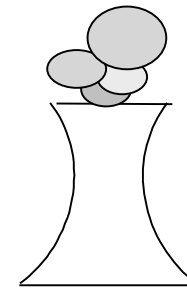


$10^9$  per  $m^3$

Cosmic Ray  
Showers



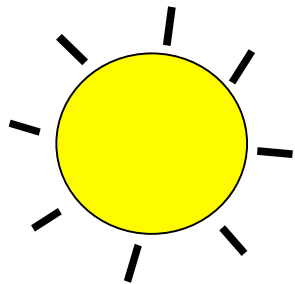
vs from  
the sun



Beams made from Reactors  
and Particle Accelerators

Low energy sources produce neutrinos via  
beta decay and electron capture

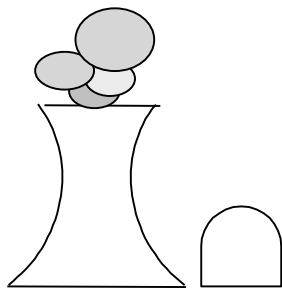
Both involve the electron flavor



electron neutrinos

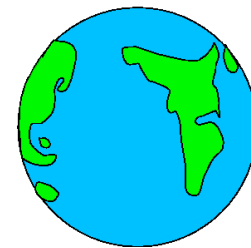
(< 15 MeV)

Production  
is very  
flavor pure!



electron antineutrinos

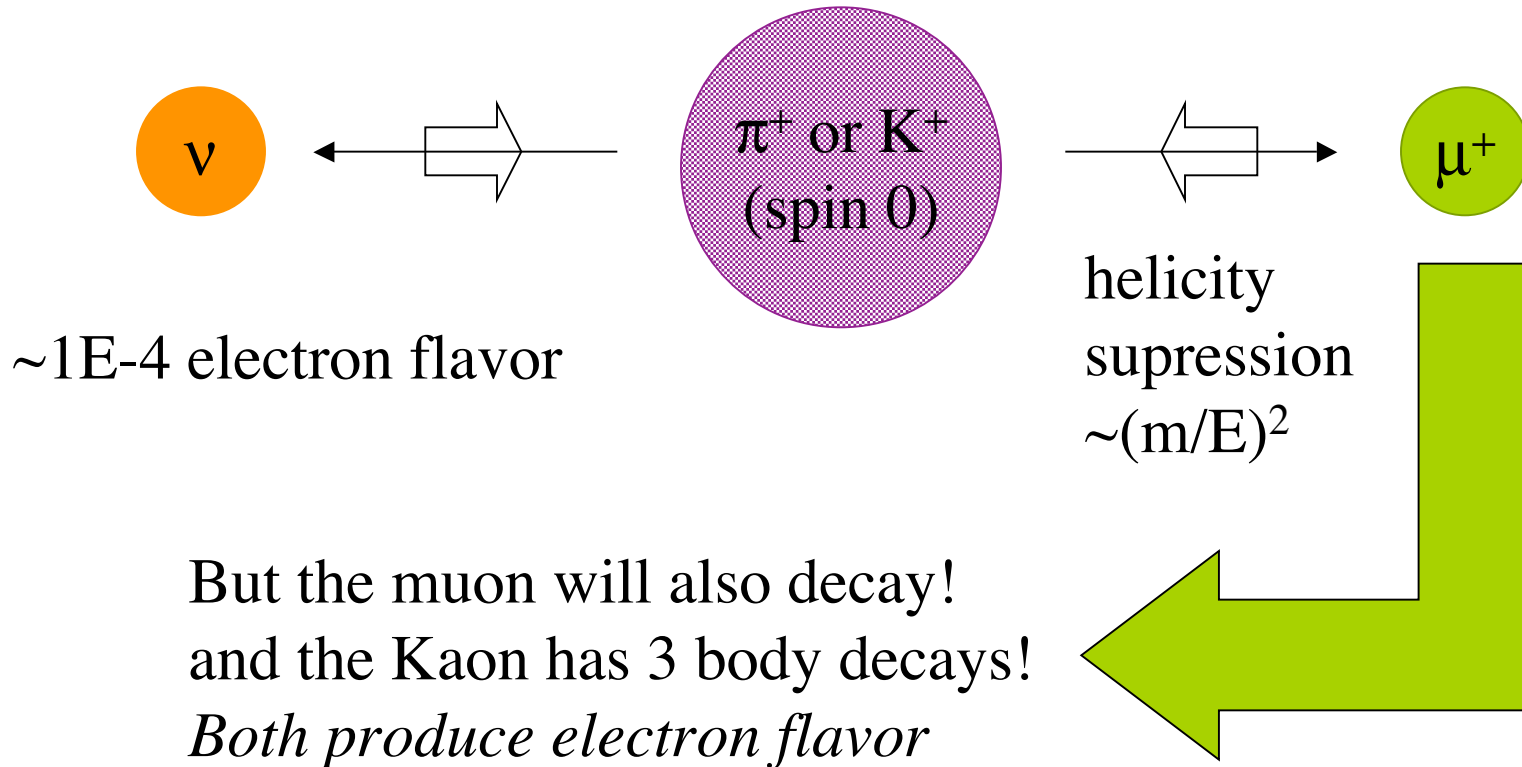
(< 10 MeV)



But observing low energy neutrinos is difficult



Sources with enough energy to produce muons, will dominantly produce muon flavor neutrinos



Conventional high energy sources are mostly muon neutrino, but generally have a few % electron flavor at production

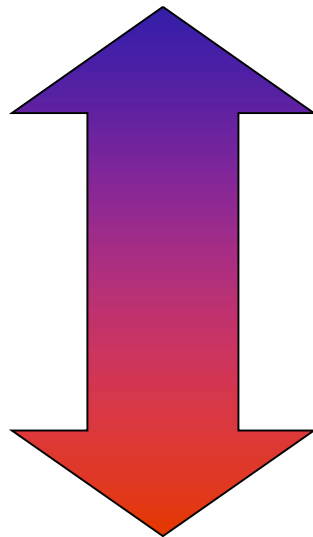
The interaction depends upon the  $\nu$  energy...

The main sources

Reactors,  
The Sun

Cosmic rays,  
accelerators

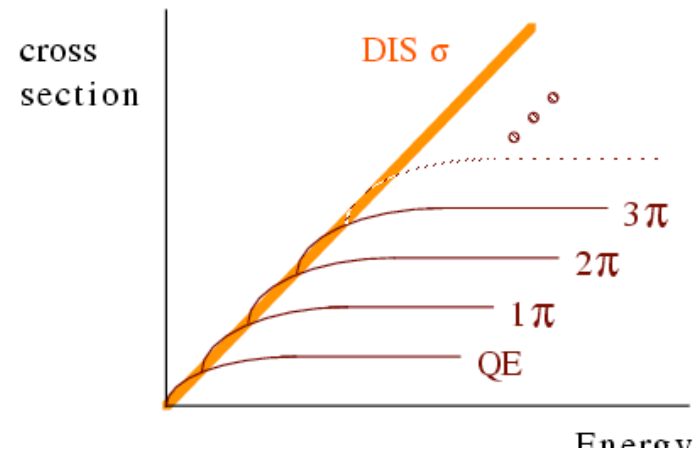
Few MeV



Multi-GeV+

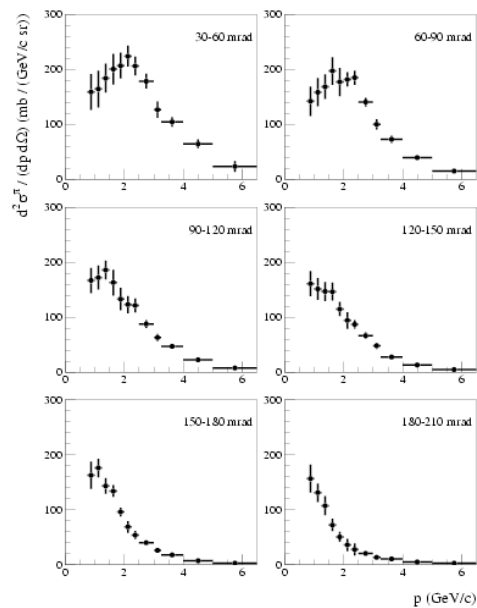
Useful interactions

Elastic (esp.  $\nu e \rightarrow \nu e$ )  
Quasielastic ( $\nu N \rightarrow \ell N'$ )  
Single Pion Production  
(resonant & coherent)  
Deep Inelastic Scattering



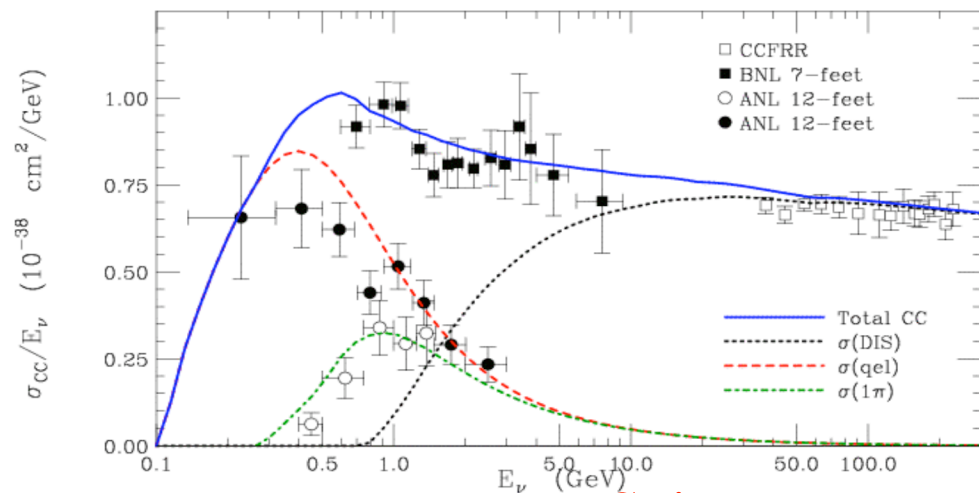
Nearly all “new physics” neutrino searches experiments require accurate knowledge of the beam and SM cross sections.

In neutrino physics, these are experiments like:



HARP  
MIPP  
SHINE

These are crucial experiments



SciBooNE

Argoneut

Minerva

MicroBooNE

So lets review...

We have a Standard Model Neutrino

**But it isn't very standard**

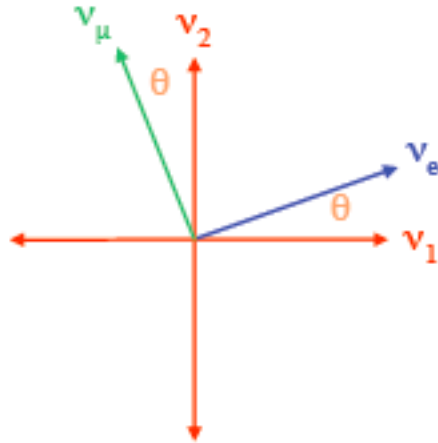
- The only fermion that does not carry electric charge
- The only fermion that is only left handed
- The only fermion which is massless



The Neutrinos We Know Today...

Lets say that neutrinos can mix, like the quarks...

And lets say that neutrinos do have mass states, like the quarks...



The neutrino flavor states in bra-ket notation.

For Two Neutrinos...

$$\begin{array}{cc} \text{flavor} & \text{mass} \\ \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix} \end{array}$$

The mixing of the states is expressed by a rotation matrix.

$$|\nu_e\rangle = \cos \theta |\nu_1\rangle + \sin \theta |\nu_2\rangle$$

$$|\nu_\mu\rangle = -\sin \theta |\nu_1\rangle + \cos \theta |\nu_2\rangle$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

So starting with the mixing matrix.

$$|\nu_\mu(0)\rangle = -\sin \theta |\nu_1\rangle + \cos \theta |\nu_2\rangle$$

The state at time  $t=0$ .

$$|\nu_\mu(t)\rangle = -\sin \theta e^{-iE_1 t} |\nu_1\rangle + \cos \theta e^{-iE_2 t} |\nu_2\rangle$$

The state's evolution in time.

Then the probability is given by the amplitude squared.

$$P_{osc} = |\langle \nu_e | \nu_\mu(t) \rangle|^2 = \frac{1}{2} \sin^2 2\theta (1 - \cos(E_2 - E_1)t)$$

$$P_{osc} = |\langle \nu_e | \nu_\mu(t) \rangle|^2 = \frac{1}{2} \sin^2 2\theta (1 - \cos(E_2 - E_1)t)$$

$$E_i = \sqrt{p^2 + m_i^2} \approx p + m_i^2/2p$$

We know the mass is small so we can use a Taylor expansion and then change some units.

$$t/p = L/E$$

$$P_{osc} = \frac{1}{2} \sin^2 2\theta \left( 1 - \cos \left( \frac{(m_2^2 - m_1^2)L}{4E} \right) \right)$$

$$P_{osc} = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

Look! It depends on mass differences, so if neutrinos oscillate they must have mass!



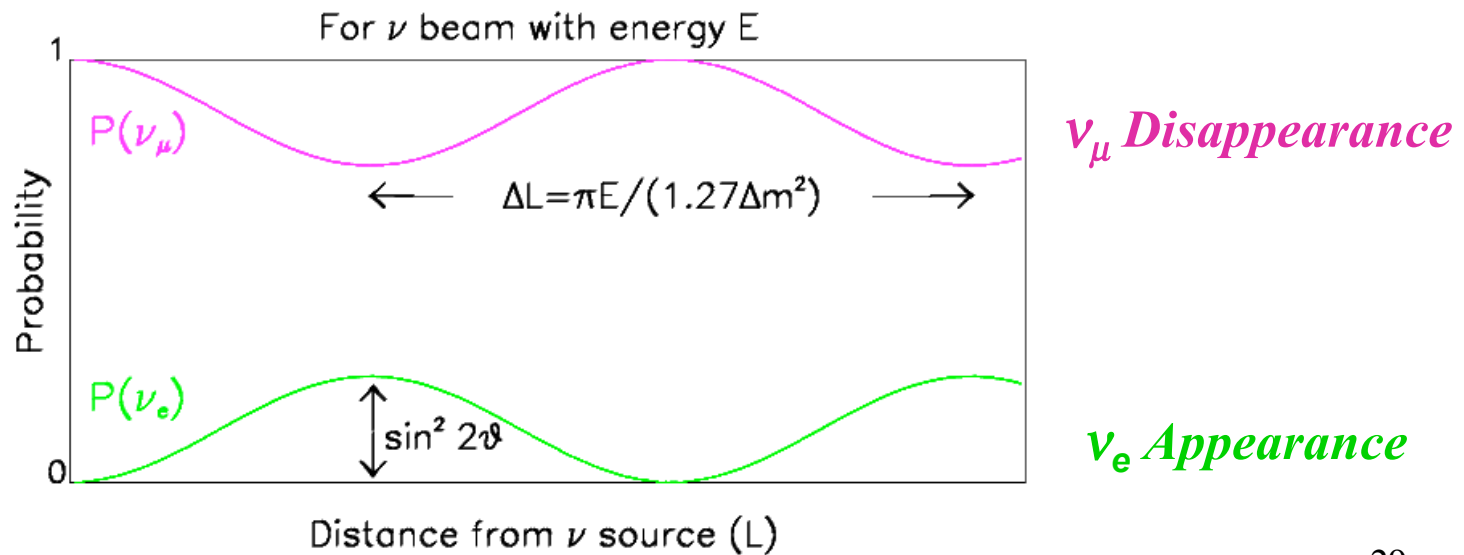
$$P_{Osc} = \sin^2 2\theta \sin^2 \left( 1.27 \Delta m^2 L / E \right)$$

...Depends Upon Two Experimental Parameters:

- $L$  – The distance from the  $\nu$  source to detector (km)
- $E$  – The energy of the neutrinos (GeV)

...And Two Fundamental Parameters:

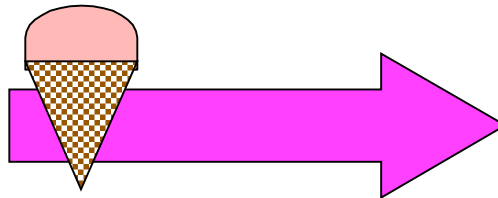
- $\Delta m^2 = m_1^2 - m_2^2$  ( $eV^2$ )
- $\sin^2 2\theta$



## Disappearance experiments

source

start with a  
certain flavor



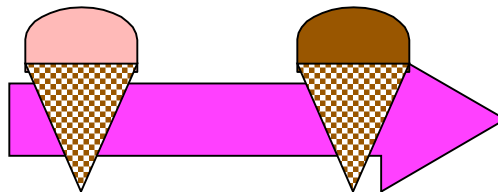
detector

Do you see the  
same flavor?

New flavor components  
may be too massive to  
produce in a CC interaction

## Appearance experiments

start with a  
certain flavor



Do you see a  
new flavor?

New flavor components  
may “stick out” clearly  
in the event sample

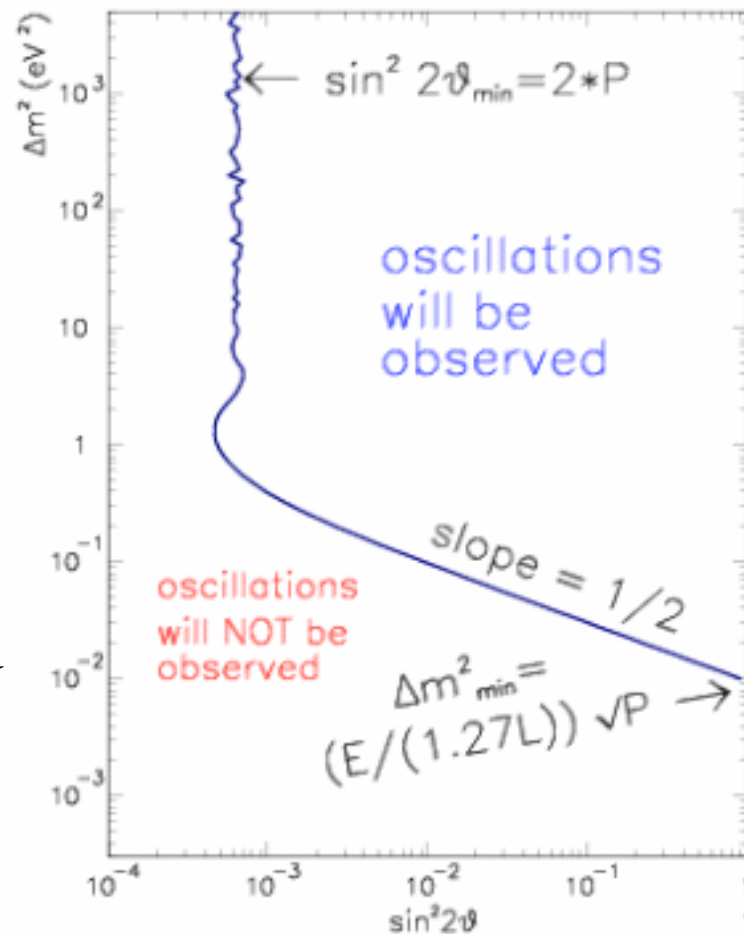
$$P_{Osc} = \sin^2 2\theta \sin^2 (1.27 \Delta m^2 L / E)$$

at high  $\Delta m^2$ ,  
 $\langle \sin^2(1.27 \Delta m^2 L / E) \rangle = 1/2$

1 measurement  
 and  
 2 parameters...

Allowed regions will  
 look like "blobs"

Exclusions by experiments  
 with no signal are indicated  
 by lines...



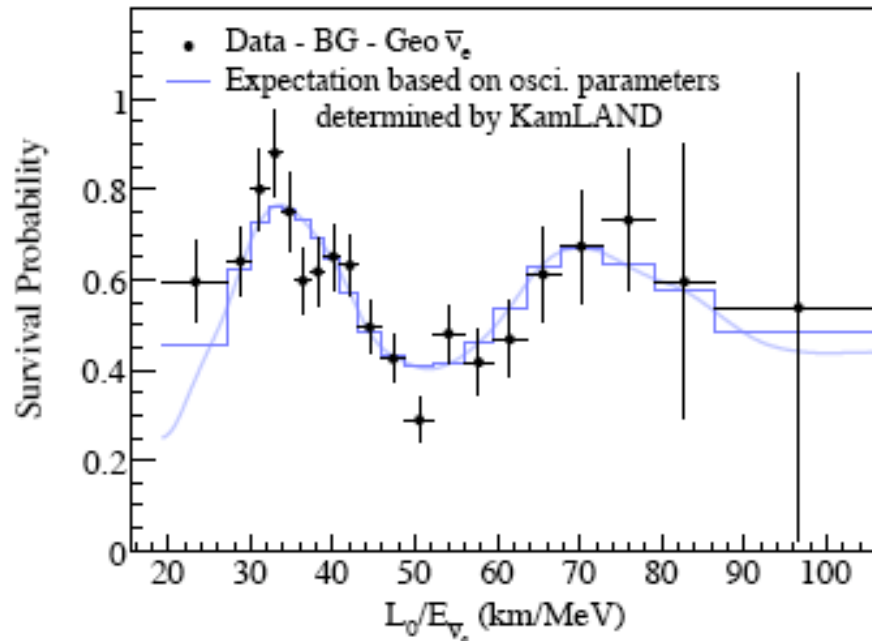
At low  $\Delta m^2$   
 use the  
 small angle  
 approx.

## *The Probability for Oscillations...*

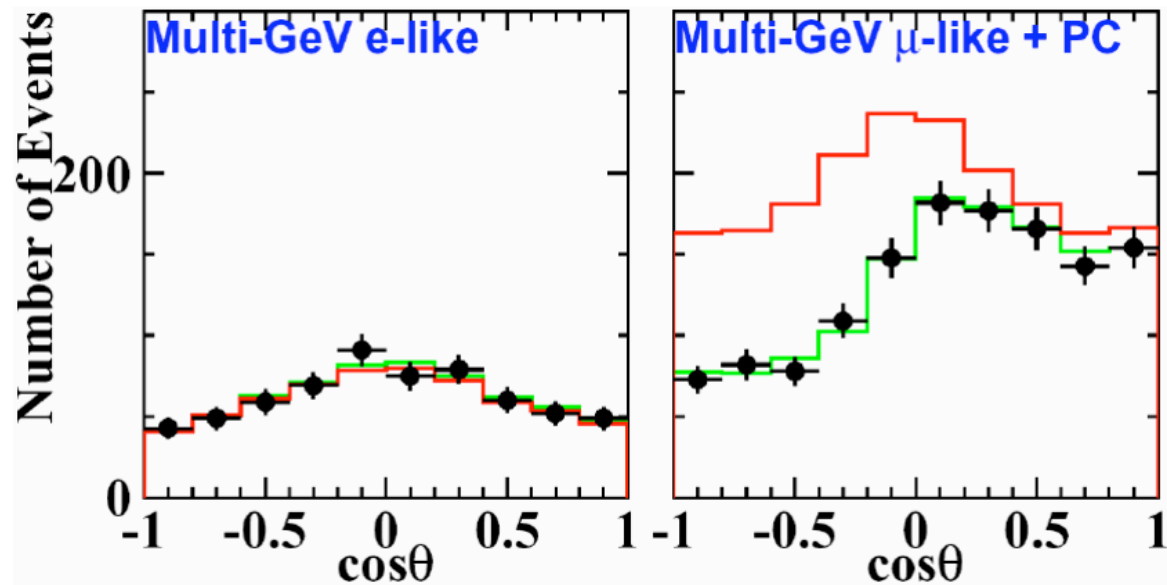
$$P_{osc} = \sin^2 2\theta \sin^2(1.27\Delta m^2 L/E)$$

For example, in Kamland!

anti-electron neutrinos from a reactor disappear  
with a wavelength consistent with  $\Delta m^2 \sim 5E-5 \text{ eV}^2$



The Super-K experiment showed that atmospheric muon neutrino disappearance fits an oscillation hypothesis



with  $\Delta m^2 \sim 3E-3 \text{ eV}^2$

Confirmed by K2K and MINOS accelerator beam expts

Right now, we have no clear evidence for appearance  
in any oscillation experiment

But we do have evidence for both disappearance and appearance  
in another effect that requires  
both mixing and mass differences

 Solar Neutrino Oscillations  
~~Oscillations~~  
Morphing

The Sun

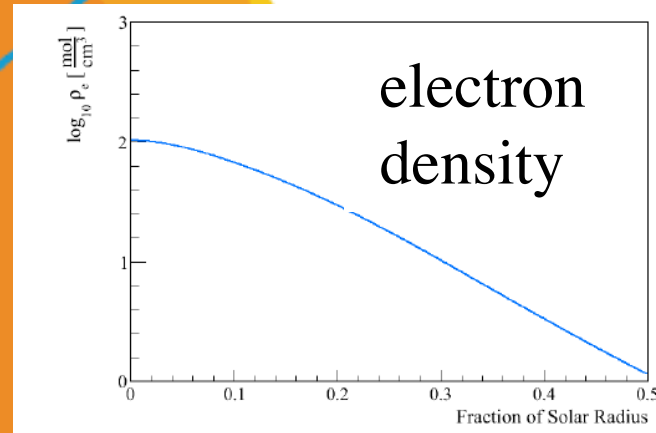
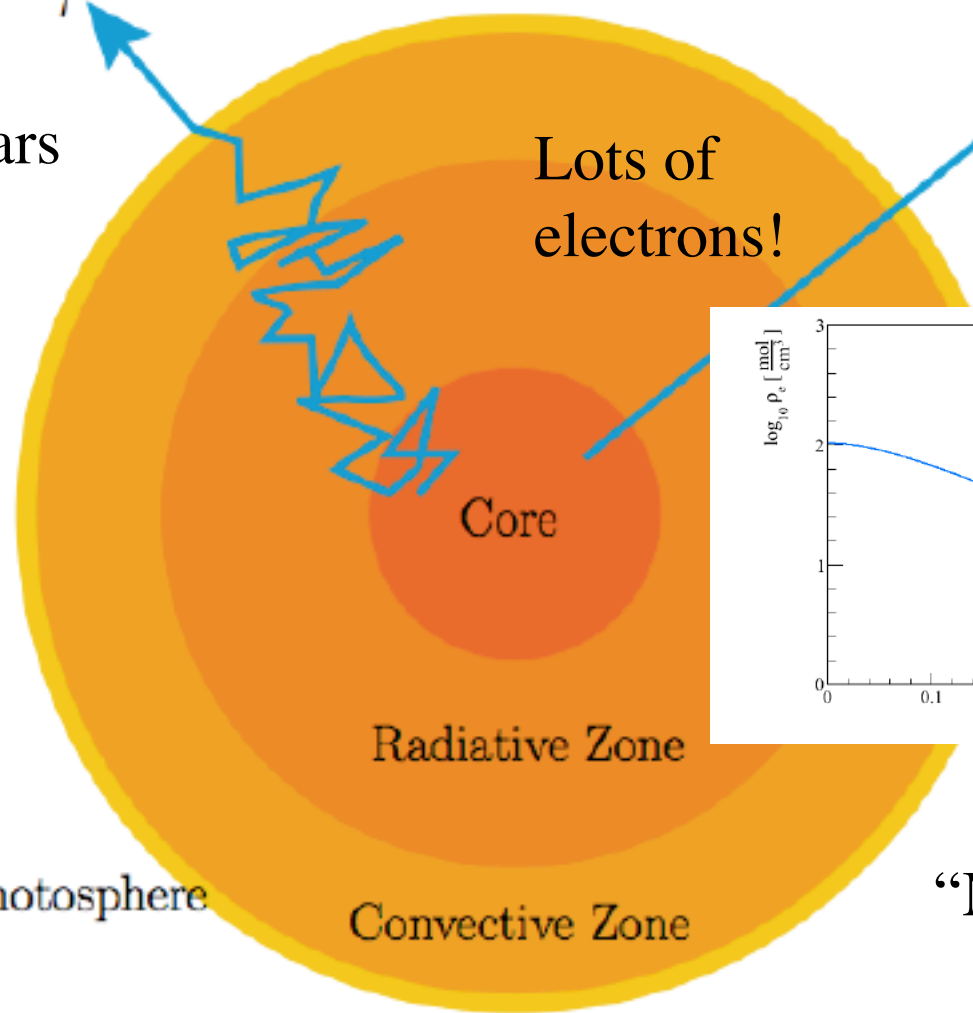
immediate

10,000 years

$\gamma$

Lots of electrons!

$\nu$



Photosphere

Convective Zone

Radiative Zone

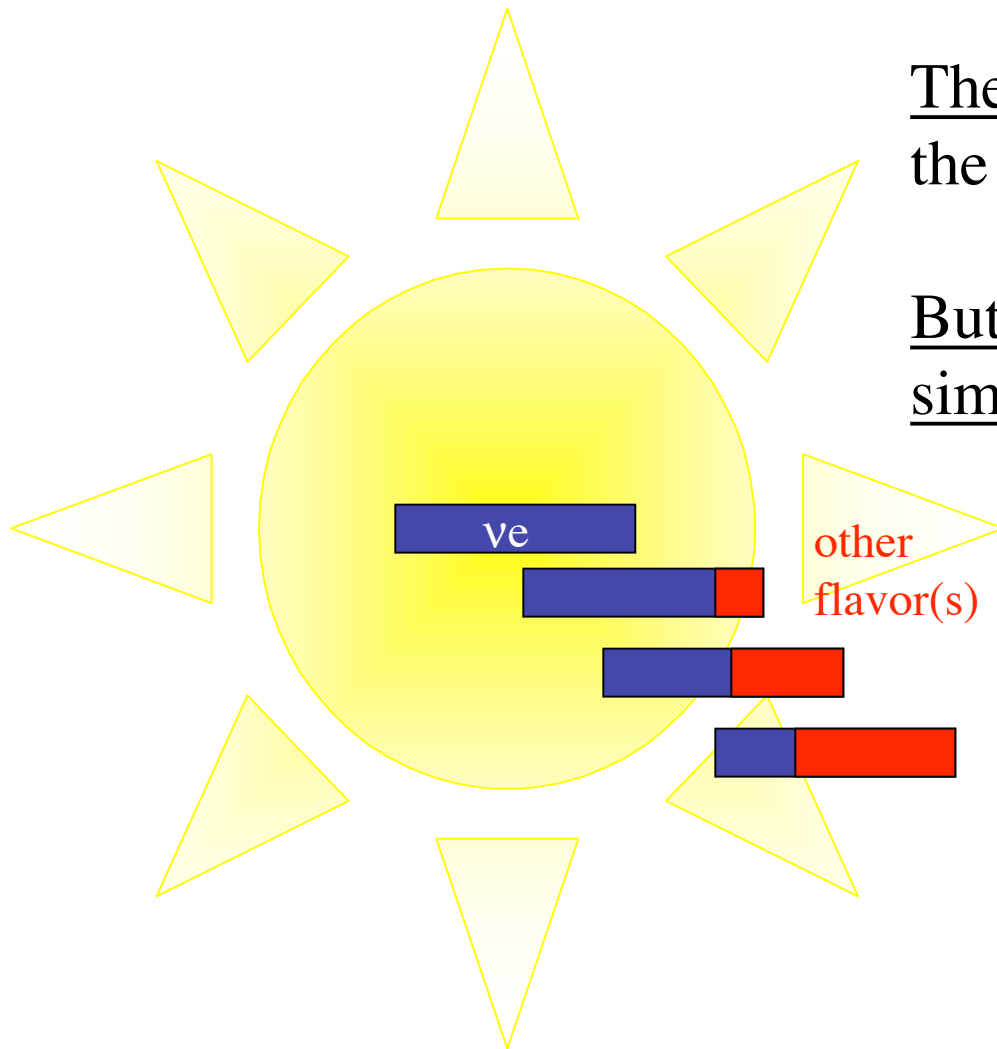
Core

“Matter Effects”

In the electron “soup”

The  $\nu_e$  sees a CC and NC potential

The  $\nu_\mu$  and  $\nu_\tau$  see only the NC potential



There is flavor evolution as the neutrinos traverse the sun.

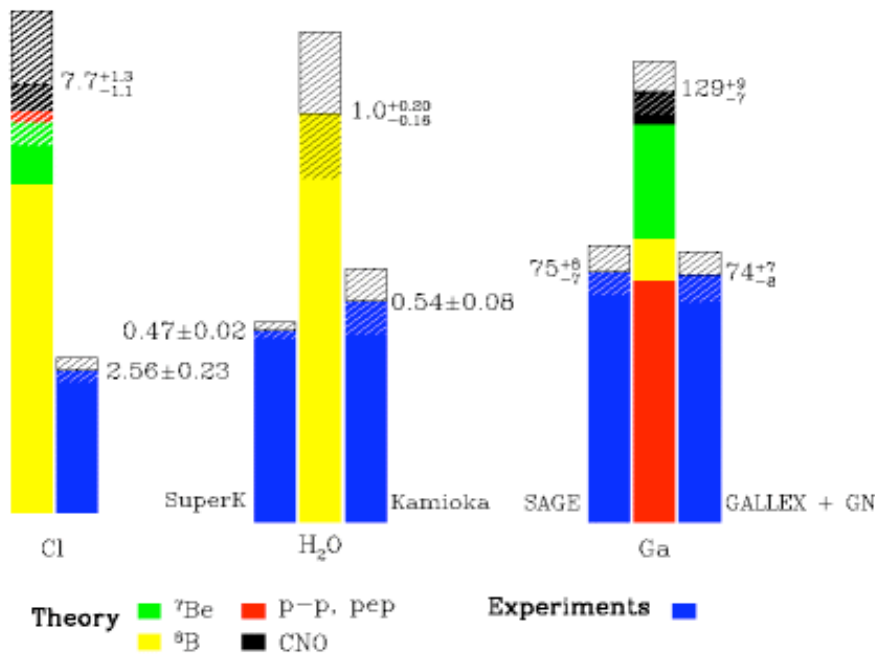
But the equations do not simplify to oscillations

The result looks like disappearance in detectors sensitive to only  $\nu_e$  flavors...



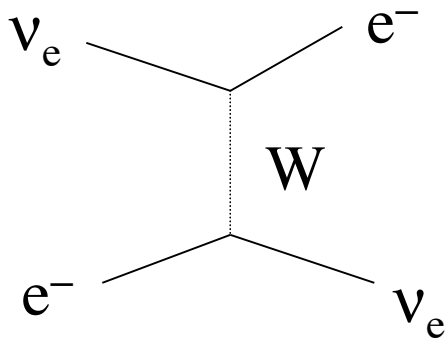
# The famous “Solar Neutrino Deficit”

Total Rates: Standard Model vs. Experiment  
Bahcall-Pinsonneault 2000

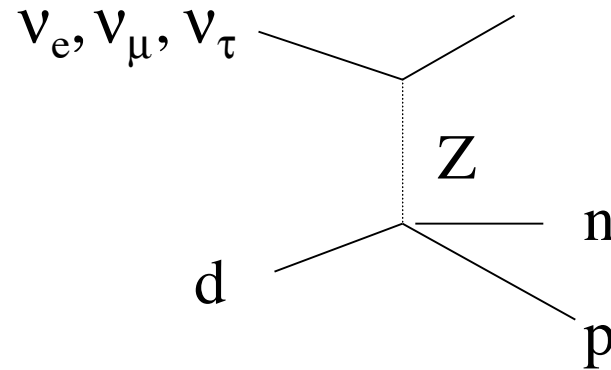


The rate of morphing with energy depends on  $\Delta m^2$  and the mixing angle

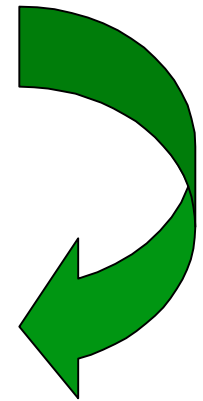
Of course it is only a deficit if you can only see  $\nu_e$  CC scatters!



most solar experiments



SNO



SNO:  $\phi_{\nu_e} + \phi_{\nu_\mu} + \phi_{\nu_\tau} = (4.94 \pm 0.21 \pm 0.36) \times 10^6/\text{cm}^2\text{sec}$

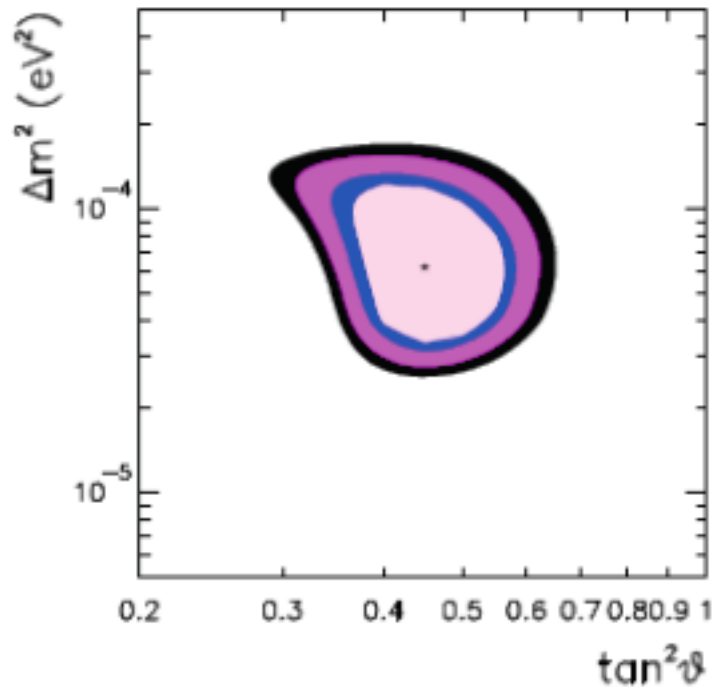
Theory:  $\phi_{\text{total}} = (5.69 \pm 0.91) \times 10^6/\text{cm}^2\text{sec}$

Bahcall, Basu, Serenelli

The NC interaction shows the neutrinos are still there!

Using the energy dependence of solar morphing...

You can extract an allowed region in the oscillation parameter space from solar neutrinos alone



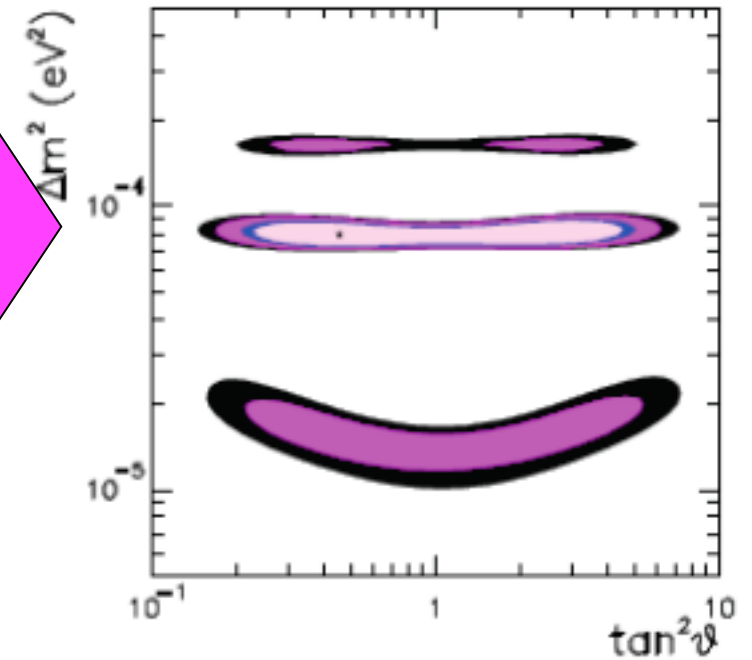
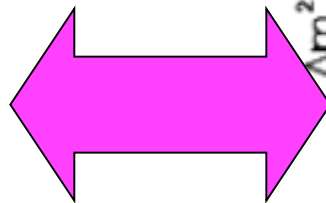
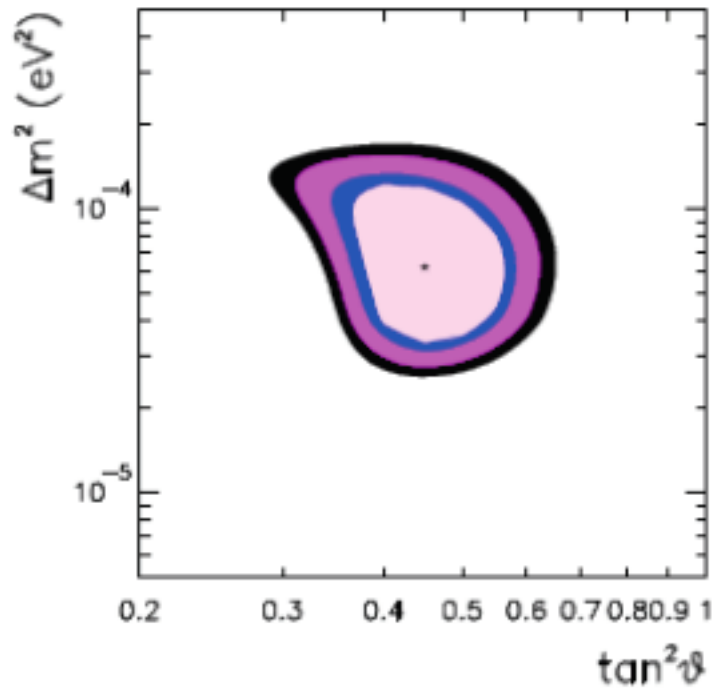
if this is due to  $\nu_e \rightarrow \nu_{\text{other}}$

then  $\bar{\nu}_e \rightarrow \bar{\nu}_{\text{other}}$   
should be observable  
here too!

## It all fits together

Allowed region for  
solar neutrino oscillation  
measurements,

Allowed region for the  
Kamland reactor  
 $\bar{\nu}_e \rightarrow \bar{\nu}_{\text{other}}$  Experiment!



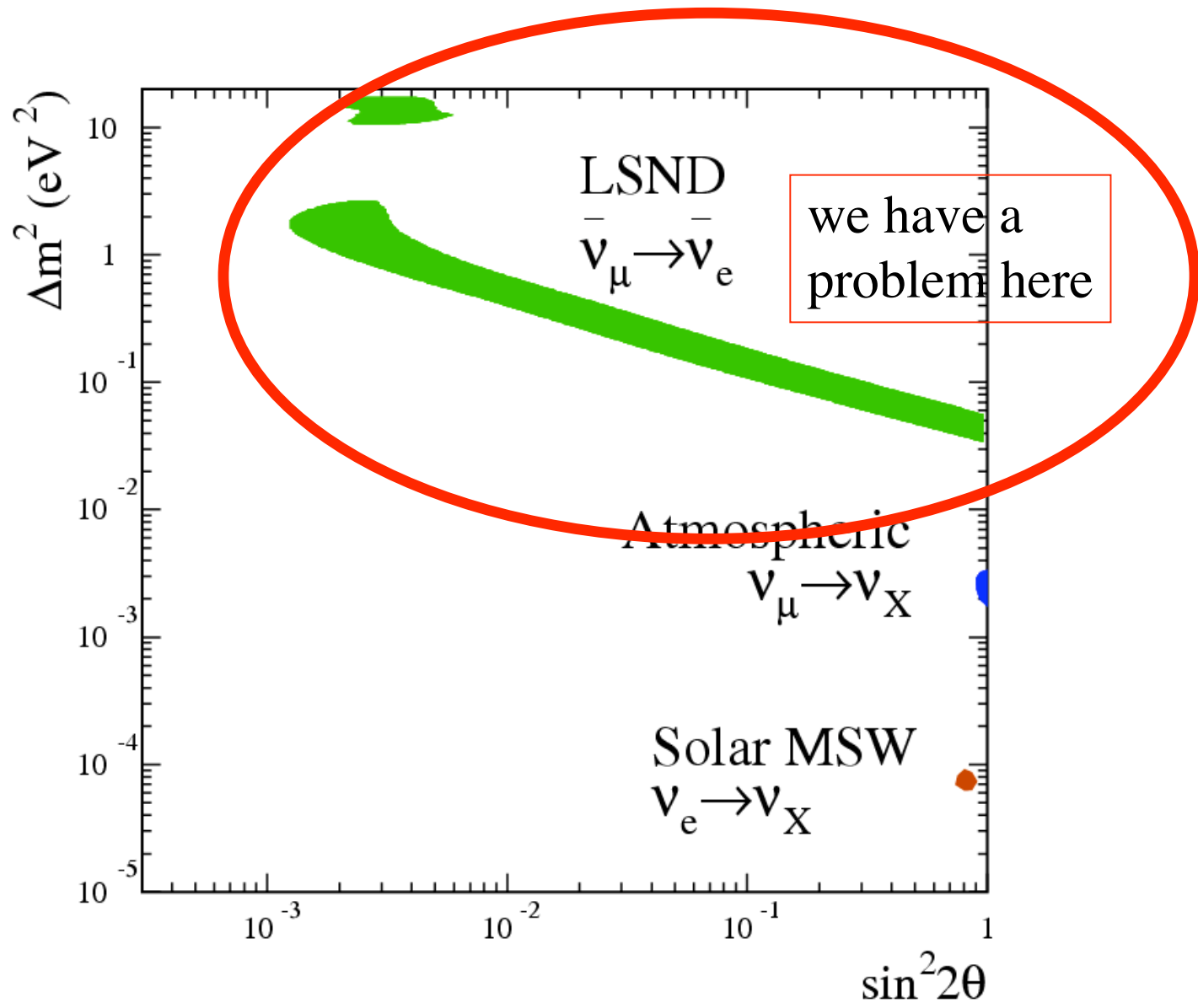
So... where are we?

Our world view has changed because we see...

Oscillations at  $\Delta m^2$  at  $\sim 10^{-3}$  and  $10^{-5} \text{ eV}^2$

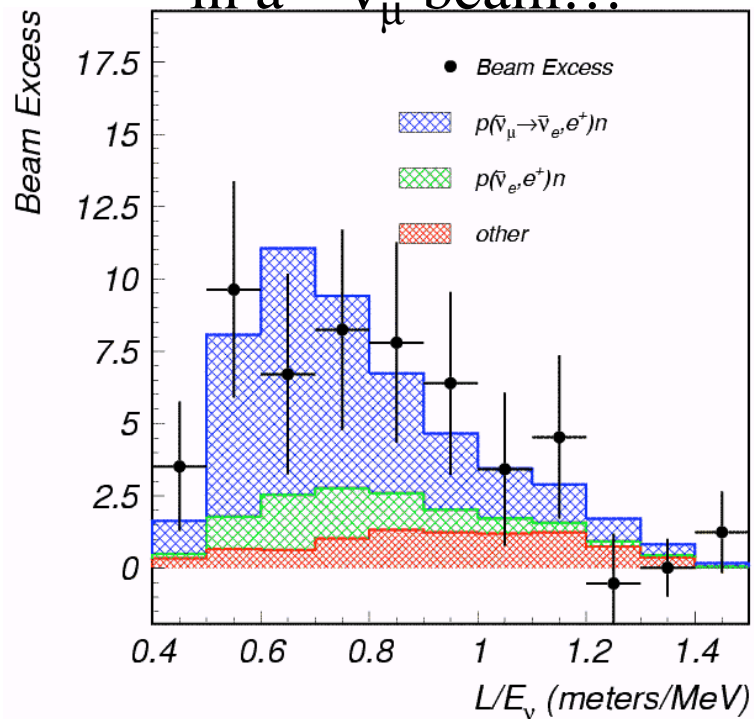
We see solar neutrino “morphing” that fits in.

But there is other data out there,  
and it's a problem...



## LSND ran in the 1990's

An excess of  $\bar{\nu}_e$  events  
in a  $\bar{\nu}_\mu$  beam...

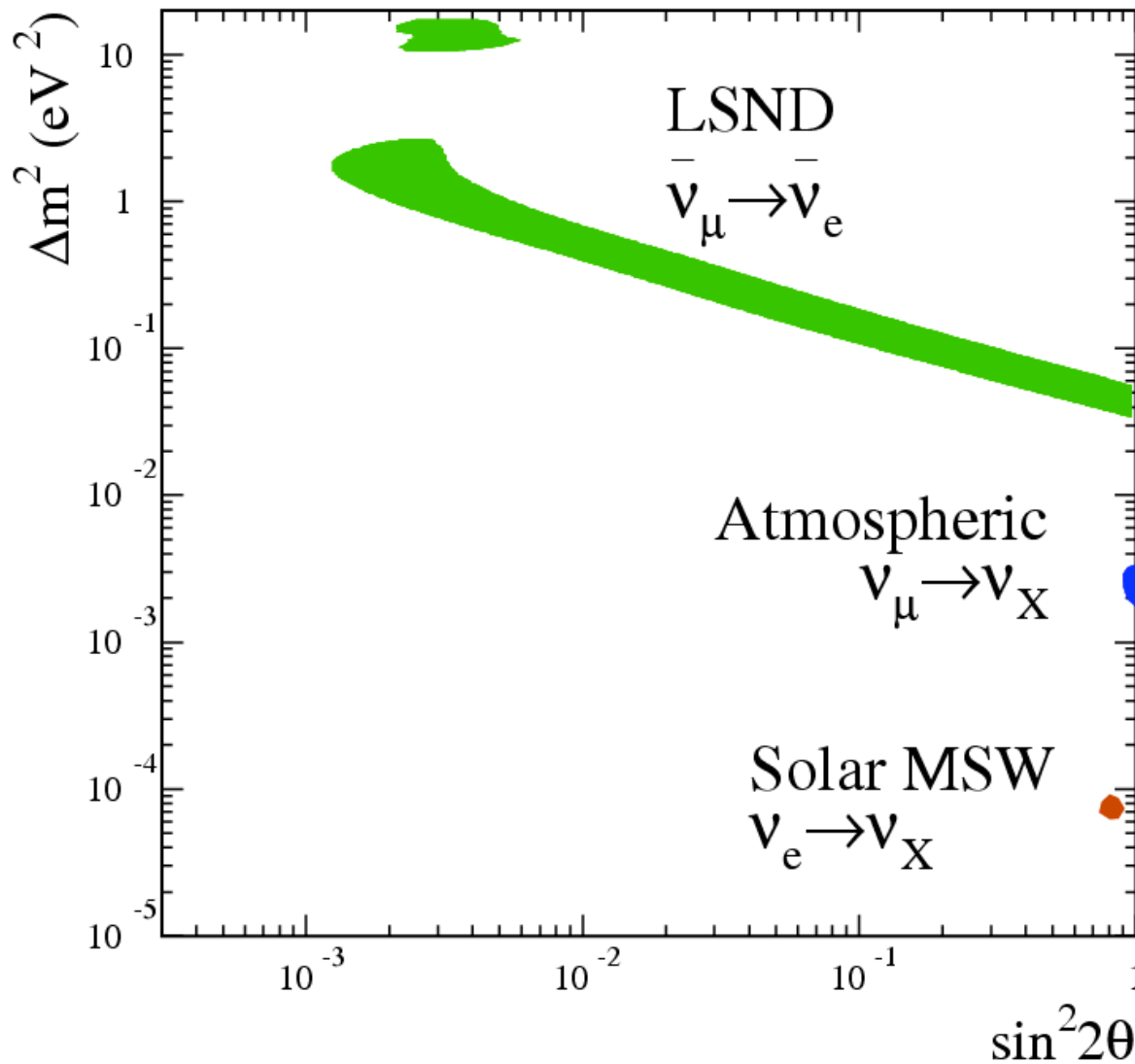


This signal was a big surprise!  
Best solution was very different  
from other signals!

- high  $\Delta m^2$
- small mixing

Why is this a problem?

Consistent with high  $\Delta m^2$   
2 neutrino oscillations



Three neutrino  
 mass states  
 yield only  
 2 independent  
 mass differences

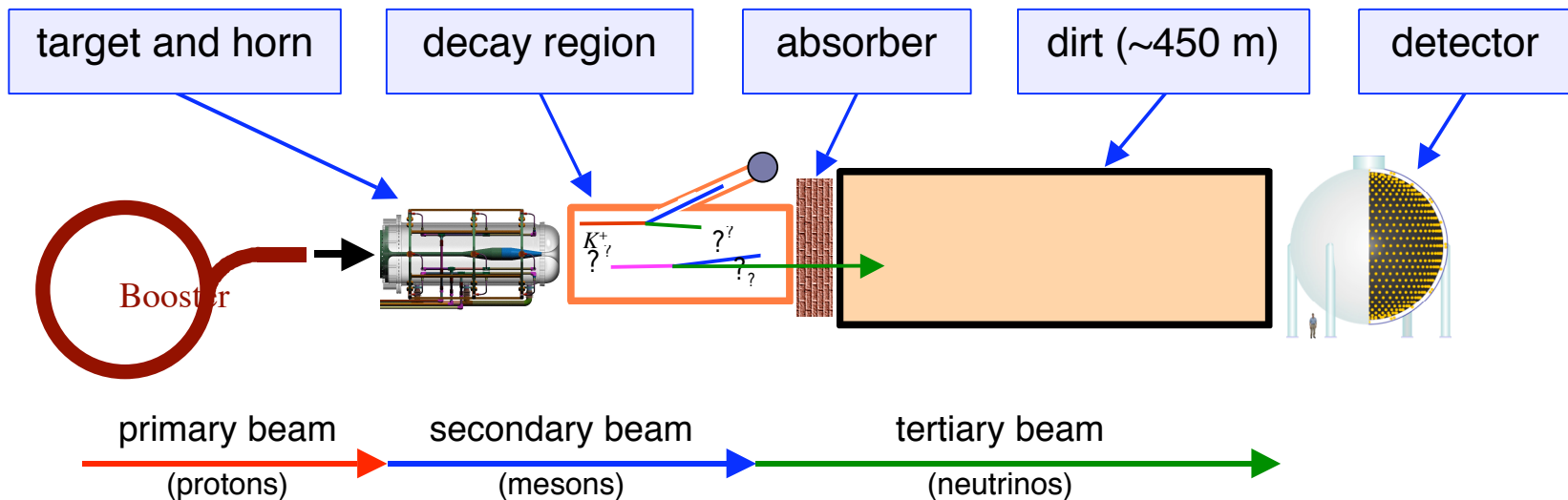
And  
 $1\text{E-}5 + 1\text{E-}3 \neq 1$



There have now been follow-up experiments,  
looking for the same appearance signal  
and also looking for disappearance at high  $\Delta m^2$

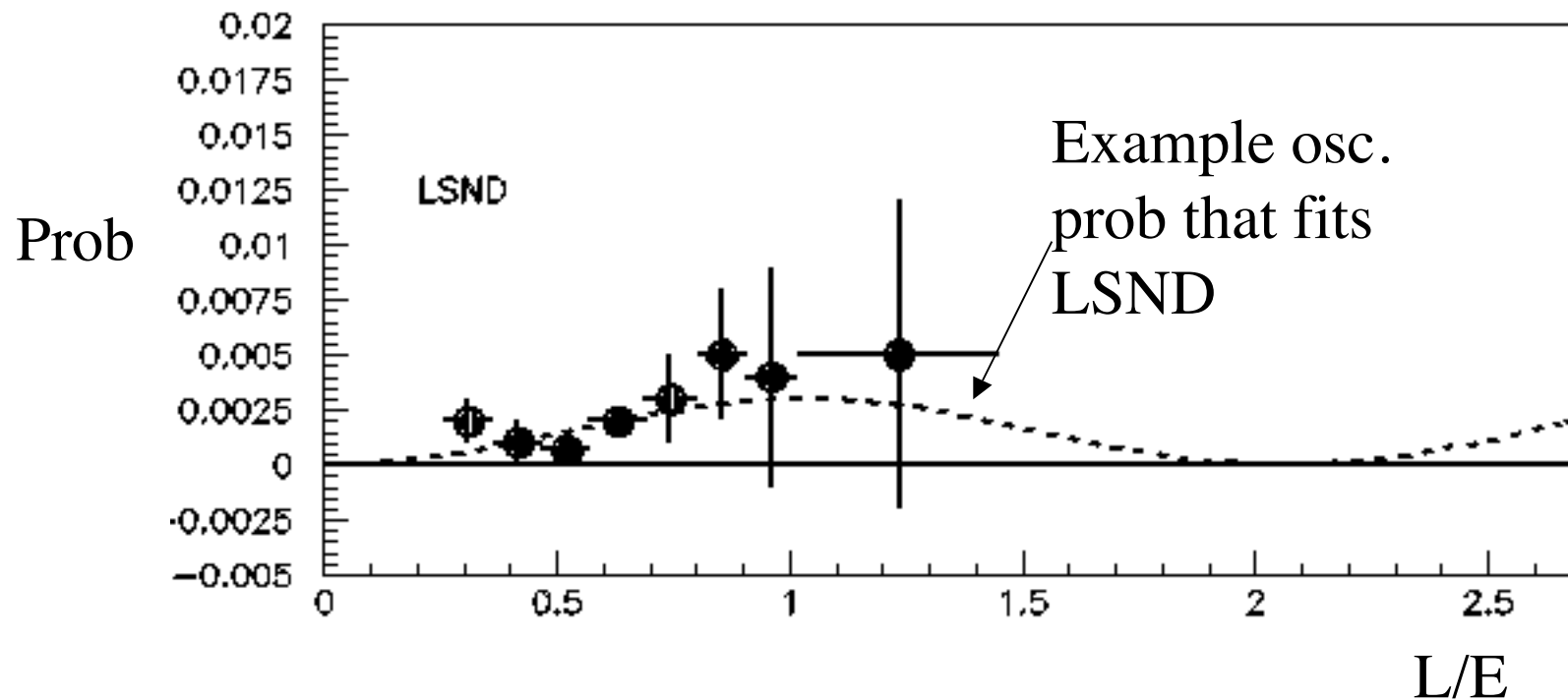
$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E)$$

Keep  $L/E$  same while changing systematics



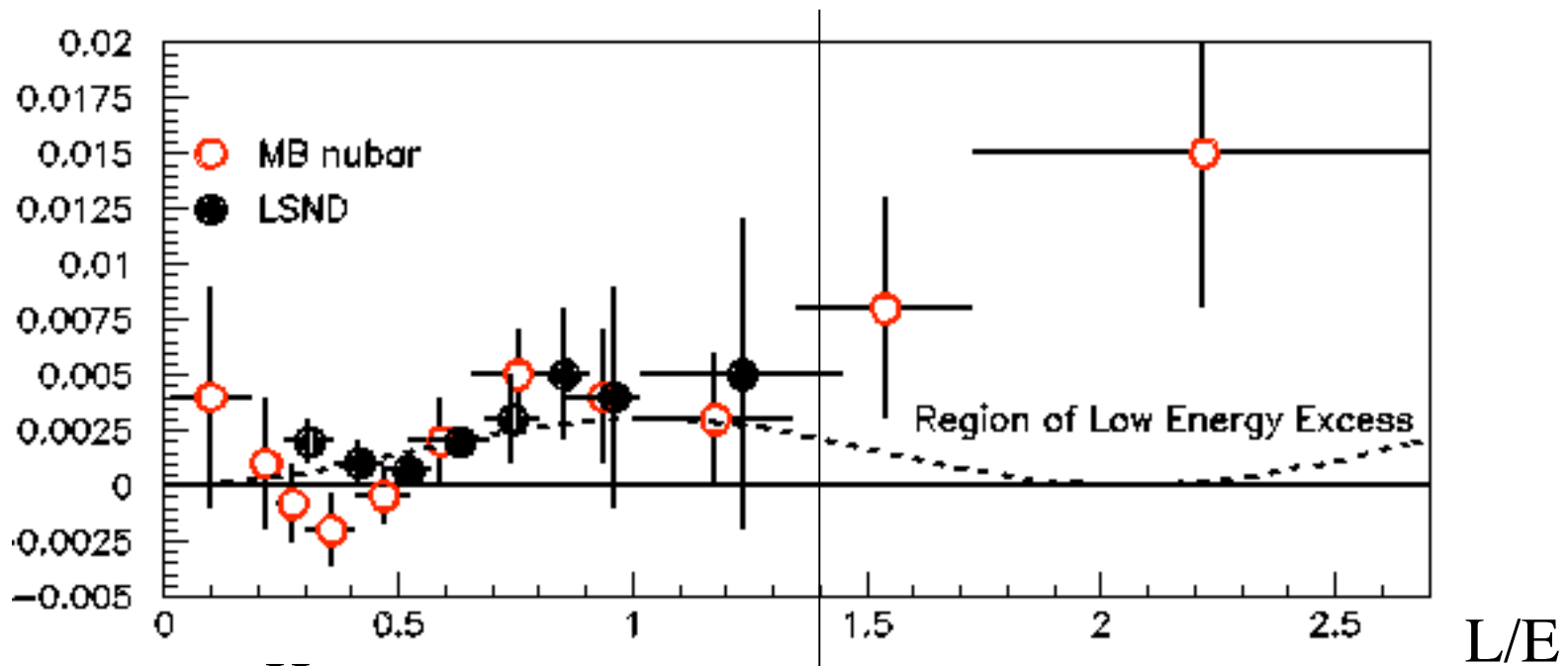
MiniBooNE

To compare LSND to other experiments, that will have different beam energies and distances, convert the excess into an oscillation probability bin-by-bin...



Now lets add results from MiniBooNE,  
with different L and E but same L/E ratio...

### Antineutrino data first

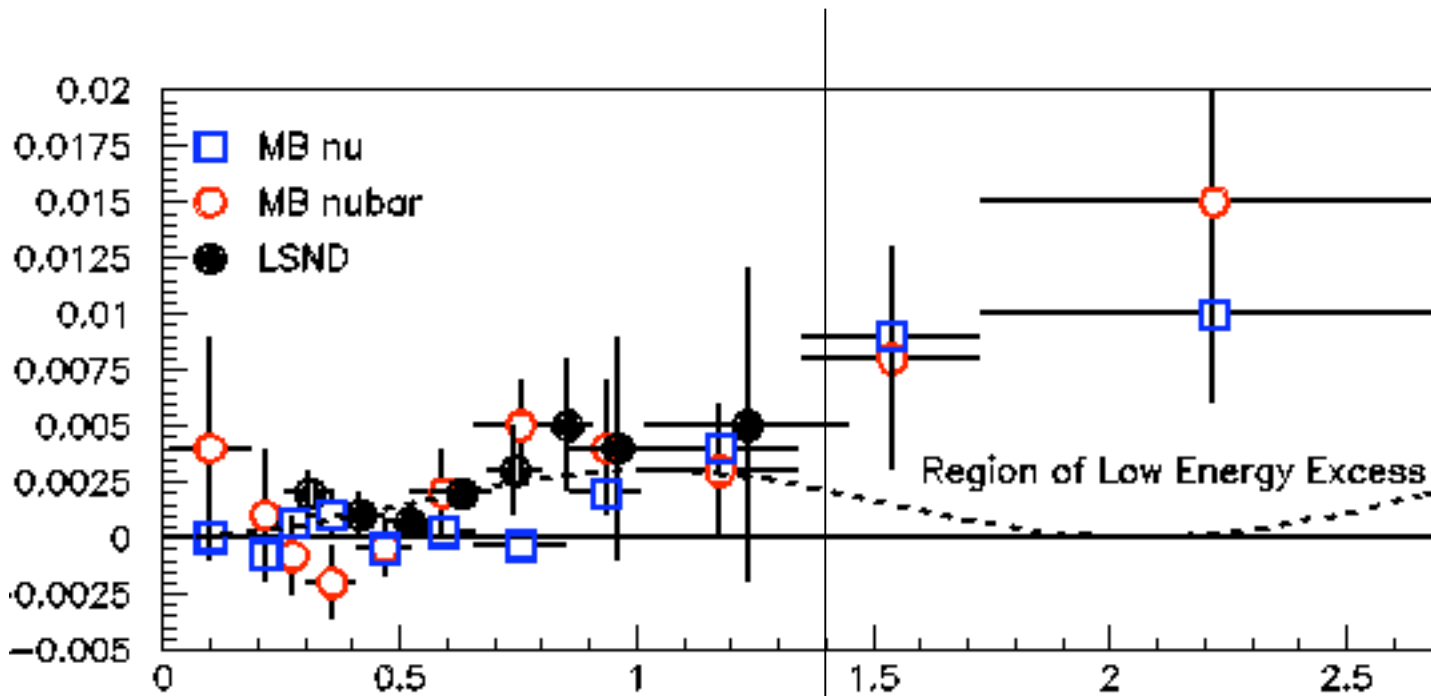


Hmmm...  
similar in this range.

What's going on here  
where LSND had no data?



But the neutrino data shows no oscillation in the LSND-region!



Flat and consistent  
with zero

But shows the same  
strange rise...

The issue is murky...

LSND (antineutrino) is the only  $>3\sigma$  signal

MiniBooNE has an  $\sim 2\sigma$  signal in antineutrino mode  
and no signal in neutrino mode.

Hot off the press: The reactor data (antineutrino) seems to be  
indicating disappearance  
in an overlapping  $\Delta m^2$  range,  
at  $2.7\sigma$

Putting these together with all other results  
(neutrino and antineutrino), it is very hard to fit in models!

We just had a terrific workshop,  
that reviewed all of these results and opportunities...

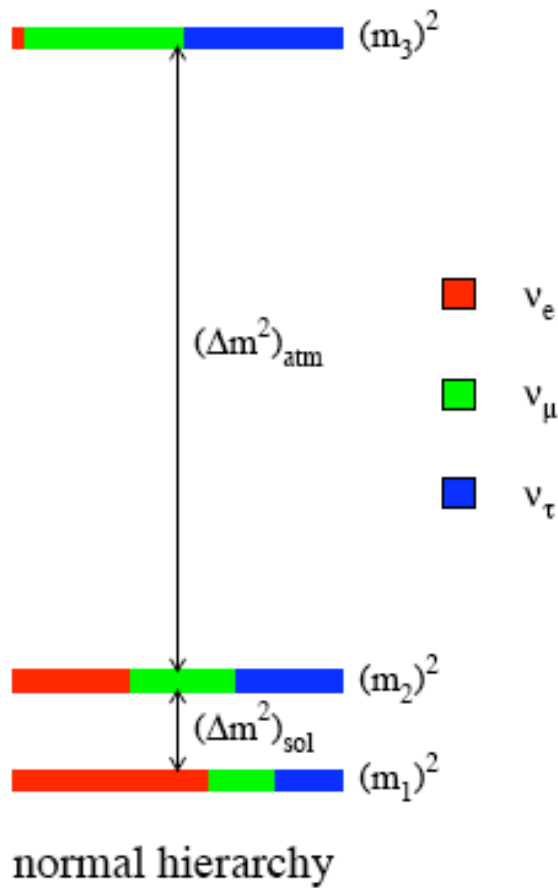
Short Baseline Neutrino Workshop -- SBNW11

<https://indico.fnal.gov/conferenceDisplay.py?confId=4157>

There are interesting opportunities here!

But for our discussion,  
lets leave this and go back to  
the atmospheric and solar oscillations.

Let's try to make a model...



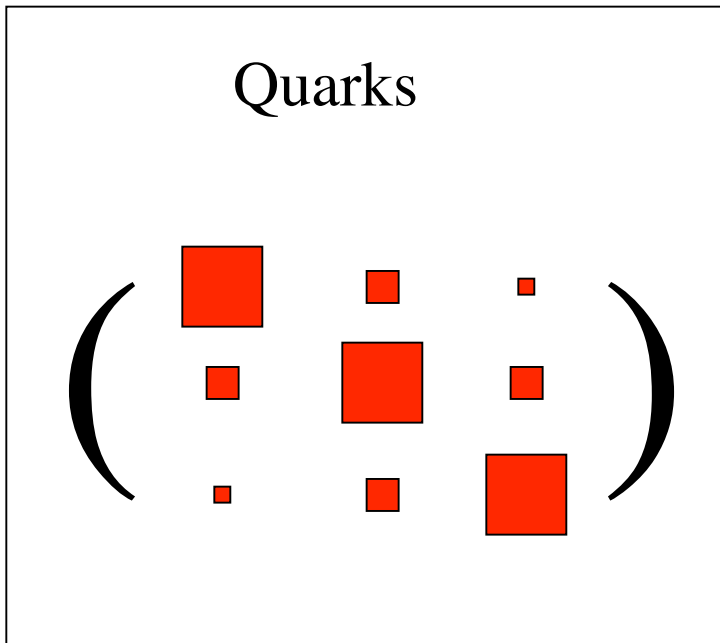
## Our Model

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

“mixing” between neutrinos  
is parameterized by  
three “mixing angles”

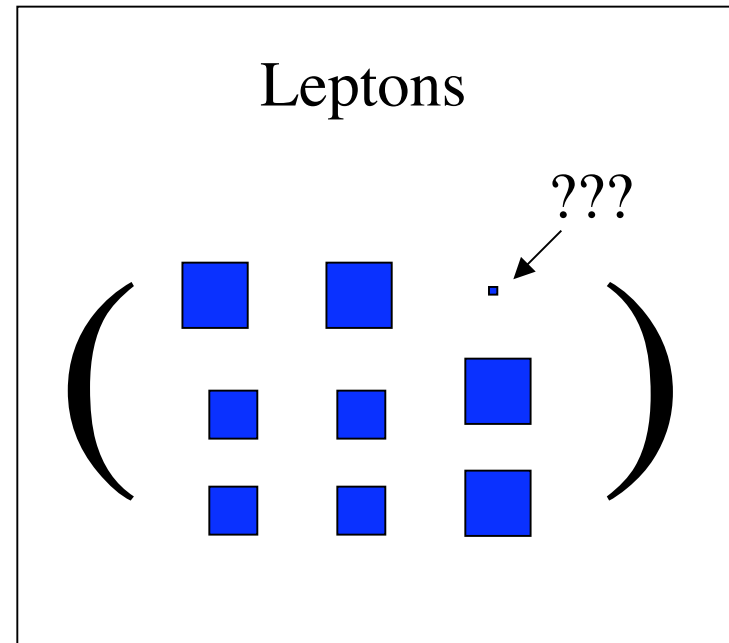
$$\theta_{12}, \theta_{13}, \theta_{23}$$

# What we know about mixing



Large entries on diagonal  
small off diagonal

vs.



Moderately large entries  
except for one,  
which might be zero!



From last week's SSI lecture

## The CP Violation Parameter

$$c_{ij} = \cos\theta_{ij}$$

$$s_{ij} = \sin\theta_{ij}$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

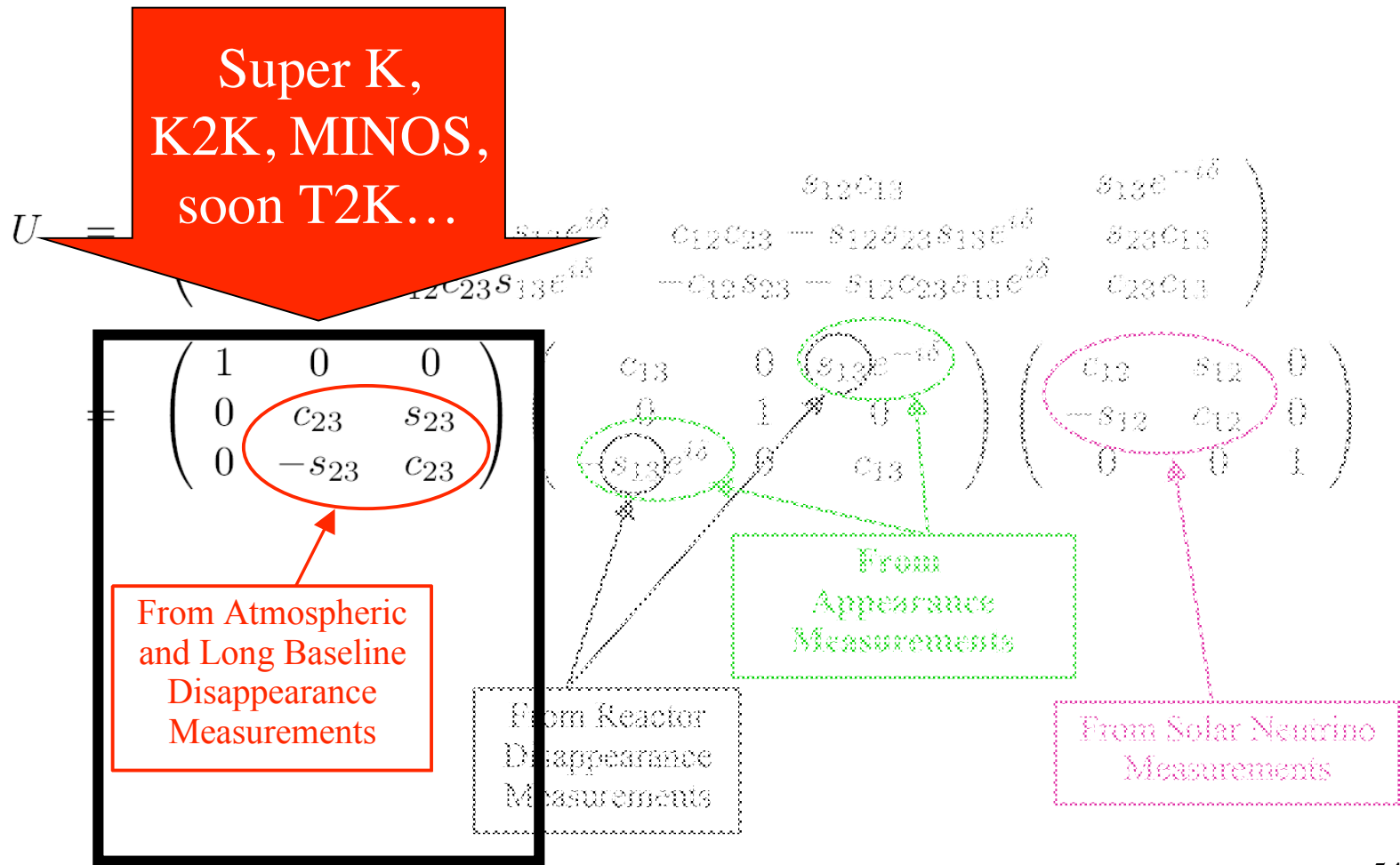
From Atmospheric  
and Long Baseline  
Disappearance  
Measurements

From Reactor  
Disappearance  
Measurements

From  
Appearance  
Measurements

From Solar Neutrino  
Measurements

This matrix is well-known



& this matrix is well-known

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & 0 \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{13}e^{i\delta} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{13}e^{i\delta} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Super K,  
SNO,  
KamLAND

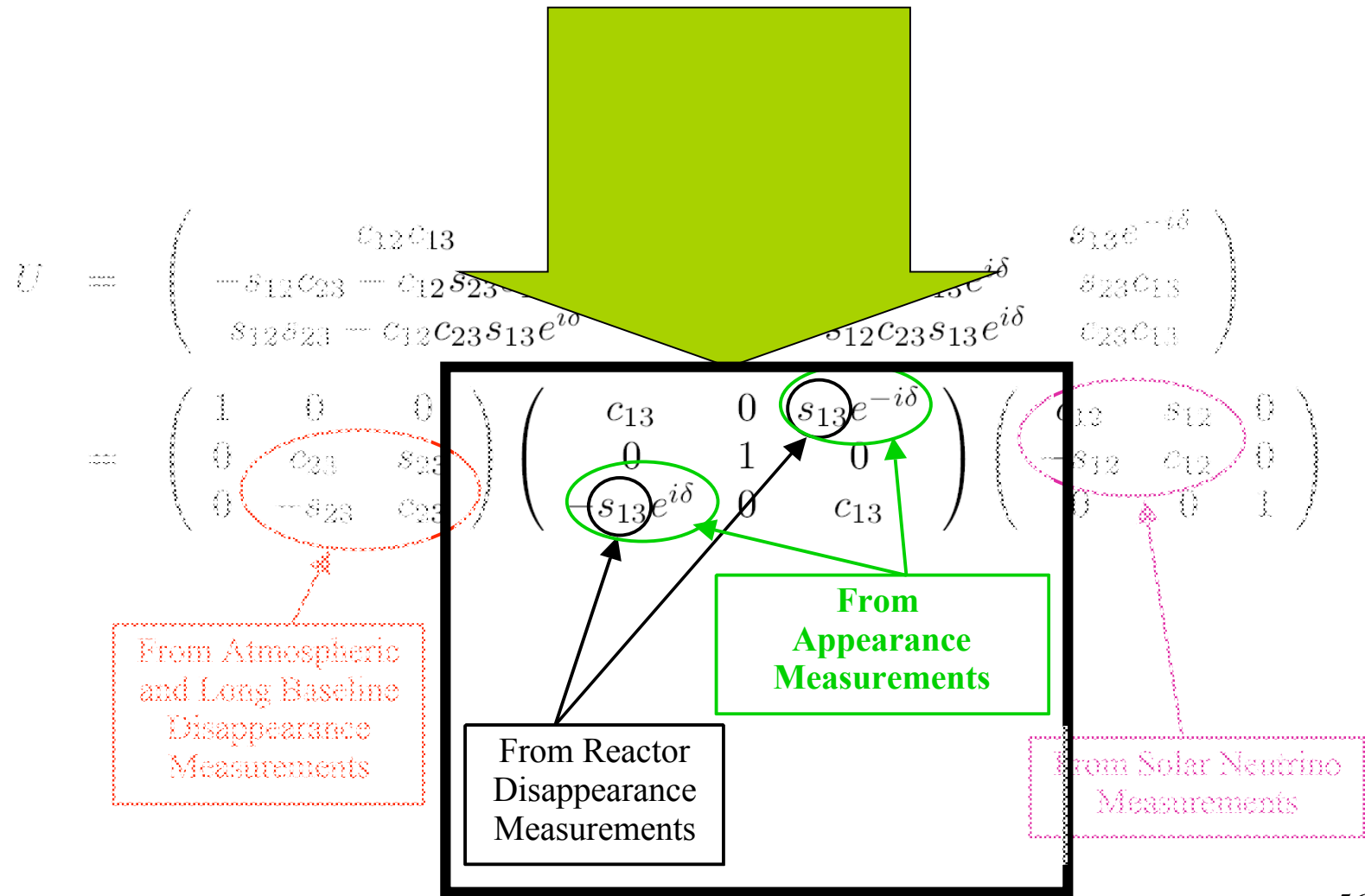
From Atmospheric  
and Long Baseline  
Disappearance  
Measurements

From Reactor  
Disappearance  
Measurements

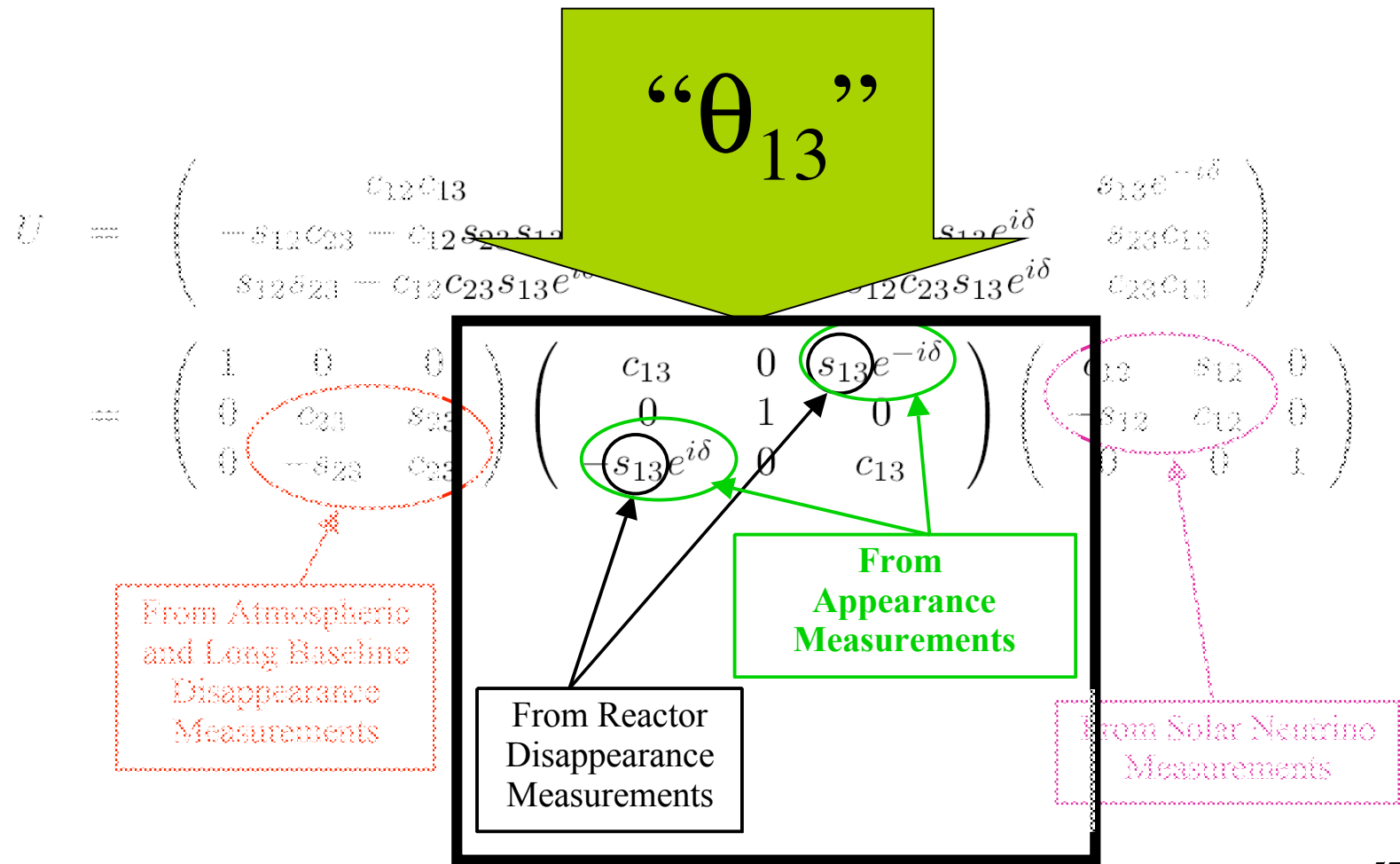
From  
Appearance  
Measurements

From Solar Neutrino  
Measurements

But this one is not known  
at all!

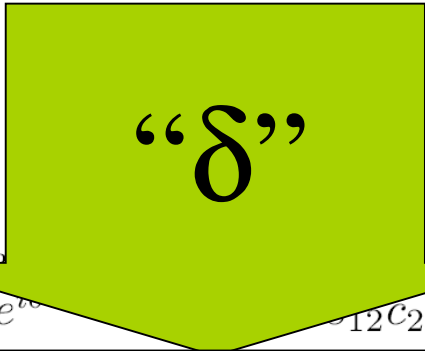


Many experiments are searching for the last mixing angle



We'll discuss both parameters more in the next lecture!

As well as ...



“ $\delta$ ”

$$U = \begin{pmatrix} c_{12}c_{13} & s_{13}e^{-i\delta} & s_{12}c_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}\delta_{23} - c_{12}c_{23}s_{13}e^{i\delta} & s_{12}c_{23} + c_{12}s_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

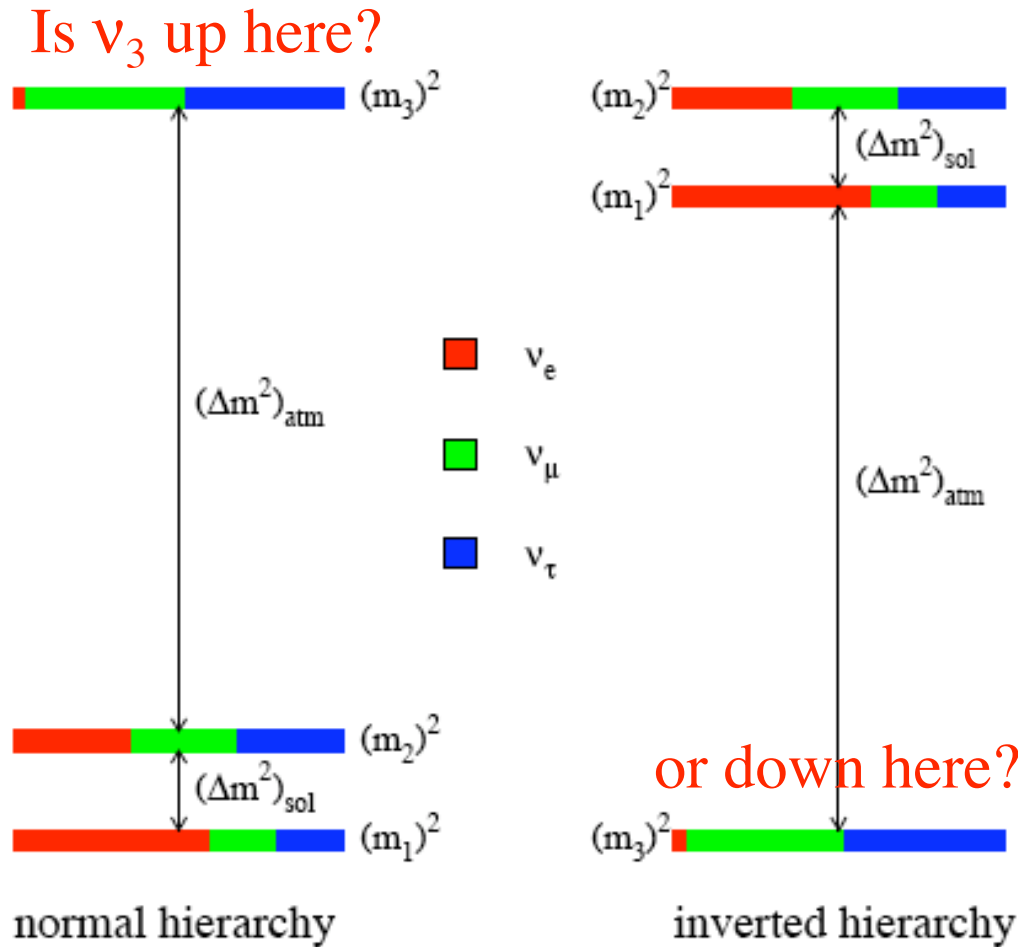
From Atmospheric and Long Baseline Disappearance Measurements

From Reactor Disappearance Measurements

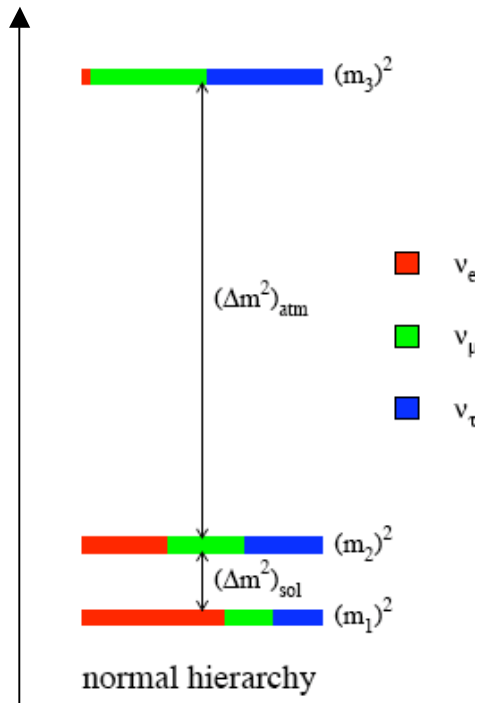
From Appearance Measurements

From Solar Neutrino Measurements

What do we not know about the masses?  
The hierarchy:



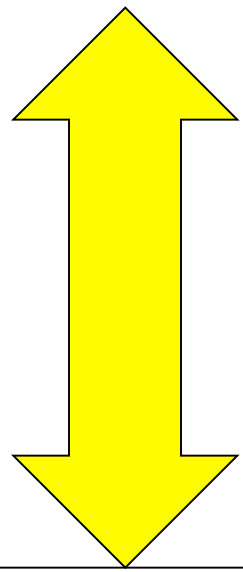
we know the order of these two from the solar neutrino morphing model



And now in our model,  
 the mass an experiment like KATRIN measures  
 is much more complicated

$$\langle m_\beta \rangle^2 = \sum_j m_j^2 |U_{ej}|^2 = m_1^2 |U_{e1}|^2 + m_2^2 |U_{e2}|^2 + m_3^2 |U_{e3}|^2$$

And we do not know the offset!



The smallest that the neutrino masses  
 can possibly be, is the case where  
 the lowest state is exactly zero  
 (which would be weird)

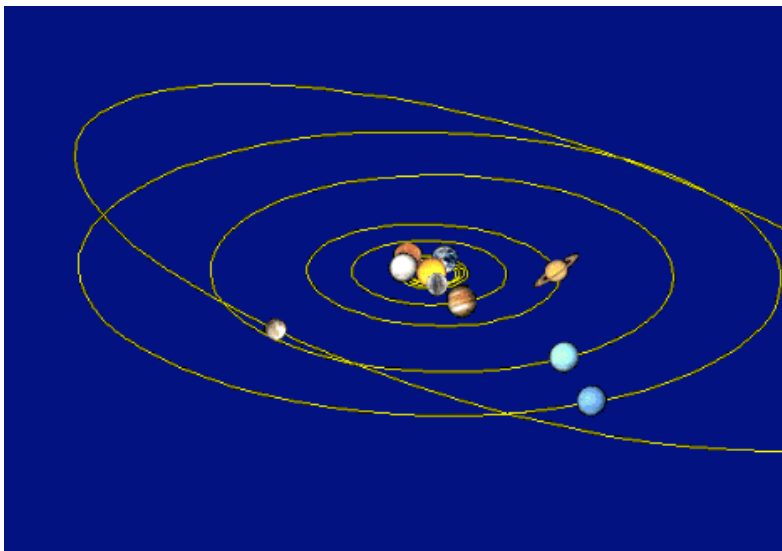


Just to be provocative....

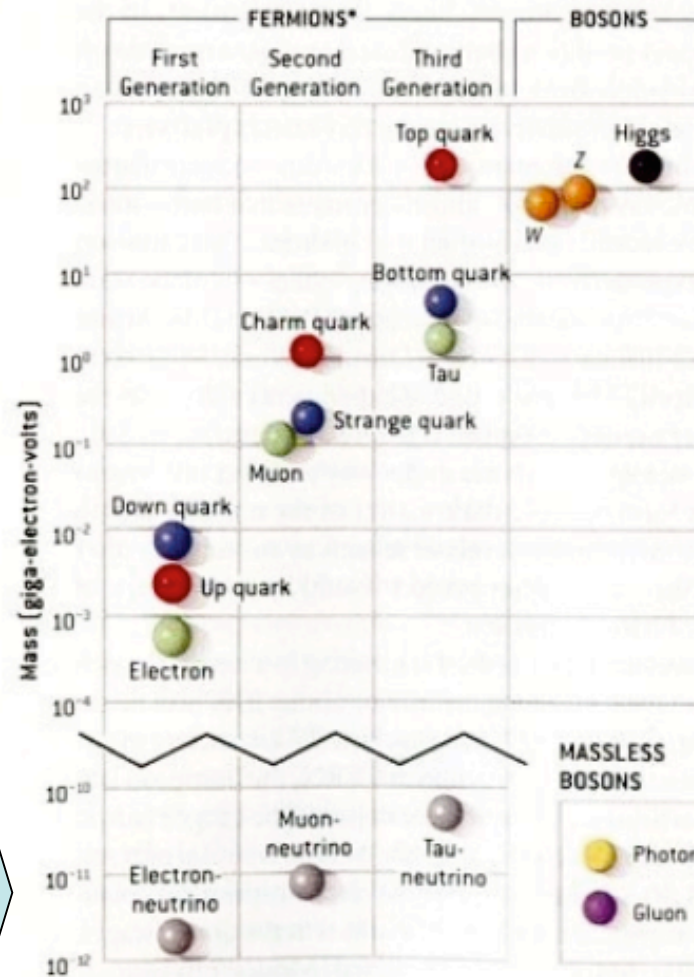
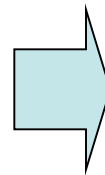
Does the smallness of the mass *really* mean anything?

Or is the smallness an accident of a huge range of choices?

Like the orbits of planets?



mass if you just take  
 $\sqrt{\Delta m^2}$  as the mass





Can we make a “nu” Standard Model?



Theoretical

Theory

Experiment

1. Neutrinos are Majorana
2. And have CP violation
3. and GUT scale partners

Three happy theoretical consequences:

- 1) You get a neutrino which is apparently very light, even though  $m_\nu \sim$  other lepton masses...
- 2) You get a natural connection to GUT models
- 3) There is a mechanism for leptogenesis

1. Neutrinos are Majorana
2. And have CP violation
3. and GUT scale partners

Three happy theoretical consequences:

- 1) You get a neutrino which is very light
- 2) You get a natural connection to GUT models
- 3) There is a mechanism for leptogenesis

# What's a Majorana neutrino?

The spin defines particle vs. antiparticle



This is the antiparticle



and this is the particle

... but it is all the same “thing”

A simple solution to the handedness problem in the theory! <sup>66</sup>

This is only possible if there is no charge  
that distinguishes a particle vs antiparticle



Clearly not  
true in EM!

Also not true  
for the strong force.

But possibly true  
of the weak force!

## Our Model:

1. Neutrinos are Majorana
2. **And have CP violation**
3. and GUT scale partners



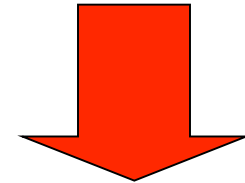
## Recall from the lecture on CP-violation

Any  $3 \times 3$  unitary matrix has

3 associated free parameters (Euler angles)

$$c_{ij} = \cos\theta_{ij} \quad s_{ij} = \sin\theta_{ij}$$

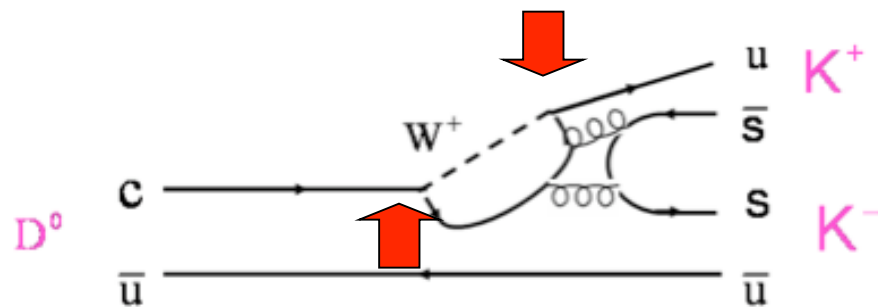
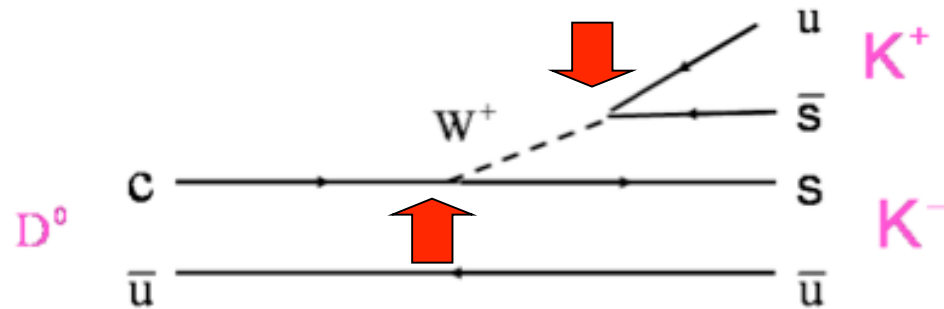
& can have a complex phase hidden in it!



$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix},$$

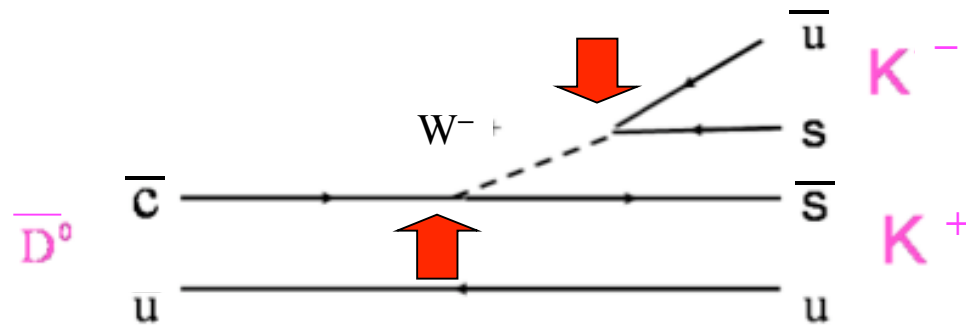
This “CP violating phase” can lead to a different decay rate  
for matter vs. antimatter

The effect shows up in weak decays  
when you have 2 paths to the same outcome...



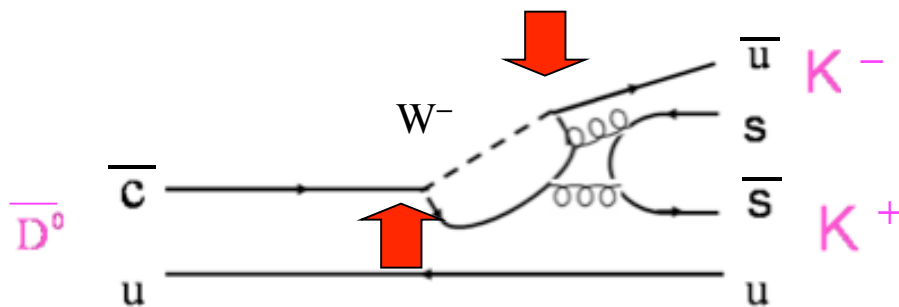
You will get an interference term  
in the decay probability...

Now consider the  $\overline{D}^0$



There are still 2 paths to the outcome.

Compared to the D<sup>0</sup>  
the interference  
term changes sign!



e.g. D<sup>0</sup> and  $\overline{D}^0$  decays can have different decay rates  
if  $\delta$  is nonzero!

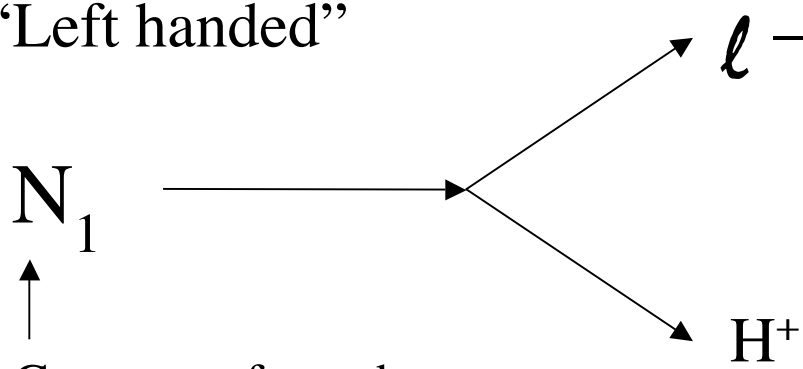
## Our Model:

1. Neutrinos are Majorana
2. And have CP violation
3. and GUT scale partners

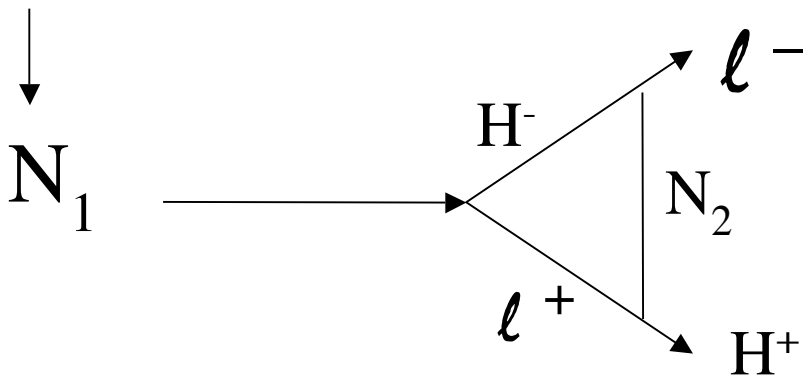
Lets say neutrinos have VERY heavy partners,  
and those partners can decay,  
and that a **phase** appears in the loops associated  
with the decay...

Before the electroweak phase transition...

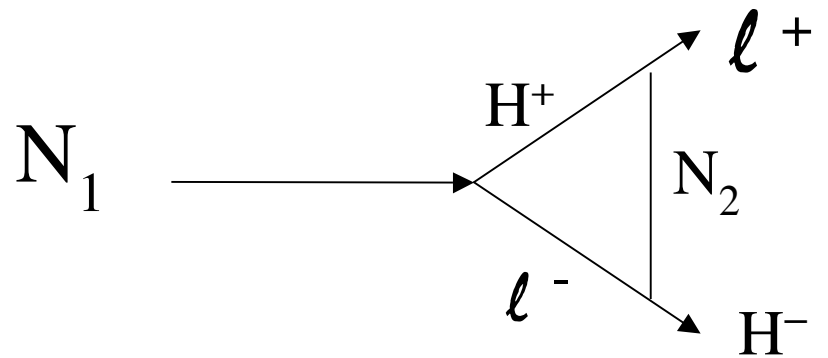
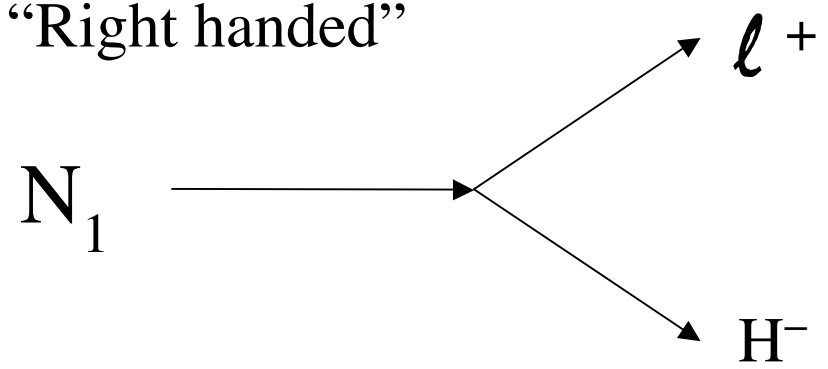
“Left handed”



Gets mass from the Majorana term



“Right handed”

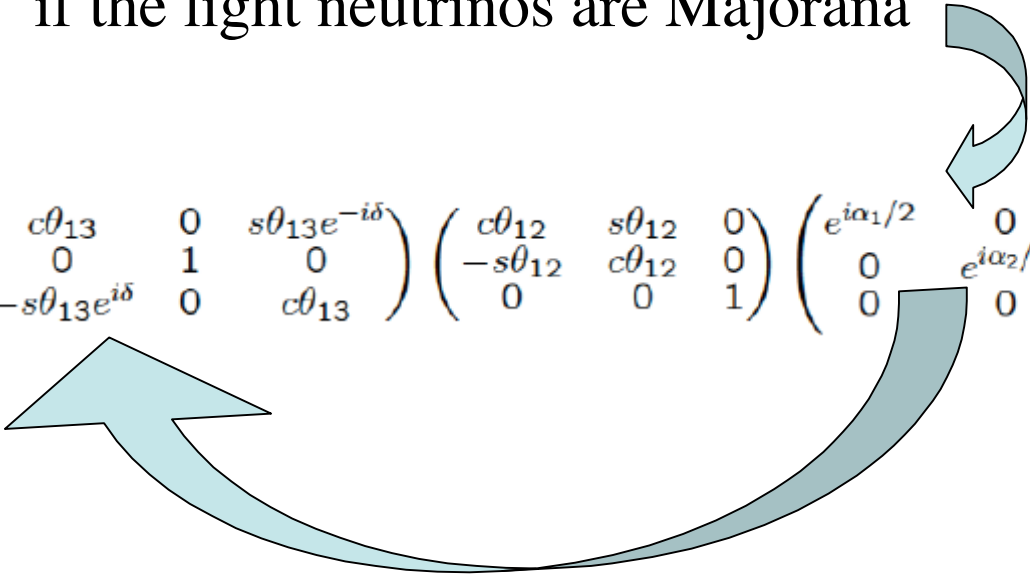


The interference terms will have opposite sign!

(This should tie back to your SSI lectures on Leptogenesis)

This phase is a “Majorana Phase”

A similar Majorana phase would appear in U  
if the light neutrinos are Majorana

$$U_{\alpha j} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c\theta_{23} & s\theta_{23} \\ 0 & -s\theta_{23} & c\theta_{23} \end{pmatrix} \begin{pmatrix} c\theta_{13} & 0 & s\theta_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s\theta_{13}e^{i\delta} & 0 & c\theta_{13} \end{pmatrix} \begin{pmatrix} c\theta_{12} & s\theta_{12} & 0 \\ -s\theta_{12} & c\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$


And in most theories, if the  $\alpha$ 's are nonzero  
then  $\delta$  is nonzero...

*A great topic for young theorists:*

*understanding the connections better, making them predictive* 75

Connecting the circle back to light neutrino mass....

If the neutrino is Majorana, then  
the result is new “mass-like” terms in the Lagrangian

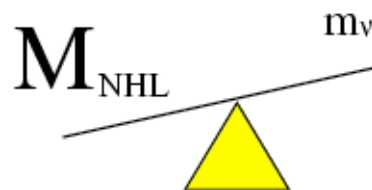
▷ Dirac Mass terms like  $m(\bar{\psi}_L\psi_R + \dots)$

▷ and things which look like:

$$(M_L/2)(\bar{\psi}_L^c\psi_L) + (M_R/2)(\bar{\psi}_R^c\psi_R) + \dots$$

“Majorana mass terms”

This provides a natural explanation for tiny neutrino masses,  
through mixing with the heavy partner  
(The same heavy partner responsible for leptogenesis)



- $\mu_{light} \approx m_\nu^2/M$

- $\mu_{heavy} \approx M$



Proof of this “New Paradigm” will be circumstantial for a while...

It will be a long, long time,  
before experiments are sensitive to GUT scale particles.

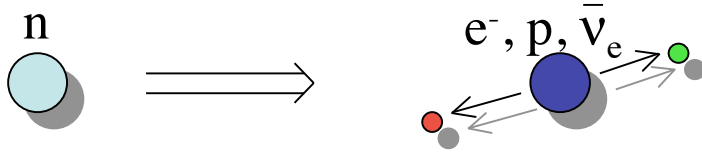
But...

You can have modified seesaw models that invoke  
particles at LHC scales!

You can look for CP violation in the light neutrinos ( $\delta$ )  
because this is expected to be connected to the  $\alpha$ 's

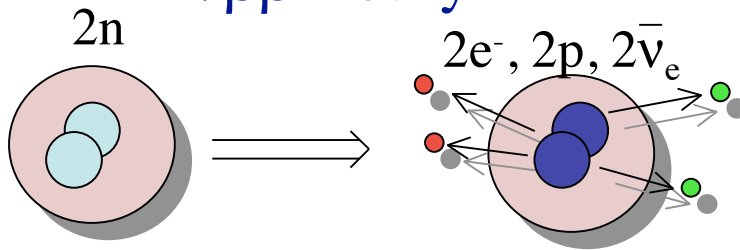
You can test if neutrinos are Majorana...

## Single $\beta$ Decay



Half-life: About 10 minutes

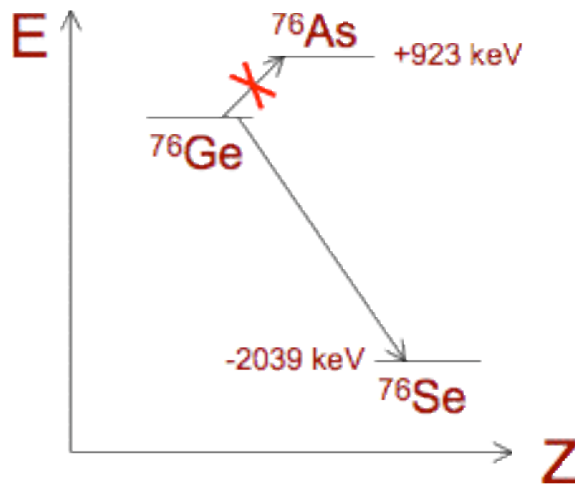
## $2\nu\beta\beta$ Decay



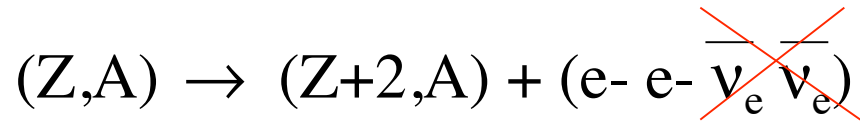
Can occur if single  $\beta$  decay is energetically forbidden

Half-life:  $10^{18-24}$  years

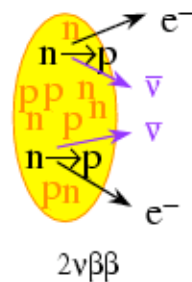
$^{48}\text{Ca}$ ,  $^{76}\text{Ge}$ ,  $^{82}\text{Se}$ ,  $^{96}\text{Zr}$ ,  
 $^{100}\text{Mo}$ ,  $^{116}\text{Cd}$ ,  $^{128}\text{Te}$ ,  $^{130}\text{Te}$ ,  
 $^{150}\text{Nd}$ ,  $^{238}\text{U}$ ,  $^{242}\text{Pu}$



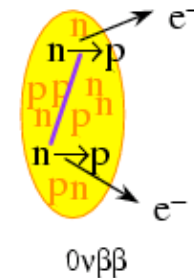
# Neutrinoless Double Beta Decay



Nuclei that do this...

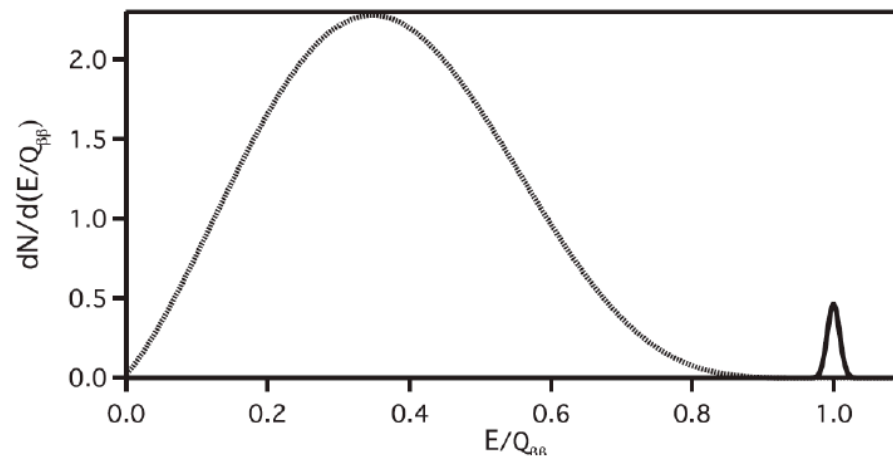


Can sometimes also do this



*IF* neutrinos are their own antiparticles

The tell-tale signature is in the electron energy spectrum:



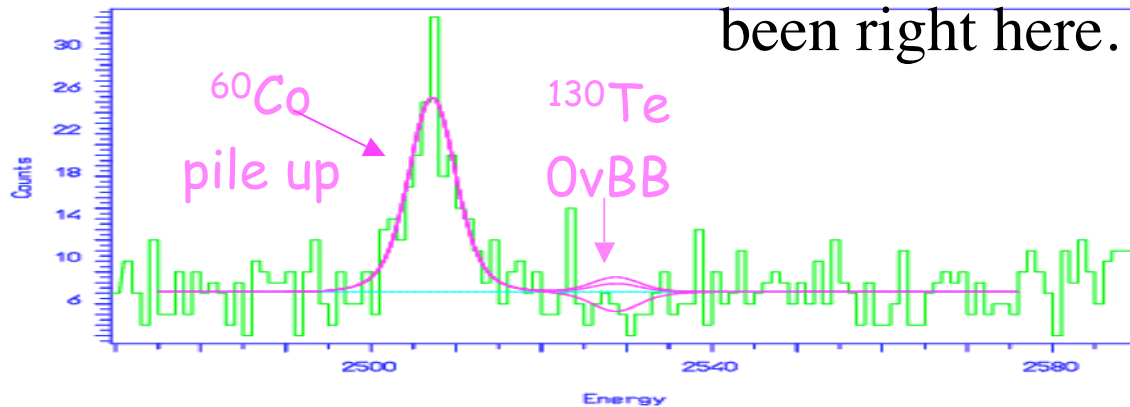
The Q-value of the decay tells you exactly where to look

Knowing where to look is crucial to rejecting backgrounds!

e.g. results from Cuoricino

This peak is  
a background

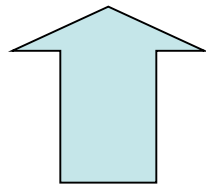
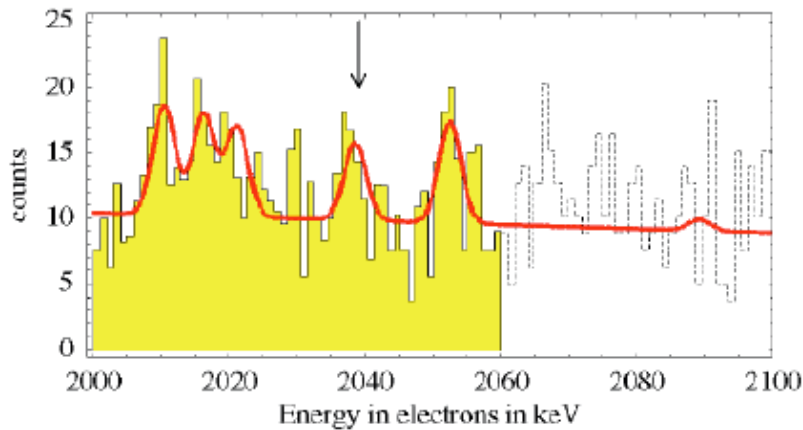
If a signal had been  
seen it would have  
been right here.



From this, Cuoricino sets a limit on this process

# A controversial result! The Heidelberg-Moscow Signal

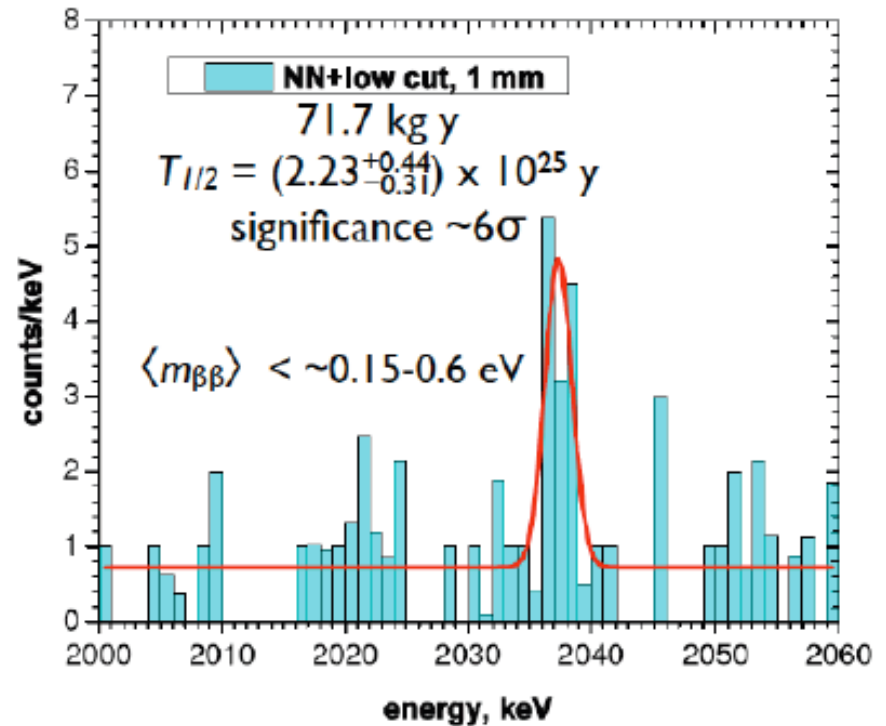
The first result:



This is where  $0\nu\beta\beta$  says there should be a peak...

The final analysis had cuts to eliminate backgrounds:

Klapdor Kleingrothaus et al., *Mod. Phys. Lett. A* **21** (2006) p 1547.



The lifetime for this process is given by:

$$\frac{1}{T_{1/2}^{0\nu}} = G^{0\nu}(E_o, Z) |M^{0\nu}|^2 \left| \langle m_{\nu, \beta\beta} \rangle \right|^2$$

The phase space factor  
( $3 \times 10^{-26}/\text{y}$  in Ge)

$$|M^{0\nu}|^2 = \left| M_{GT}^{0\nu} - \left( \frac{g_V}{g_A} \right)^2 M_F^{0\nu} \right|^2$$

The nuclear matrix element,  
can be calculated at some level,  
can be measured from  
excited states of  $2\nu\beta\beta$

$$\left| \langle m_{\nu, \beta\beta} \rangle \right| = \left| \sum_i \lambda_i^{CP} m_i |U_{ei}^L|^2 \right|$$

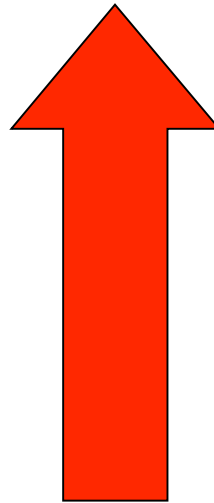
Weights the mass w/ the mixing  
(what's the contribution from  
the  $\nu_e$ ?)

From this you can see why measuring the Majorana CP violation phases ( $\phi_1, \phi_2$ ) is very difficult...

$$\frac{1}{T_{1/2}^{0\nu}} = G^{0\nu}(E_o, Z) |M^{0\nu}|^2 \left| \langle m_{\nu, \beta\beta} \rangle \right|^2$$



You need to compare the measured lifetime to the predicted lifetime,



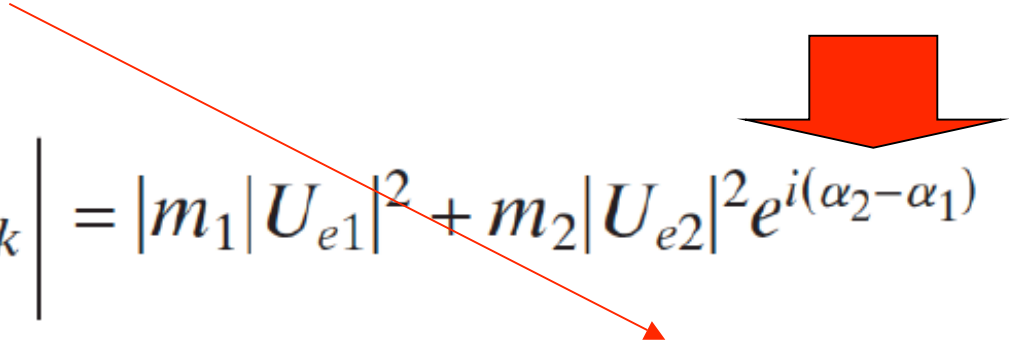
Where this term is predicted from the light neutrino mixing matrix...

The problem is here!

This has theoretical errors  $\sim \times 2$  !!!

## Allowing for CP Violation...

$$U_{\alpha j} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c\theta_{23} & s\theta_{23} \\ 0 & -s\theta_{23} & c\theta_{23} \end{pmatrix} \begin{pmatrix} c\theta_{13} & 0 & s\theta_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s\theta_{13}e^{i\delta} & 0 & c\theta_{13} \end{pmatrix} \begin{pmatrix} c\theta_{12} & s\theta_{12} & 0 \\ -s\theta_{12} & c\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

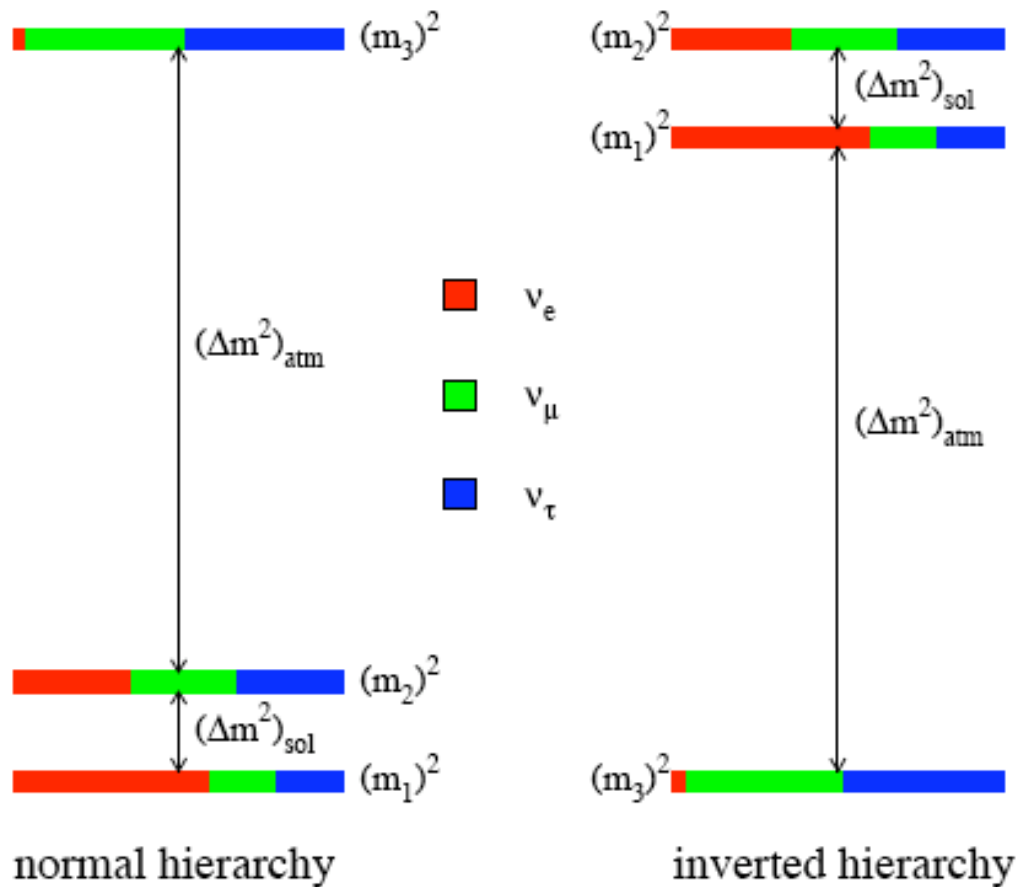
$$\langle m_{\beta\beta} \rangle \equiv \left| \sum_k m_k U_{ek}^2 \right| = |m_1|U_{e1}|^2 + m_2|U_{e2}|^2 e^{i(\alpha_2 - \alpha_1)} + m_3|U_{e3}|^2 e^{i(-\alpha_1 - 2\delta)}$$


Complementary to what you measure in direct searches, like Katrin (or infer from cosmology)...

$$\langle m_{\beta} \rangle^2 = \sum_j m_j^2 |U_{ej}|^2 = m_1^2 |U_{e1}|^2 + m_2^2 |U_{e2}|^2 + m_3^2 |U_{e3}|^2$$

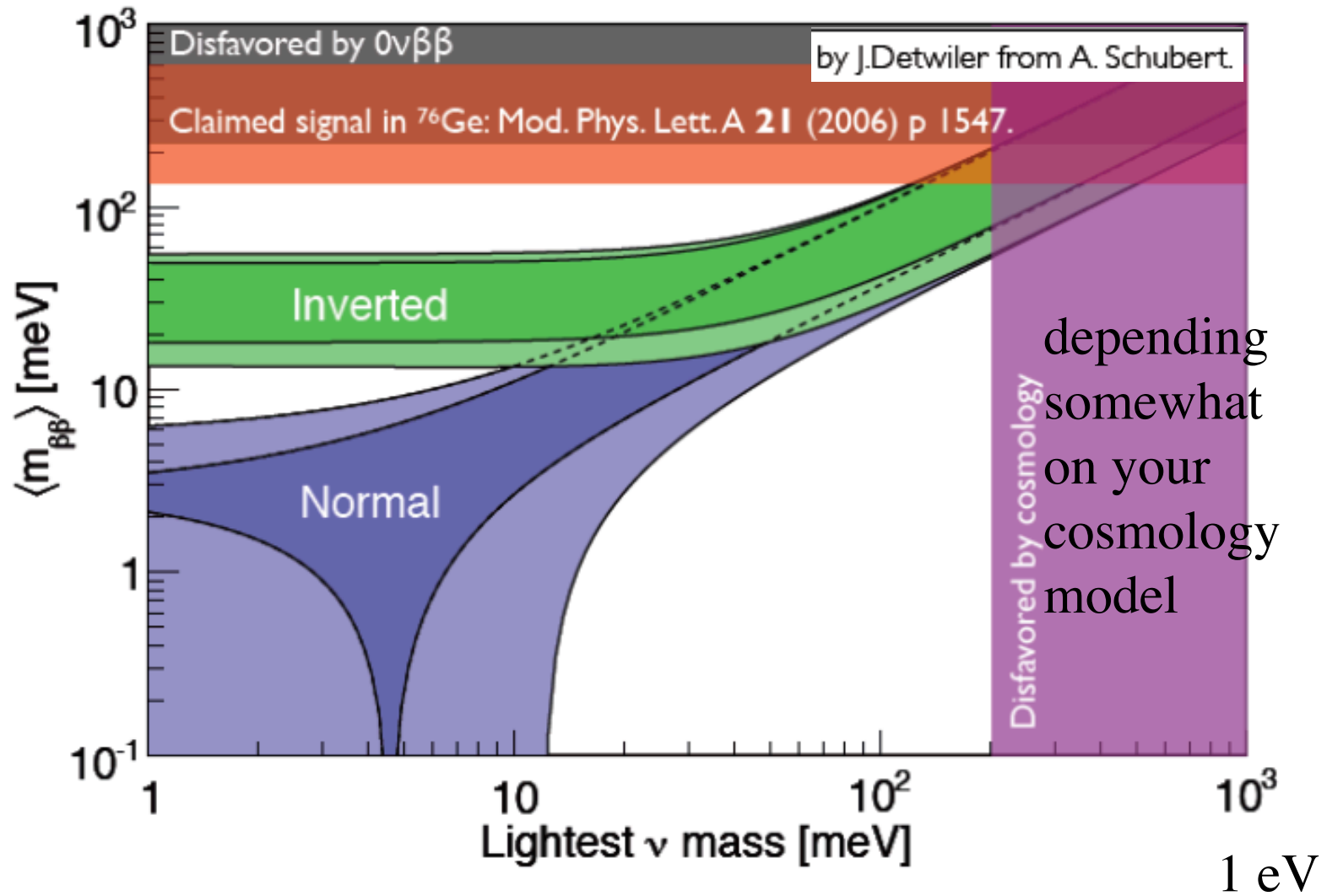


In  $0\nu\beta\beta$ , having the inverted hierarchy really helps the search!

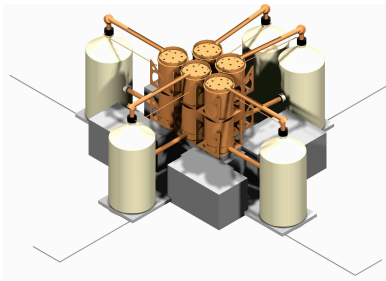


It means a lot of electron flavor in the highest mass state!

# Where we are at right now...



$0\nu\beta\beta$  is a big industry for the future!



GERDA: Bare Ge crystals in LN

CUORE:  $\text{TeO}_2$  crystal bolometer

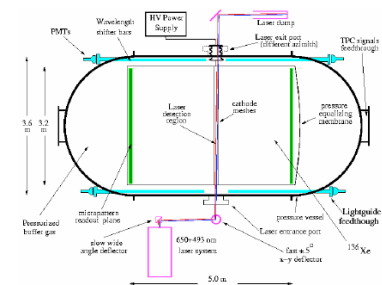
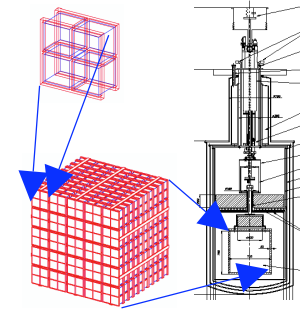
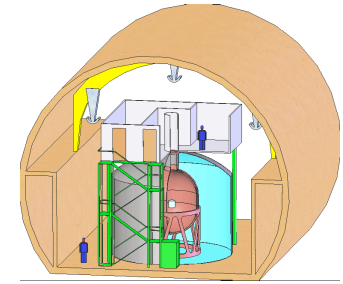
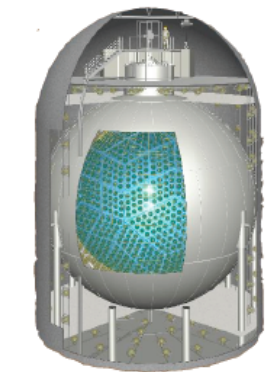
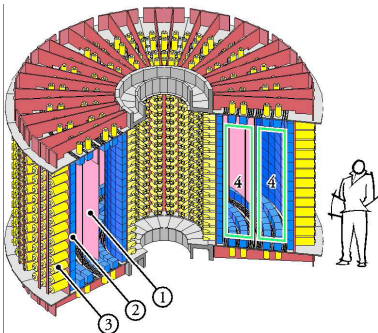
EXO: Liquid Xenon with Ba tagging

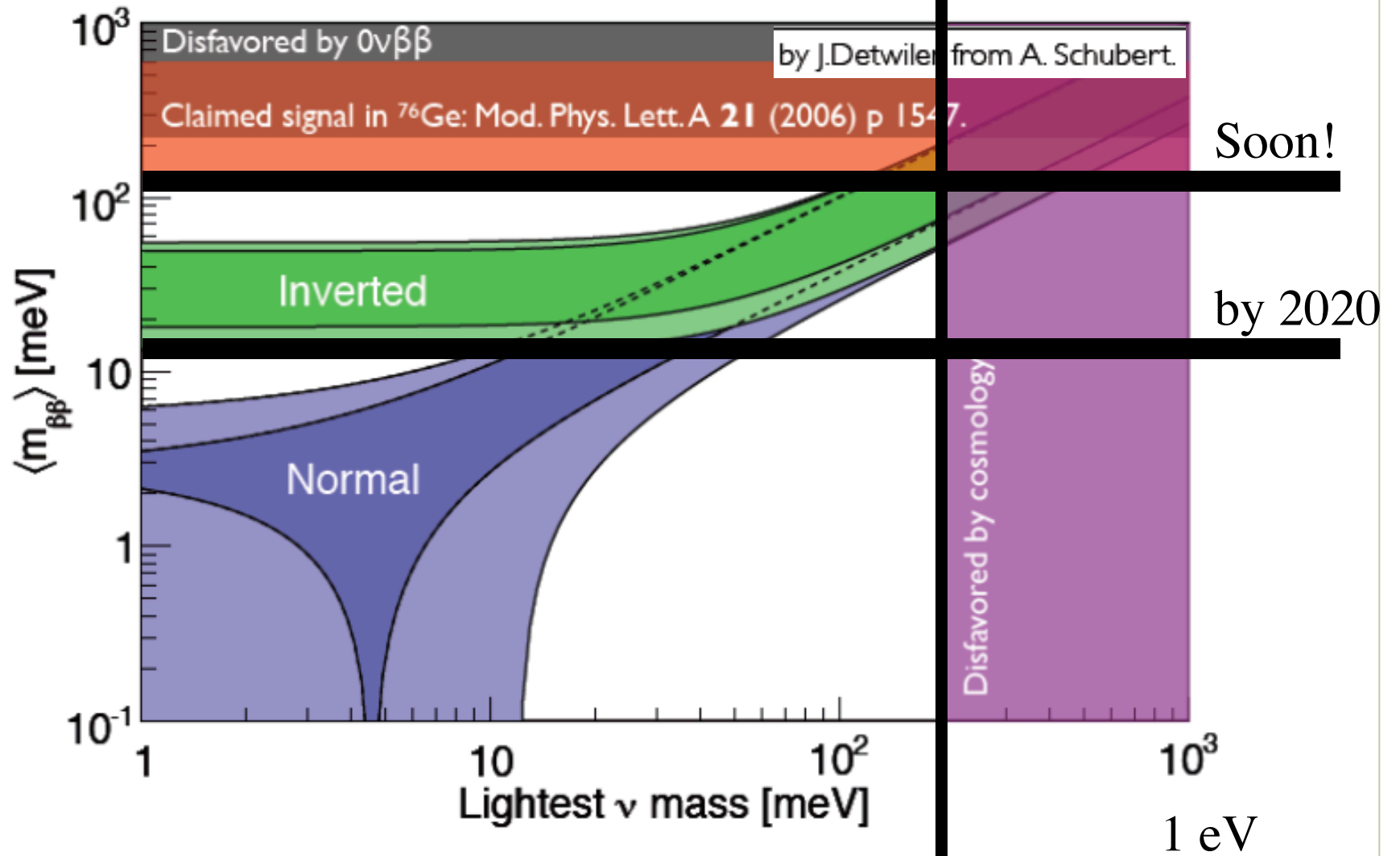
XEN: KamLAND w/ Xe gas

SuperNemo: Many types of foils,  
with tracking and scintillator

Majorana: Ge detector in a cryostat

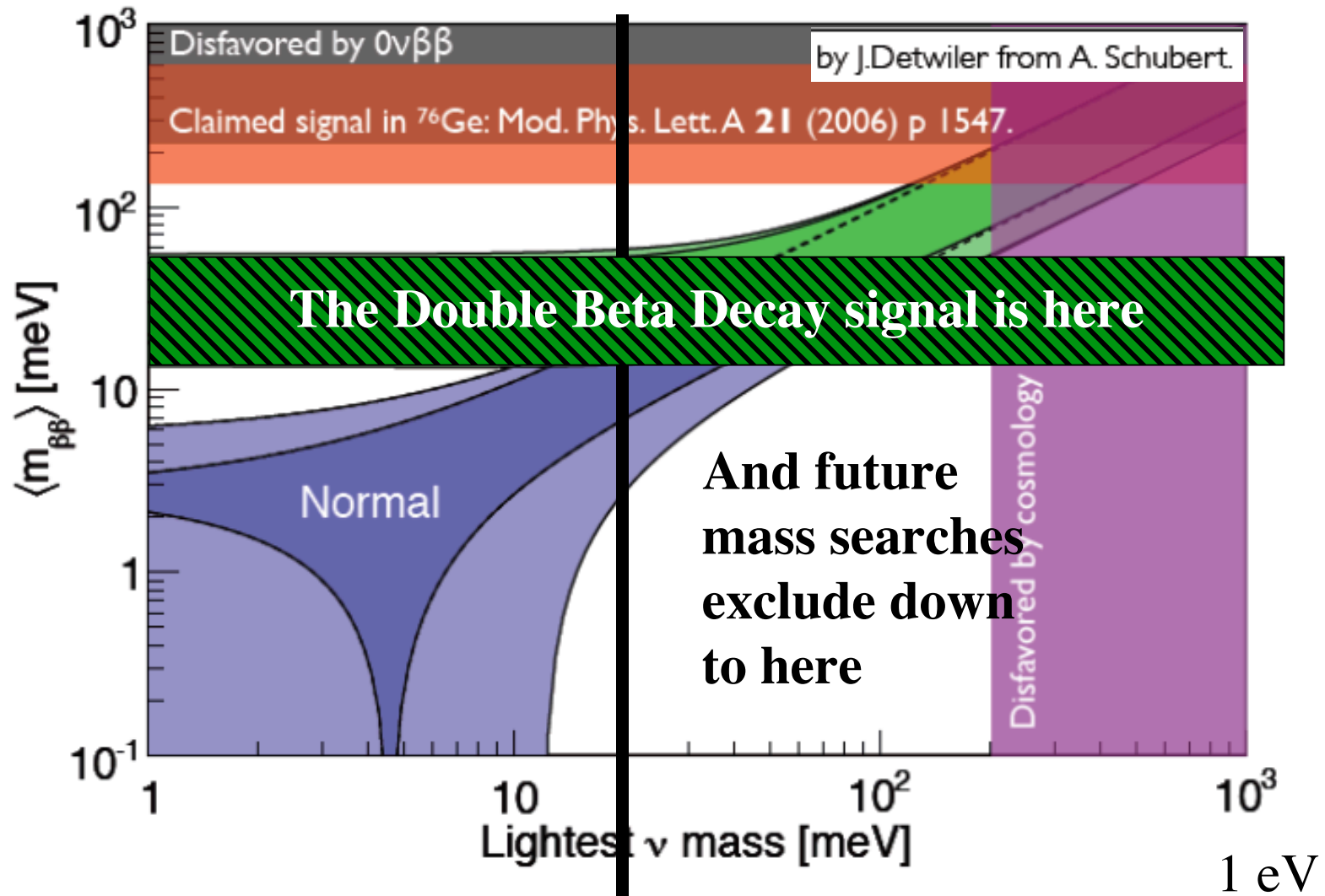
...BUT WAIT! THERE'S MORE!!!  
TOO MANY TO LIST!





Katrin

We can know neutrinos are inverted hierarchy if...



The future experiment to watch: Project 8



Final Thought For This Lecture

My theme:

If I were a graduating student or recent postdoc,  
and considering working in neutrino physics,  
what would I consider working on?

This lecture has pointed out a lot of the theoretical issues  
(Is there a meaning to the mixing matrix?  
to the mass hierarchy? Are there sterile  $\nu$ 's?...  
and some neat neutrino-but-not-oscillation experiments...  
(Solar, Neutrino mass, Double Beta Decay...)

All of these have great prospects for interesting results soon!

Next lecture: more about oscillation experiments.

-- end of Part I --